

# An Adaptive Weight Update Based Supervised Learning Predictive Control Method for PMSM

Sen Hong, Yixiao Luo <sup>✉</sup>, *Member, IEEE*, Kai Yang <sup>✉</sup>, *Senior Member, IEEE*, Shuangxia Niu, *Senior Member, IEEE*, and Jincheng Yu <sup>✉</sup>, *Member, IEEE*

**Abstract**—The existing learning-based predictive control methods rely on large amounts of data for offline training. To address this issue, this article proposes a supervised learning-based continuous control set predictive method, which only requires the sampling data at the current time to achieve online updates of the controller, significantly reducing implementation complexity and data requirements. Specifically, the proposed method approximates the ideal input using a radial basis function neural network and updates the weight matrix via gradient descent. Through the derivation of the relationship between state error and tracking error, the tracking error term in the update law is replaced, enabling the online update of the approximator. Considering the inherent approximation error of the neural network and external disturbances, a robust control term is introduced to correct the approximated input. Finally, the proposed method is validated on an experimental platform.

**Index Terms**—Model predictive control (MPC), neural network (NN), permanent magnet synchronous motor (PMSM), supervised learning.

## I. INTRODUCTION

MODEL predictive control (MPC) has become a widely used strategy for controlling permanent magnet synchronous motors (PMSMs), owing to its advantages such as fast dynamic response and excellent steady-state performance [1], [2]. Depending on the implementation approach, MPC can be categorized into finite control set MPC (FCS-MPC) and continuous control set (CCS-MPC). Compared to FCS-MPC, CCS-MPC generates the optimal control inputs directly and exhibits lower current ripple and torque ripple in the steady state. Nevertheless, CCS-MPC may experience a substantial decline

in performance if the controller parameters deviate from those of the actual system [3], [4].

### A. Literature Review

A wide range of strategies has been investigated in previous studies to address the adverse impact of parameter mismatch in control system design. The first class focuses on parameter identification techniques, which seek to continuously adjust system parameters during operation, thereby improving the control system's resilience to parameter mismatch. [5]. However, due to the nonlinear characteristics of inverters, the accuracy of parameter identification is often difficult to guarantee. Moreover, the complexity of simultaneously identifying multiple parameters poses a significant challenge, limiting the practical applicability of these methods [6]. The second category focuses on observer-based methods, which estimate and compensate for the equivalent disturbances caused by parameter mismatches in real time. Commonly used observers include extended state observers (ESOs) [7], sliding mode observers [8], and Luenberger observers [9]. While such methods offer notable advantages in improving system robustness, they often require intricate parameter tuning. Additionally, both parameter identification and observer-based methods fundamentally rely on mathematical models of the motor, thereby constraining their generalizability and flexibility.

In recent years, the accelerated digitalization of industrial processes has led to a substantial increase in the volume of operational data generated. Leveraging this, data-driven control approaches have emerged as promising alternatives for improving the parameter robustness of MPC systems [10], [11]. These methods replace traditional motor models with data-driven constructs such as look-up table models, ultralocal models, and autoregressive models with exogenous inputs (ARX) [12]. The look-up table-based approach predicts the future current using stored current gradient information. However, its accuracy heavily depends on the precision of the current sampling. Furthermore, the repeated application of an identical voltage vector across consecutive control cycles can lead to stagnation in current gradient updates, ultimately impairing prediction accuracy [13]. The ultralocal model-based approach offers structural simplicity but still requires inductance parameters for gain computation [14]. In the ARX model, the motor dynamics are modeled as a set of discrete-time transfer functions, with the coefficients obtained through input–output decoupling, thus enabling effective control [15].

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Sen Hong, Yixiao Luo, and Kai Yang are with the School of Electrical and Electronic Engineering, Huazhong University of Science and Technology, Wuhan 430074, China (e-mail: m202472450@hust.edu.cn; luoyx@hust.edu.cn; yk@hust.edu.cn).

Shuangxia Niu is with the Department of Electrical Engineering, The Hong Kong Polytechnic University, Hong Kong, China (e-mail: shuangxia.niu@polyu.edu.hk).

Jincheng Yu is with the School of Mechanical Engineering and Automation, Harbin Institute of Technology, Shenzhen, Shenzhen 518055, China (e-mail: yujincheng@hit.edu.cn).

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TABLE I  
COMPARISON OF DIFFERENT LEARNING-BASED CONTROL METHODS

Methods Metrics	Reinforcement learning	Deep learning	Imitation learning
Requirement for model parameters	No	No	No
Computational burden	Low to Moderate	Low to Moderate	Low
Implementation complexity	High	Very high	Moderate to high
Training data requirement	Large	Large	Large
Need for offline training	Yes	Yes	Yes
References	[16], [17], [18]	[19], [20]	[21], [22]

With the increasing adoption of artificial intelligence in motor control and power electronics, learning-based data-driven approaches—including reinforcement learning (RL), deep learning (DL), and imitation learning—have gained considerable attention in the MPC context. RL enables control policy learning through interaction with the environment, where the agent refines its behavior based on received rewards or penalties. For instance, an actor–critic RL strategy was proposed in [16], in which the controller learns to mimic an MPC-based policy without model parameters, ultimately optimizing the switching strategy for power converters. Additionally, deep Q-learning networks have been employed to design PMSM controllers [17]. However, the effectiveness of these methods is strongly influenced by both the adequacy and reliability of the available training data. To mitigate this issue, a meta-RL strategy was introduced in [18], framing the data environment as a partially observable Markov decision process to reduce dependence on large datasets. Nonetheless, overfitting remains a potential concern within this approach that could compromise system robustness. DL-based methods approximate the MPC control law through multilayer neural networks, thereby enhancing robustness to parameter variations. However, DL-based predictive control methods typically require the deployment of multilayer neural networks, and their training process is computationally intensive, which may pose challenges for real-time implementation [19], [20]. In contrast, imitation learning generates extensive training data using expert demonstrations or algorithms and uses this data to train agents that approximate the MPC control law, thereby eliminating dependence on explicit model parameters. Nevertheless, the effectiveness of this approach hinges on whether the training data adequately covers the entire state space; insufficient coverage may lead to inaccurate predictions [21], [22].

Table I summarizes the comparative analysis of representative learning-based techniques. As can be observed, most learning-based data-driven approaches still heavily rely on high-quality training data and necessitate an offline training phase, thereby significantly increasing implementation complexity and computational overhead.

### B. Motivation and Innovation

Inspired by the aforementioned studies, this work investigates a novel learning-based MPC approach that eliminates the need for offline training and extensive reliance on pre-collected

datasets—common limitations of traditional learning-based methods. Specifically, a radial basis function neural network (RBFNN) is utilized to approximate the ideal control input, with its parameters updated online via gradient descent. This process can be regarded as a form of supervised learning. Moreover, a robust control term is incorporated to actively compensate for disturbances.

The primary achievements of this research are as follows.

- 1) *Supervised online learning*: The proposed controller approximates the ideal output through an online, supervised process, without requiring an offline learning phase. Additionally, the only parameter that needs adjustment is the learning rate, significantly reducing the workload.
- 2) *Robustness to uncertainties*: A robust compensation term is designed to mitigate the effects of neural network approximation errors and external disturbances, enhancing the system's disturbance rejection capability.
- 3) *Model-free predictive control*: The proposed method avoids reliance on motor parameters by directly generating the control voltage through the neural network, thus improving robustness against parameter mismatches.

## II. CONVENTIONAL CCS-MPC METHOD

The voltage equations of an interior PMSM in the  $dq$ -axes are given by

$$\begin{cases} u_d = L_d \frac{di_d}{dt} + R_s i_d - \omega_e L_q i_q \\ u_q = L_q \frac{di_q}{dt} + R_s i_q + \omega_e (L_d i_d + \psi_f) \end{cases} \quad (1)$$

Where  $\omega_e$  is the electrical angular velocity,  $u_d$  and  $u_q$  are the  $d$ - and  $q$ -axis voltages of the motor,  $i_d$  and  $i_q$  are the corresponding currents,  $R_s$  is the stator resistance,  $L_d$  and  $L_q$  refer to the  $d$ - and  $q$ -axis stator inductances, and  $\psi_f$  is the rotor flux linkage.

Applying the forward Euler method, the discrete current predictive model of the IPMSM can be obtained. The cost function governing current control is expressed as

$$g = (i_d^* - i_d(k+1))^2 + (i_q^* - i_q(k+1))^2 \quad (2)$$

where  $i_d^*$  and  $i_q^*$  denote the reference currents of the  $d$ - and  $q$ -axis currents, and  $i_d(k+1)$  and  $i_q(k+1)$  are the predictive currents at the  $(k+1)$ th period. The optimal voltage inputs  $u_d^*$  and  $u_q^*$  can be obtained by solving  $\nabla g = 0$ . Since voltage and current constraints are not considered, the optimization reduces to an unconstrained quadratic program, indicating that the CCS-MPC

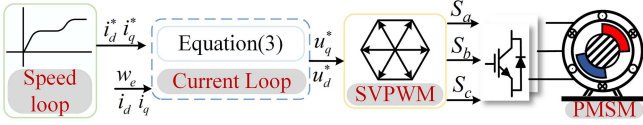


Fig. 1. Schematic diagram of CCS-MPC.

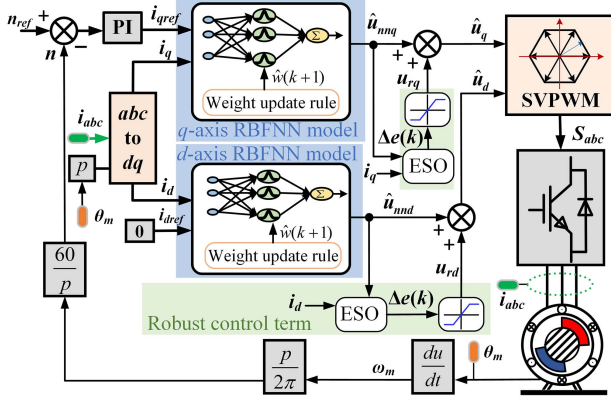


Fig. 2. Schematic diagram of the proposed method.

is an unconstrained MPC approach.

$$\begin{cases} u_d^*(k) = R_s i_d^*(k) + \frac{L_d}{T_s} (i_d^* - i_d(k)) - \omega_e(k) L_q i_q(k) \\ u_q^*(k) = R_s i_q^*(k) + \frac{L_q}{T_s} (i_q^* - i_q(k)) + \omega_e(k) (L_d i_d(k) + \psi_f) \end{cases} \quad (4)$$

where  $T_s$  is the control period.

Once the optimal voltage inputs are obtained, substitute them into the space vector pulsewidth modulation algorithm to generate the corresponding switching signals, thereby realizing control of the IPMSM. This process is the principle of CCS-MPC, as shown in Fig. 1. While this method offers a straightforward structure and ease of implementation, it is evident that the accuracy of the control input, as expressed in (3), is highly sensitive to the precision of the motor parameters.

### III. PROPOSED SLPC METHOD

To mitigate the adverse effects caused by motor parameter mismatches, this article proposes a supervised learning predictive control (SLPC) method. The control structure of this method mainly includes three key elements, an RBFNN approximation model, adaptive weight update rules, and a robust control term, as shown in Fig. 2. First, the establishment of the RBFNN approximation model is introduced.

#### A. Establishment of RBFNN Controller

Taking the  $d$ -axis as a representative case, rewrite the  $d$ -axis voltage equation as follows:

$$\dot{x} = f(x) + g u_d + d \quad (4)$$

where  $x = i_d$ ,  $f(x) = \frac{R_s}{L_d} i_d$ ,  $g = \frac{1}{L_d}$ , and  $d$  represents the disturbance terms in (1). At time  $k$ , by making use of Euler discretization, (4) can be written as

$$x(k+1) = H(k) + G(k) u_d \quad (5)$$

where  $G(k) = T_s g(k)$  and  $H(k) = x(k) + T_s(f(x(k)) + d(k))$ .

Based on the above equations and using the principle of the feedback linearization technique, the desired output is obtained as

$$u^*(k) = \frac{(-H(k) + \gamma e(k) + x^*(k+1))}{G(k)} \quad (6)$$

where  $e(k) = x^*(k) - x(k)$  is the system state error,  $x^*$  is the reference value of the system state, and  $\gamma$  is a constant set by the user.

In real motor operation, parameters such as inductance and magnetic flux linkage are not constants. Therefore,  $H(k)$  and  $G(k)$  are considered unknown nonlinear functions, which makes it impossible to directly obtain  $u^*(k)$  through (6).

To address this issue, this article employs an RBFNN to approximate  $u^*(k)$ . Studies have shown that RBFNN possesses a strong approximation capability even in systems with significant uncertainties. First, the ideal output of the network is defined as  $u_{nn}^*(k)$ , which serves as the ideal approximation of  $u^*(k)$  (i.e., assuming  $u^*(k) = u_{nn}^*(k)$ ). By incorporating the neural network's equations, this output can be specifically expressed as

$$u_{nn}^*(k) = \mathbf{w}^{*T} \mathbf{L}(\mathbf{X}) + \xi(k). \quad (7)$$

Let  $\xi(k)$  denote the approximation error, which satisfies  $\xi(k) < \bar{\xi}$ , where  $\bar{\xi}$  is the upper bound of the error, and its value is a normal constant. The ideal weight vector is denoted as  $\mathbf{w}^* = [w_1^* \ w_2^* \ \dots \ w_m^*]^T$ , with  $m$  being the total number of neurons.  $\mathbf{L}(\mathbf{X}) = [l_1(\mathbf{X}) \ l_2(\mathbf{X}) \ \dots \ l_m(\mathbf{X})]^T$  is the hidden layer composed of  $m$  known activation functions. Here, the neural network input is  $\mathbf{X} = e(k)$ . Equation (7) indicates that there exists an ideal neural network model that can mathematically represent the ideal input  $u^*(k)$ . Since the weight matrix and approximation error of the ideal neural network model are unknown,  $u_{nn}^*(k)$  cannot be directly obtained from (7). Therefore,  $\hat{u}_{nn}(k)$  is defined as the estimated value of  $u_{nn}^*(k)$ , and  $\hat{\mathbf{w}}$  as the estimate of  $\mathbf{w}^*$ . Combining the mathematical model of the neural network,  $\hat{u}_{nn}(k)$  can be expressed as

$$\hat{u}_{nn}(k) = \hat{\mathbf{w}}^T \mathbf{L}(\mathbf{X}). \quad (8)$$

Equation (8) represents that the established model uses  $\hat{\mathbf{w}}^T \mathbf{L}(\mathbf{X})$  to approximate  $\mathbf{w}^{*T} \mathbf{L}(\mathbf{X})$  in (7).

#### B. Adaptive Weight Update Law

To obtain the update rule of the weight matrix, the tracking error is first defined as follows:

$$\begin{aligned} \tilde{u}_{nn}(k) &= \hat{u}_{nn}(k) - u_{nn}^*(k) \\ &= (\hat{\mathbf{w}}^T - \mathbf{w}^{*T}) \mathbf{L}(\mathbf{X}) - \xi(k) \\ &= \tilde{\mathbf{w}}^T \mathbf{L}(\mathbf{X}) - \xi(k) \end{aligned} \quad (9)$$

where  $\tilde{\mathbf{w}}$  represents the error between the actual weight matrix  $\hat{\mathbf{w}}$  and the ideal weight matrix  $\mathbf{w}^*$ . To obtain the adaptive update rule of the weight, define a cost function  $J = \frac{1}{2} \tilde{u}_{nn}^2$ . In accordance with gradient descent, the weight matrix adjustment rule is

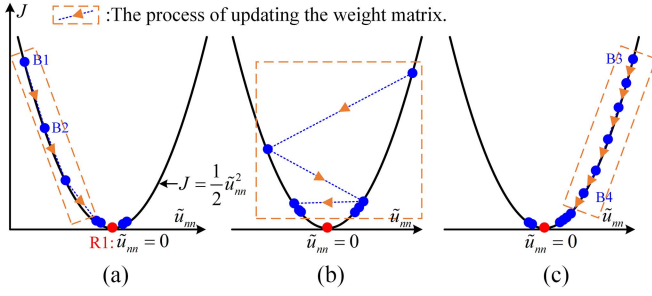


Fig. 3. Gradient descent process under various learning rate settings. (a) Suitable learning rate. (b) Excessive learning rate. (c) Insufficient learning rate.

obtained as

$$\begin{aligned}\hat{\boldsymbol{w}}(k+1) &= \hat{\boldsymbol{w}}(k) - \eta \frac{\partial J}{\partial \hat{\boldsymbol{w}}(k)} \\ &= \hat{\boldsymbol{w}}(k) - \eta \tilde{u}_{nn}(k) \boldsymbol{L}(\boldsymbol{X})\end{aligned}\quad (10)$$

where  $\eta$  is the learning rate. It is worth noting that, in order to simplify the update rule for the weight matrix, the inherent approximation error in (7) is approximated as zero, and this error will be compensated for in the subsequent robust control term.

Fig. 3(a) intuitively shows the principle of gradient descent. Suppose the error is initially located at point B1, where  $\tilde{u}_{nn} < 0$ . According to (10), the weight matrix should be decreased in the next period, thereby reducing the error, which moves from B1 to B2. This process continues iteratively until the error converges to the reference point R1. Fig. 3(b) shows the scenario with an increased learning rate. As the learning rate grows, the convergence speed improves; however, it also introduces larger oscillations around  $\tilde{u}_{nn} = 0$ , potentially destabilizing the system. In contrast, Fig. 3(c) shows the case of a smaller learning rate. Here, the error decreases from B3 to B4 at a slower pace, resulting in diminished convergence speed and a noticeably weaker dynamic response. In summary, Fig. 3 shows the significant influence of the learning rate on the convergence behavior of the system. To achieve optimal control performance, it is essential to select an appropriately tuned learning rate. The specific value will be determined through experimental validation in the subsequent sections of this study.

As can be seen from (10), at this time, the update law of the weight matrix is still related to the output error, and the system state does not directly participate in the update of the weight matrix. If the system state can be introduced to replace  $\tilde{u}_{nn}$  in the weight matrix update rule, online updating of the controller can be achieved. Therefore, this article next deduces the relationship between the output tracking error and the state error. Substituting the optimal input  $u_{nn}^*(k)$  into (5) yields the present predicted value based on this input

$$i_{d,nn}^*(k+1) = \left(1 - \frac{R_s T_s}{L_d}\right) i_d(k) + \frac{T_s}{L_d} u_{nn}^*(k) + T_s d(k)\quad (11)$$

where  $i_{d,nn}^*(k+1) = i_d^*(k+1) + \gamma e(k)$ .

By substituting the approximate output  $\hat{u}_{nn}(k)$  of the neural network into (5), the predicted current value  $\hat{u}_{nn}$  under this input is

given by

$$i_d(k+1) = \left(1 - \frac{R_s T_s}{L_d}\right) i_d(k) + \frac{T_s}{L_d} \hat{u}_{nn}(k) + T_s d(k).\quad (12)$$

Since the approximate output is the voltage actually applied to the motor, the predicted value from (12) will be the current value at the next step.

Subtracting (12) from (11) yields the relationship between the system state error and the output tracking error, as shown in the following equation:

$$e(k+1) + \gamma e(k) = -\frac{T_s}{L_d} \tilde{u}_{nn}(k).\quad (13)$$

It is assumed that the neural network provides a reliable approximation. Assuming the neural network model provides an effective approximation for the ideal input, the state error at the next time step will be smaller than the state error at time  $k$ . At this point, there exists a variable  $M$  (where  $M$  satisfies  $0 < M < 1$ ) such that the state error satisfies  $e(k+1) = M e(k)$ . Thus, (13) can be updated as

$$(M + \gamma)e(k) = -\frac{T_s}{L_d} \tilde{u}_{nn}(k).\quad (14)$$

Inserting (14) into (10) yields the following formulation for the network's weight update rule:

$$\hat{\boldsymbol{w}}(k+1) = \hat{\boldsymbol{w}}(k) + \eta \frac{L_d}{T_s} (M + \gamma)e(k) \boldsymbol{L}(X).\quad (15)$$

Through the derivation of the above formula, the weight matrix update rule is transformed into online learning and update using the system state. For ease of subsequent analysis, the learning rate of the  $d$ -axis neural network approximator is defined as  $\eta_d$ , as shown in the following equation:

$$\eta_d = \eta \frac{L_d}{T_s} (M + \gamma).\quad (16)$$

Similarly, the learning rate  $\eta_q$  of the  $q$ -axis neural network approximator can be defined by substituting the inductance parameters in (16) with the  $q$ -axis inductance parameters. In the experiment, there is no need to calculate  $\eta_d$  using (16) and the inductance parameters. Instead, the corresponding values of  $\eta_d$  and  $\eta_q$  are directly set, thereby achieving MPC without the need for motor parameters.

### C. Robust Control Term Output

When deriving the update rule for the neural network weight matrix, the effect of the inherent approximation error was neglected. To address this, a robust control term is introduced in this section to compensate for the error. Experimental results demonstrate that this robust control term not only effectively compensates for the inherent approximation error but also mitigates the influence of external disturbances. Since ESO can accurately estimate the motor state and compensate for external disturbances, it has been widely applied in MFPC of PMSM. Therefore, this article designs an ESO to obtain the data required

for robust control, as shown in the following equation:

$$\begin{cases} e_1 = x - z_1 \\ \dot{z}_1 = az_1 + bu + z_2 - \beta_1 e_1 \\ \dot{z}_2 = z_3 - \beta_2 e_1 \\ \dot{z}_3 = -\beta_3 e_1 \end{cases} \quad (17)$$

The variables are defined as follows:  $z_1$  is the estimate of state  $x$ ,  $z_2$  is the observation of  $d$ , and  $z_3$  is the observed value of the first derivative of  $d$ .  $\beta_1$ ,  $\beta_2$ , and  $\beta_3$  are all coefficients of the observer.  $a = \frac{R_s}{L_d}$ ,  $b = -\frac{1}{L_d}$ . By discretizing the above equation using the Euler method, we can obtain

$$\begin{cases} e_1(k) = x(k) - z_1(k) \\ z_1(k+1) = (1+aT_s)z_1(k) + T_s(b\hat{u}_{nn}(k) + z_2(k) - \beta_1 e_1(k)) \\ z_2(k+1) = z_2(k) + T_s(z_3(k) - \beta_2 e_1(k)) \\ z_3(k+1) = z_3(k) - T_s\beta_3 e_1(k) \end{cases} \quad (18)$$

By properly setting the parameters of the observer,  $z_1(k+1)$  can be effectively obtained and used in the subsequent process to replace  $x(k+1)$  for control. To guarantee observer convergence, the parameter values are set as follows:  $\beta_1 = -3w_c - a$ ,  $\beta_2 = -3w_c^2$ , and  $\beta_3 = -w_c^3$ . Among them,  $w_c$  is the bandwidth of the observer. In this article, it is designed as  $w_c = 2000$ .

Through the observer, we can obtain  $e(k+1)$  and  $e(k)$ . Currently, we define the filtering error as  $\Theta(k) = e(k+1) + \sigma e(k)$ , where  $\sigma$  is the filtering coefficient. The output expression of the robust control term is

$$u_{rd}(k) = \tau \text{sat}(\Theta) \quad (19)$$

where  $\text{sat}(\Theta(k)) = \begin{cases} \frac{\Theta(k)}{|\Theta(k)|} & \text{if } |\Theta(k)| > \delta \\ \frac{\Theta(k)}{\delta} & \text{if } |\Theta(k)| \leq \delta \end{cases}$ , and  $\tau$  and  $\delta$  are constant coefficients designed by the user.

The compensatory effect of the robust control term can be understood as follows: when the observer predicts that the next-step current is greater than the reference value (this error arises from neglecting inherent errors during the derivation of the network matrix update), it indicates that the input calculated in (8) is overly large. Therefore, the robust control term applies a negative voltage to compensate for this deviation.

The output of the  $d$ -axis is finally defined as

$$\hat{u}_d(k) = \hat{u}_{nn}(k) + u_{rd}(k). \quad (20)$$

Using the same method, the control voltage input  $\hat{u}_q(k)$  on the  $q$ -axis can also be obtained.

#### D. Stability Analysis

The first step in the analysis is to determine whether  $u^*(k)$  obtained through the feedback linearization technique can stabilize the system. Define the Lyapunov function as  $V_1 = \frac{1}{2} e^2$ . Taking its derivative yields

$$\dot{V}_1 = \frac{-\lambda - 1}{T_s} e(k)^2. \quad (21)$$

When the value of  $\lambda$  is greater than  $-1$ , the system satisfies the Lyapunov stability condition. Therefore,  $u^*(k)$  can make the system tend to be stable.

Next, it is proved that the neural network output defined can effectively approximate  $u^*(k)$ . Taking the derivative of  $J$  mentioned earlier, we can obtain

$$\dot{J} = -\frac{\eta}{T_s} \hat{u}_{nn}^2(k) \mathbf{L}^T(\mathbf{X}) \mathbf{L}(\mathbf{X}) \leq 0. \quad (22)$$

From (22), it can be seen that the weight update rule obtained using the gradient descent method satisfies Lyapunov stability.

Finally, the convergence of the designed observer is demonstrated. The system (4) is rewritten as follows:

$$\begin{cases} \dot{x} = ax + bu + x_2 \\ \dot{x}_2 = x_3 \\ \dot{x}_3 = \ddot{d} \end{cases} \quad (23)$$

By subtracting (17) from (23) and supposing  $e_2 = x - z_2$  and  $e_3 = x - z_3$ , the state-space equation of estimation error is obtained as

$$\begin{cases} \dot{e}_1 = (a + \beta_1)e_1 + e_2 \\ \dot{e}_2 = \beta_2 e_1 + e_3 \\ \dot{e}_3 = \beta_3 e_1 + \ddot{d} \end{cases} \quad (24)$$

Therefore, the characteristic equation of (24) is given by

$$s^3 - (a + \beta_1)s^2 - \beta_2 s - \beta_3 = 0. \quad (25)$$

By substituting the previously designed observer parameter values, it can be shown that all three roots of (25) are  $-w_c$ . Thus, it can be concluded that the designed observer is also convergent.

In the preceding section, the observer bandwidth  $w_c$  was set to 2000. This choice was based on two primary considerations. First, the observer gains  $\beta_1$ ,  $\beta_2$ , and  $\beta_3$  are functions of  $w_c$ ; thus, increasing the bandwidth enhances the convergence speed, resulting in a faster response. Second, at this bandwidth, the observer demonstrates a favorable stability margin. As indicated in (25), the convergence of the observer depends on  $w_c$  and the parameter  $a$ . In practical systems, parameter variations can shift the poles of the transfer function, potentially affecting stability. In the theoretical derivation, parameter  $a$  in (25) is defined as  $-R_s / L_d$ . However, in experimental implementation, the theoretical value was not directly adopted; instead,  $a$  was set to  $-100$  to ensure robust convergence in practice.

To evaluate the stability margin at the chosen bandwidth,  $a$  was tested at its theoretical value  $-R_s / L_d$ , and then adjusted to four times and one-fourth of that value for testing. The resulting pole locations of the observer's transfer function are shown in Fig. 4. The pole trajectory diagram shows that even with variations in the observer parameters, the system maintains convergence.

The experimental results under varying observer parameters are shown in Fig. 5, where  $i_{dp}$  and  $i_{qp}$  are the predicted current values at the next time step. The results indicate that even in the presence of parameter mismatches, the proposed observer maintains convergence, thereby enabling accurate estimation of the system states.

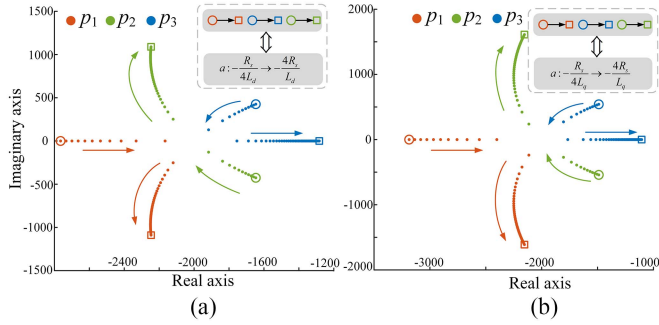


Fig. 4. Pole position trajectory plot. (a) d-axis and (b) q-axis.

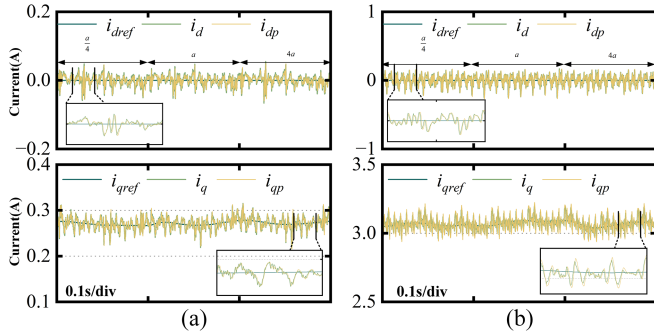


Fig. 5. Analysis of observer convergence under parameter mismatch. (a) Without load. (b) With 2 N·m load.

*Remark 1:* The robust control terms modify the system output without compromising the system’s overall stability.

#### IV. EXPERIMENTAL RESULTS ANALYSIS

In this section, experiments have been conducted to evaluate the effectiveness of the proposed SLPC strategy. The experiment platform is shown in Fig. 4, where an IPMSM serves as the driving motor. Its specific parameters are detailed in Table I. An induction motor is used as the load motor, driven by a variable frequency drive. The control period is configured as 0.0001 s. To verify the superiority of the proposed method, experiments were carried out to compare four methods: the conventional method, the proposed method, the ultralocal-based method from [14] (which uses an ESO as the disturbance observer, added as Method-I), and the RL-based predictive control method from [24] (which adopts a critic-actor structure, denoted as Method-II). It is worth noting that the implementation of Method-II requires the neural network predictor proposed in [25].

##### A. Steady Performance Comparison

Experimental evaluations are conducted in this section to verify the steady-state performance of the conventional method, Method-I, Method-II, and the proposed method.

Fig. 7 shows the steady-state performance of the four methods at 200 r/min without load (the subscript “ref” represents the reference value). The current total harmonic distortion (THD)

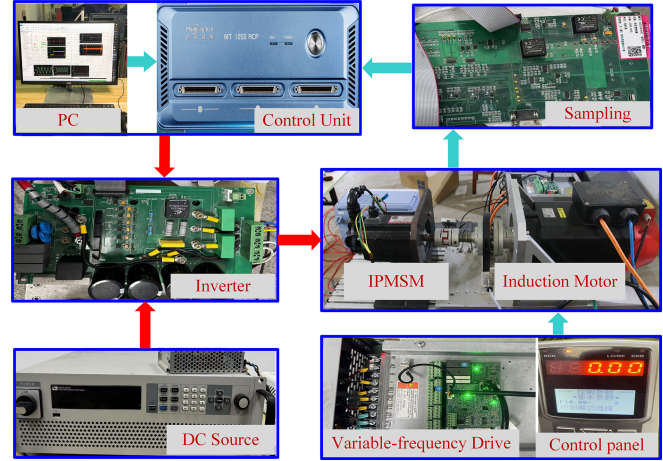


Fig. 6. Experimental platform.

 TABLE II  
PARAMETERS OF THE EXPERIMENTAL SETUP

Symbol	Parameters	Value
$R_s$	Phase resistance	$0.75 \Omega$
$L_d$	$d$ -axis inductance	$3.5 \times 10^{-3} \text{ H}$
$L_q$	$q$ -axis inductance	$9.8 \times 10^{-3} \text{ H}$
$\psi_f$	Rotor flux linkage	$0.142 \text{ Wb}$
$N_p$	Pole pairs	3
$J$	Rotational inertia	$0.0174 \text{ kg} \cdot \text{m}^2$
$n_N$	Rated Speed	1500 r/min
$T_e$	Rated torque	5 N·m
$f_s$	Sampling Frequency	10 kHz
$f_w$	Carrier Frequency	10 kHz

values for the four methods are 5.09%, 4.81%, 4.46%, and 4.04%, respectively.

Fig. 8 further shows the control performance at 1000 r/min under 5 N·m load. As shown in Fig. 8, the current THD values of the four methods are 4.54%, 3.53%, 2.59%, and 2.50%, respectively. Compared to the conventional CCS-MPC approach, the other three methods exhibit improved steady-state performance, with reduced current ripple in the  $dq$ -axis, indicating better control stability.

The experimental results under both low-speed/no-load and high-speed/rated-load conditions validate that the proposed method exhibits superior steady-state control performance.

##### B. Dynamic Performance Comparison

To assess dynamic response characteristics, experiments involving speed transitions are conducted. Fig. 9 shows the performance during a speed ramp from 500 to 1000 r/min. All four methods are capable of effectively tracking the  $dq$ -axis currents. However, the  $q$ -axis current peak of the conventional method reaches as high as 9.57 A, while the other three methods exhibit significantly lower peak values of 7.43 A, 8.46 A, and 8.71 A, respectively—indicating a substantial reduction in current overshoot. Furthermore, the proposed method demonstrates superior

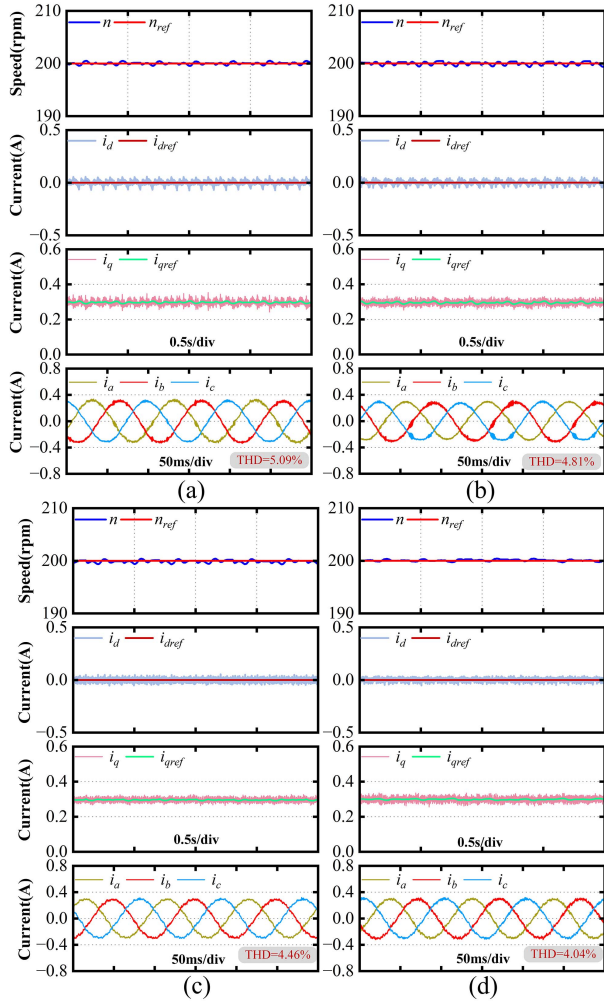


Fig. 7. Experimental results when PMSM operates at 200 r/min without load. (a) CCS-MPC. (b) Method-I. (c) Method-II. (d) Proposed method.

dynamic performance, with a settling time of 0.669 s, compared to 0.784 s for the conventional method.

The effectiveness of the designed robust term in compensating for external disturbances is shown in Fig. 10. A disturbance of the form  $\rho(t) = A(1+x)\sin(Bt)$ , with amplitude  $A = 0.06$  and frequency  $B = 200\pi$ , is injected into the phase A current sampling loop. The motor operates at 500 r/min, and the load is raised from 2 to 5 N·m. Under a 2 N·m load condition, the THD values for the four methods are 6.38%, 4.95%, 3.86%, and 3.81%, respectively. When the load increases to 5 N·m, the corresponding THD values are 6.50%, 4.83%, 4.06%, and 3.77%. Owing to their disturbance compensation capabilities, the proposed method and Method-II exhibit superior steady-state performance under external interference compared to the CCS-MPC and Method-I.

### C. Control Performance Under Parameter Mismatch

Fig. 11 shows the control performance of the CCS-MPC under parameter mismatches. The IPMSM runs at 500 r/min under a 2 N·m load. To quantitatively assess the control performance, two metrics—current ripple  $r_z$  and current fluctuation  $p_z$  are defined. These metrics provide a more intuitive reflection of

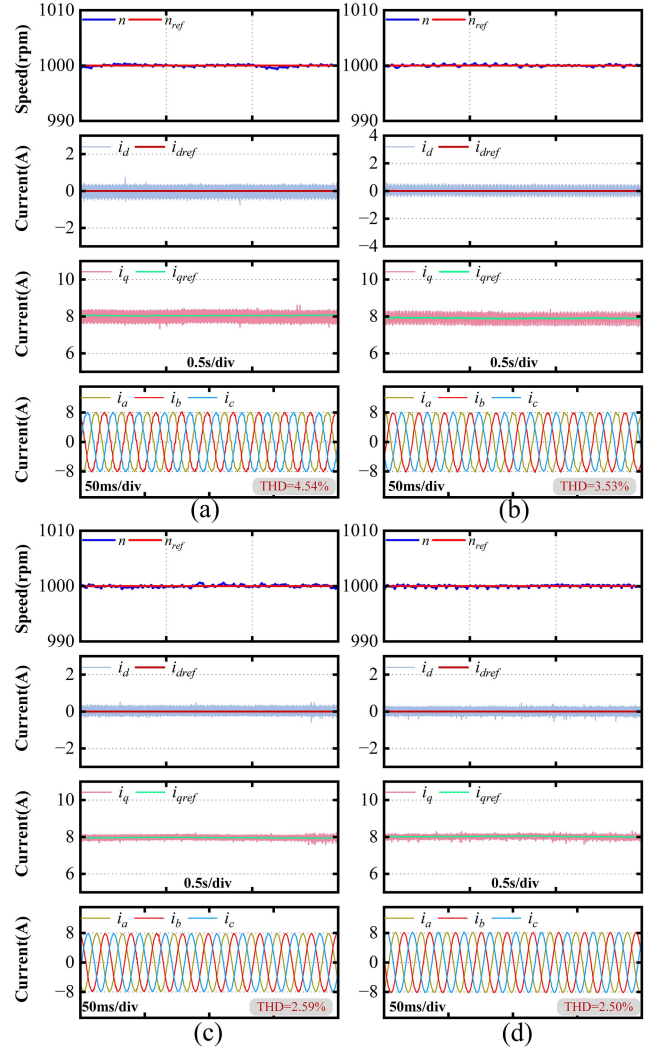


Fig. 8. Experimental results when PMSM operates at 1000 r/min with 5 N-m load. (a) CCS-MPC. (b) Method-I. (c) Method-II. (d) Proposed method.

control performance, enabling a clearer comparison between the four methods.

$$r_z = \sqrt{\frac{1}{N} \sum_{t=1}^N (i_z^*(t) - i_z(t))^2} \quad z \in (d, q) \quad (26)$$

$$p_z = \max(i_z(1), \dots, i_z(N)) - \min(i_z(1), \dots, i_z(N)) \quad z \in (d, q) \quad (27)$$

where  $N$  represents the sample size.

The performance metrics under parameter mismatch are summarized in Table III. As shown in the table, resistance mismatch has a minimal impact on the conventional method. However, as shown in Fig. 11(b), inductance mismatch results in a significant deterioration in the control effectiveness of the CCS-MPC method. Specifically, under  $0.5L_d$  and  $0.5L_q$ , the current ripple  $r_d$  increases to 0.193 A, while under  $2L_d$  and  $2L_q$ , the current fluctuation  $p_d$  rises to 2.13 A, leading to noticeable current fluctuations. Additionally, while flux linkage mismatch has little effect on the  $d$ -axis current performance of the conventional method, it significantly amplifies the  $q$ -axis current ripple, as

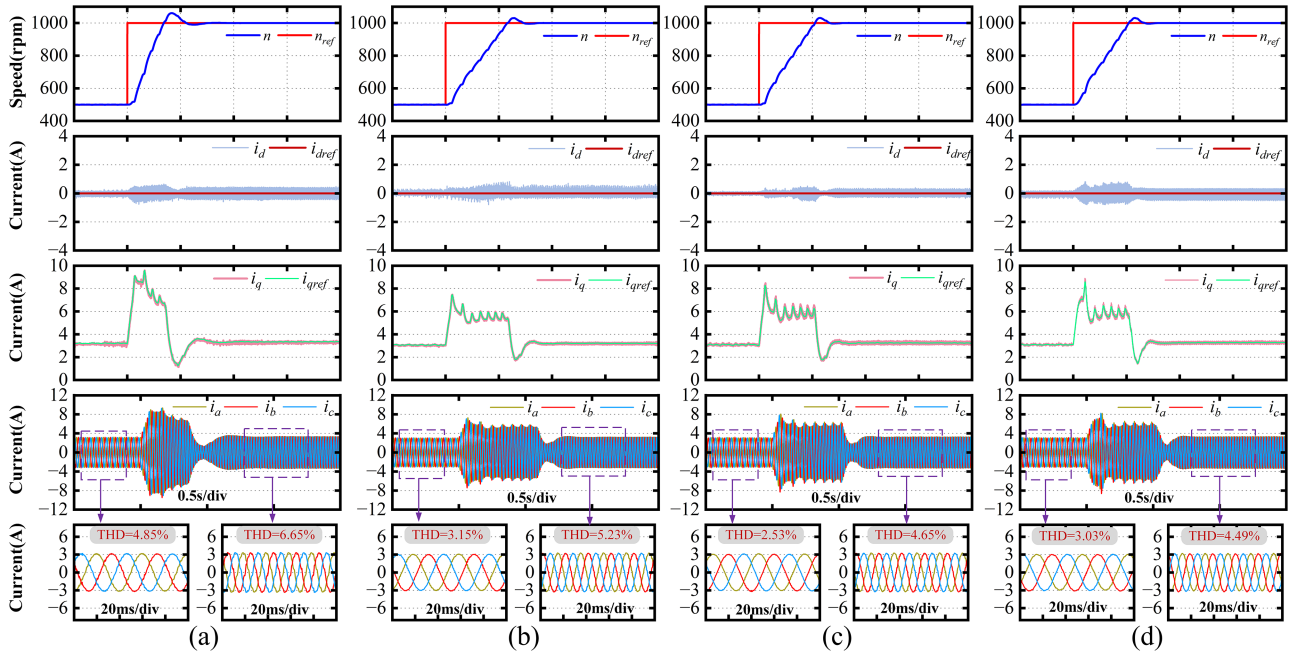


Fig. 9. Control performance when PMSM operates speed increase from 500 to 1000 r/min with 2 N-m load. (a) CCS-MPC. (b) Method-I. (c) Method-II. (d) Proposed method.

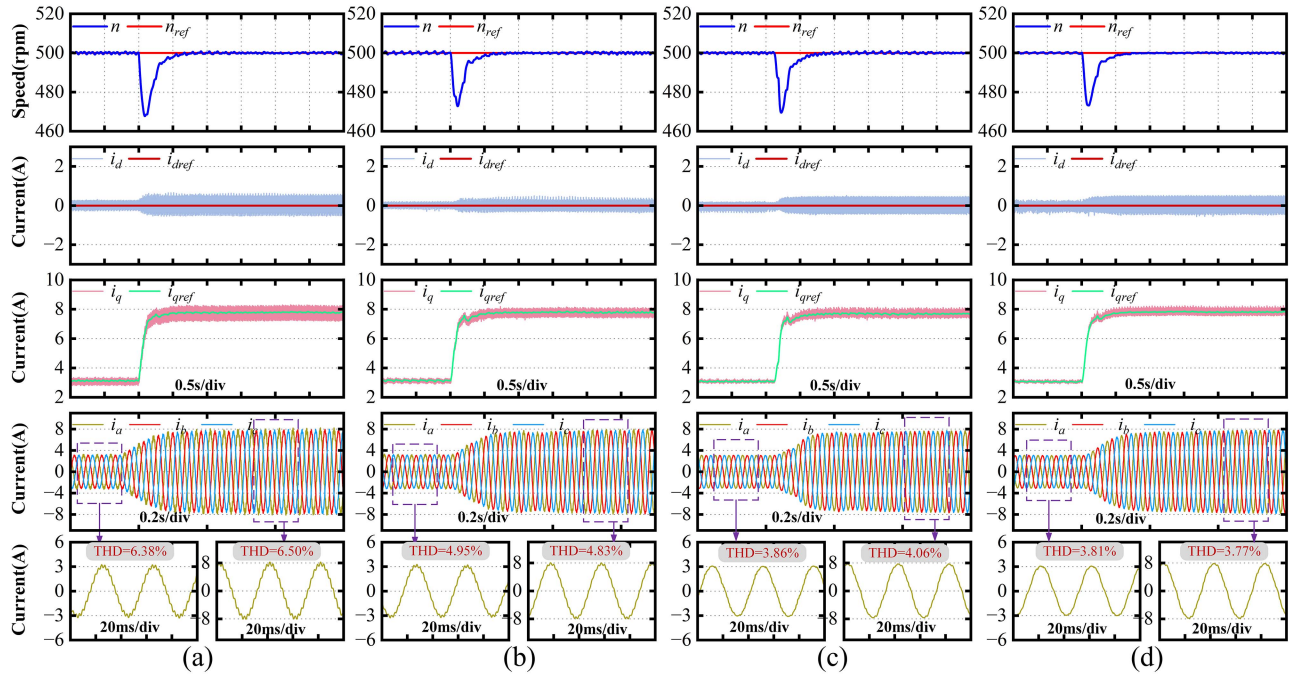


Fig. 10. Control performance when PMSM operates at 500 r/min under sudden load change (2 to 5 N-m) and disturbance. (a) CCS-MPC. (b) Method-I. (c) Method-II. (d) Proposed method.

shown in Fig. 11(c), which reaches as high as 0.617 A, substantially increasing the fluctuation. In addition, Table III evaluates the performance metrics of Method-I and Method-II. Method-I and Method-II are model-free control methods, and their algorithm implementations do not involve motor model parameters, thus eliminating the need for experiments involving changes in

motor parameters. Only the corresponding performance metrics are provided under the same operating conditions. The method proposed in this article involves the inductance parameter in the learning rate term, but this parameter is not used in the actual implementation. To ensure fairness in comparison, we simulated the parameter mismatch by multiplying this parameter by the

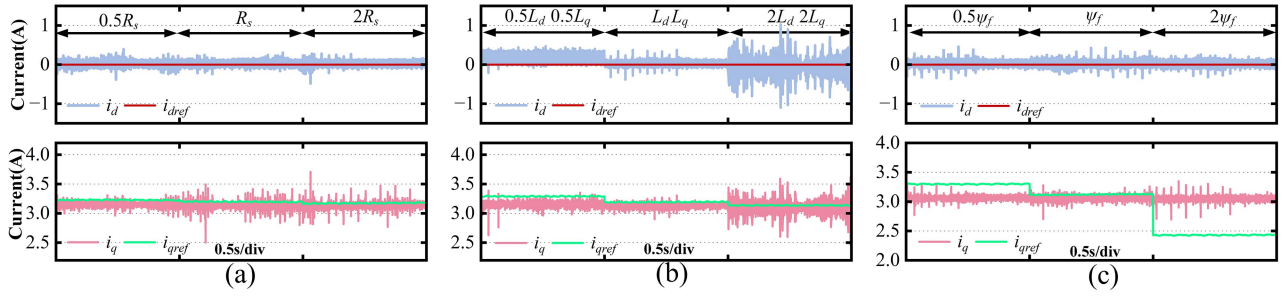


Fig. 11. Control performance under parameter mismatch of conventional method. (a) Under resistance mismatch. (b) Under inductance mismatch. (c) Under flux linkage mismatch.

TABLE III  
PERFORMANCE METRICS UNDER PARAMETER MISMATCH

Method	Parameter	$r_d$ (A)	$r_q$ (A)	$p_d$ (A)	$p_q$ (A)
Conventional Method	nominal	0.072	0.083	0.541	1.001
	$0.5R_s$	0.068	0.076	0.545	0.989
	$2R_s$	0.070	0.054	0.060	0.939
	$0.5\psi_f$	0.071	0.237	0.818	0.734
	$2\psi_f$	0.070	0.617	0.581	0.752
	$0.5L_d, 0.5L_q$	0.193	0.139	0.681	0.760
Method-I	$2L_d, 2L_q$	0.190	0.092	2.130	1.156
	nominal	0.064	0.082	0.443	0.672
Method-II	nominal	0.077	0.042	0.401	0.302
	nominal	0.068	0.043	0.394	0.308
Proposed method	$0.5\eta_d, 0.5\eta_q$	0.067	0.043	0.409	0.305
	$2\eta_d, 2\eta_q$	0.067	0.044	0.417	0.372

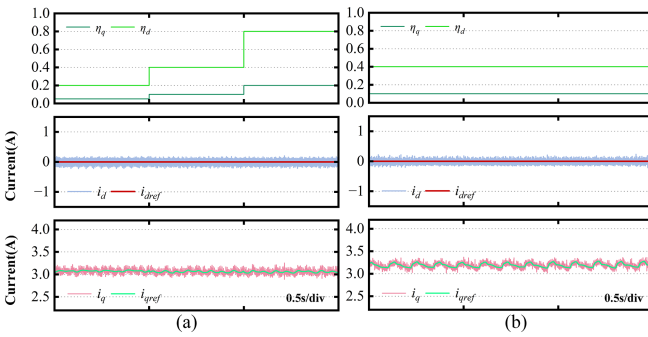


Fig. 12. Verification of the proposed method under inductance parameter mismatch. (a) Control performance under varying learning rate without external inductance. (b) Control performance with external inductance.

corresponding coefficient. The relevant performance metrics are shown in Table III, and the control performance before and after modifying the learning rate is shown in Fig. 12(a). The comparison results clearly demonstrate that the steady-state performance of the proposed method remains unaffected by changes in the learning rate.

To further validate the parameter robustness of the proposed method, the physical parameters of the motor system were modified on the experimental platform, and two sets of experiments were conducted. First, a 3 mH inductor was connected in series between the motor and the inverter to simulate variations in the equivalent inductance. The experimental waveforms under this

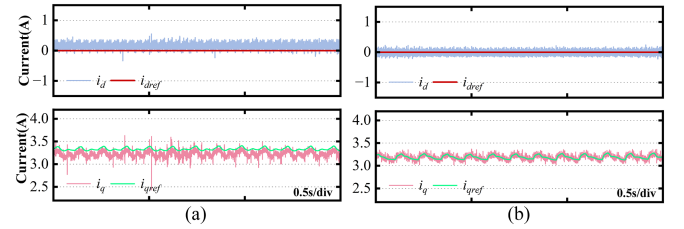


Fig. 13. Control performance with external inductance. (a) CCS-MPC. (b) Proposed method.

condition are shown in Fig. 12, where the controller parameters remained unchanged. The results indicate that the  $dq$ -axis current ripples did not increase significantly, with ripple factors of 0.065 and 0.041, compared to 0.068 and 0.043 without the inductor, which are nearly identical.

In addition, the control performance of the conventional method and the proposed method was compared under the condition of an external inductor. In this comparison, the current loop of the conventional method was designed based on the nominal parameters of the motor, and the PI regulator parameters were kept identical to those of the proposed method. As shown in Fig. 13, when the external inductor is connected, the  $dq$ -axis currents of the conventional method fail to achieve effective tracking. Specifically, the ripple coefficients of the  $d$ -axis and  $q$ -axis currents are 0.182 and 0.112, respectively. In contrast, the proposed method achieves significantly lower ripple coefficients of 0.065 and 0.041 for the  $d$ - and  $q$ -axis currents, respectively, demonstrating superior control performance.

Second, since the flux linkage of the permanent magnets in the test motor cannot be directly adjusted, it was indirectly varied by raising the motor operating temperature. The control performance before and after the temperature change is shown in Fig. 14. The experimental waveforms demonstrate that the  $d$ -axis current tracking is not affected by the temperature variation, as the  $d$ -axis voltage equation does not involve the flux linkage parameter. In contrast, the  $q$ -axis current increases because the flux linkage decreases with rising temperature, requiring a higher  $q$ -axis current to balance the electromagnetic torque with the load torque. Importantly, even though the current magnitude increases, the proposed method still ensures effective current tracking. Specifically, the ripple factors of the  $d$ -axis current

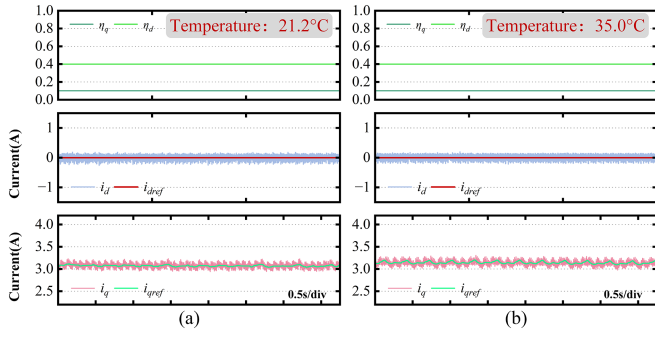


Fig. 14. Current tracking performance with temperature variation. (a) 21.2°C. (b) 35°C.

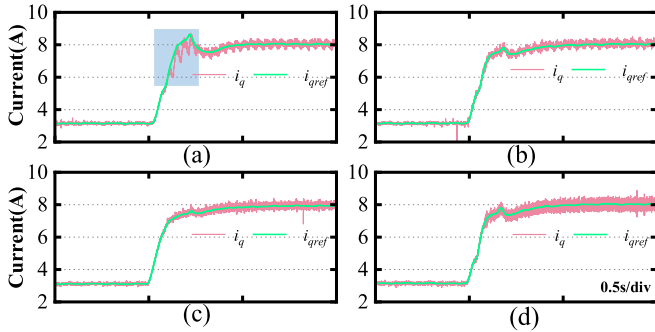


Fig. 15. Dynamic response results under different  $q$ -axis learning rates (load from 2 to 5 N·m). (a)  $\eta_q = 0.001$ . (b)  $\eta_q = 0.01$ . (c)  $\eta_q = 0.1$ . (d)  $\eta_q = 1$ .

before and after the temperature change were 0.065 and 0.066, respectively, while those of the  $q$ -axis current were 0.043 and 0.044, showing almost no difference.

The above experimental results demonstrate that the proposed method can still achieve effective current tracking under variations in both controller parameters and motor physical parameters, thereby exhibiting strong parameter robustness.

#### D. Control Performance Under Different Learning Rates and Different Numbers of Neurons

The previous experiments demonstrated the effectiveness of the SLPC method in steady-state performance, dynamic response, disturbance rejection, and parameter mismatch. However, an in-depth analysis of the proposed method's internal structural characteristics is still lacking. The following experiments focus on evaluating the impact of two key parameters—learning rate and the number of neurons—on motor control performance.

As shown in Fig. 15, with the learning rate of the  $d$ -axis neural network fixed, increasing the learning rate of the  $q$ -axis network reduces the overall dynamic response time. This result aligns with previously obtained findings. Specifically, the dynamic response times for four different learning rates are 0.546 s, 0.525 s, 0.489 s, and 0.479 s, respectively. At lower learning rates, the motor's dynamic response slows, and there are instances where the current fails to effectively track the desired values, leading to

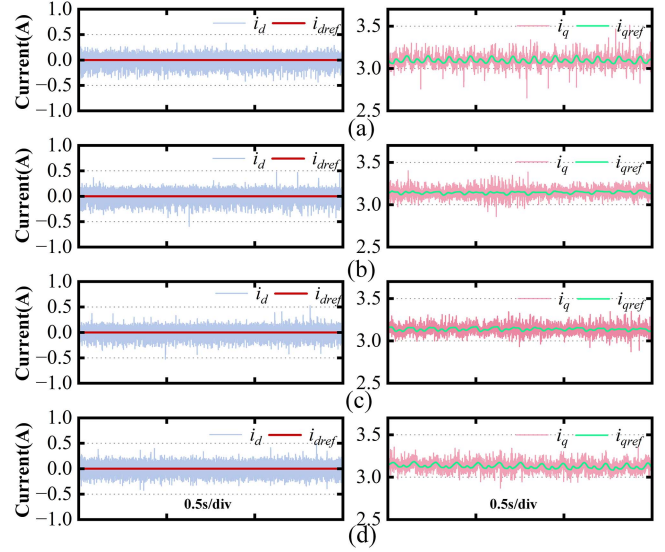


Fig. 16. Current tracking performance of the  $dq$ -axes under different numbers of neurons. (a)  $m = 5$ . (b)  $m = 10$ . (c)  $m = 15$ . (d)  $m = 20$ .

poorer control performance, as shown in the blue-shaded area of Fig. 15(a). As the learning rate increases, the dynamic response time improves.

However, the waveforms shown in Fig. 15(c) and (d) reveal that while increasing the learning rate accelerates the dynamic response, it also induces greater fluctuation in the  $q$ -axis current. Specifically, the  $r_q$  values are 0.048 and 0.122 for the two cases. Based on these observations, the optimal learning rate can be determined experimentally. As shown in the analysis, only a few experiments are necessary to accurately determine this parameter, demonstrating the simplicity and efficiency of the proposed method in terms of parameter tuning.

When using neural networks for approximation, the number of neurons is typically selected to be between 5 and 20 [23]. To determine the optimal number of neurons, experiments are conducted to evaluate the current tracking performance under different neuron counts. Fig. 16 shows the experimental results. For the  $d$ -axis current tracking, no significant difference in tracking performance is observed as the number of neurons  $m$  increases. To reduce computational complexity, the number of neurons in the  $d$ -axis neural network should be set to 5. When the number of  $q$ -axis neurons increases from 5 to 10, the current ripple indices  $r_q$  and  $p_q$  decrease from 0.049 and 0.855 to 0.043 and 0.490, respectively. Further increasing the number of neurons to 15 results in  $r_q = 0.044$  and  $p_q = 0.476$ . These results indicate that, compared to the case with 10 neurons, the performance improvement becomes marginal when the number of neurons is further increased. Therefore, for the experiments, the number of neurons in the  $q$ -axis neural network should be set to 10. Hence, for the experimental setup, the  $q$ -axis neural network is configured with 10 neurons.

The experimental results (as shown in Fig. 16) indicate that the control performance of the proposed method shows no significant correlation with the number of neurons. The main reasons

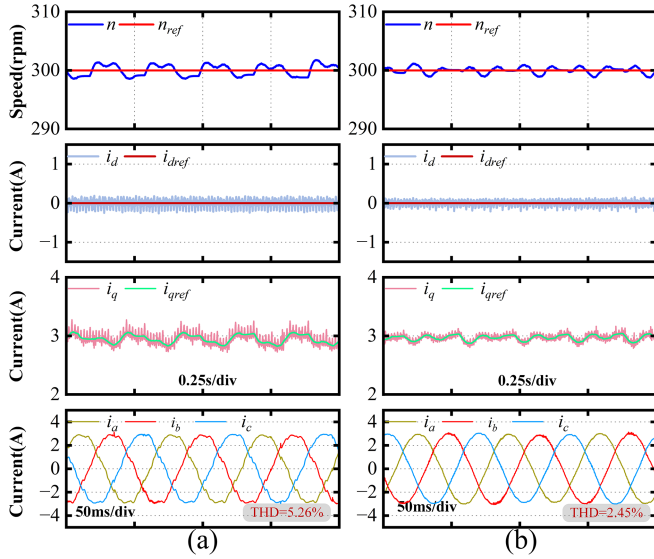


Fig. 17. Comparison of the impact of the robust control term on control performance. (a) Without robust control term. (b) With robust control term.

are as follows: first, the proposed method is based on online learning, where the network is updated solely using sampling information from the current time step. Due to the limited amount of available data, increasing the number of neurons can easily lead to parameter redundancy and a higher computational burden, making it difficult to achieve further performance improvement. Second, for the sake of implementation simplicity, a fixed learning rate is adopted in this study. As the network size increases, the lack of adaptive adjustment in the learning rate may restrict the optimization process, preventing the additional neurons from fully exploiting their potential.

Based on our experimental observations, a practical guideline is to start with a small learning rate (e.g., 0.0001) to ensure stability, then gradually increase it while monitoring dynamic performance, stopping the adjustment when the optimal trade-off between response speed and steady-state performance is achieved. For the number of neurons, start with 5 and incrementally increase until further improvements in steady-state performance become insignificant.

### E. Control Performance Without Robust Control Term

To assess the role of the robust control term relative to the neural network approximator, this article analyzes the control performance without the robust control term. As shown in Fig. 17, after removing the robust control term, the current THD increases from 2.45% to 5.26%. As shown in Fig. 18, under external disturbance injection, after removing the robust term, the A-phase current THD increases from 3.65% to 9.55%. These results demonstrate that the robust control term can effectively compensate for both the inherent approximation errors in the neural network and the external disturbances.

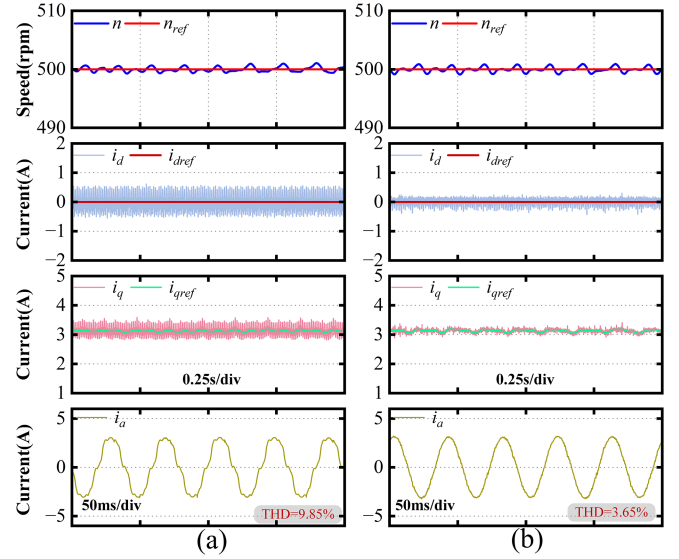


Fig. 18. Comparison of the impact of the robust control term on control performance under disturbance injection. (a) Without robust control term. (b) With robust control term.

TABLE IV  
COMPUTATIONAL TIME COMPARISON OF FOUR METHODS

Method	CCS +MPC	Method I	Method II	Proposed method
Computational time	20.93 $\mu$ s	22.77 $\mu$ s	40.29 $\mu$ s	26.55 $\mu$ s

### F. Comparison of the Four Methods

This section presents a comparative analysis of the four methods from multiple perspectives. Table IV details the computation time of each method. The conventional method, owing to its simple structure, has the shortest execution time. The RL-based Method-II, due to the incorporation of multiple neural networks, has the longest computation time. The proposed method has a computation time of 26.55  $\mu$ s, placing it in the midrange among the four methods.

In terms of parameter robustness, the proposed method, Method-I, and Method-II all demonstrate strong robustness, since they do not rely on motor model parameters. However, due to the lack of dedicated disturbance rejection mechanisms, both the conventional method and Method-I exhibit weaker disturbance rejection capabilities.

A detailed performance comparison of the four methods is presented in Fig. 19. Overall, the proposed method performs excellently in improving parameter robustness and disturbance rejection. Meanwhile, its structure remains simple, with a weight matrix update process straightforward to derive and implement.

### G. Scalability of the Proposed Method

In addition, to verify the scalability of the proposed method, leading angle flux-weakening control experiments and tests under higher load torque conditions were added in this section.

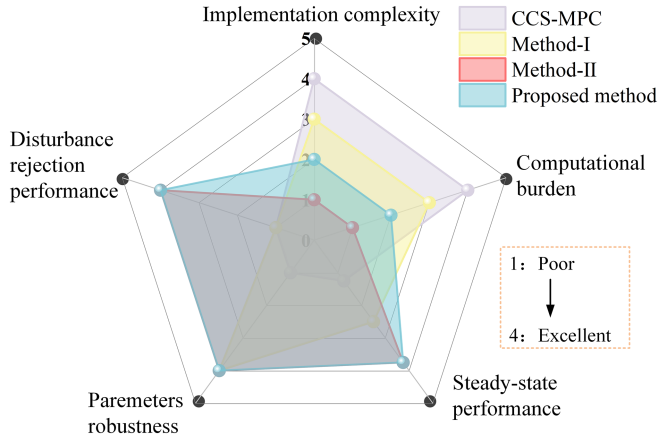


Fig. 19. Comparison of the four methods.

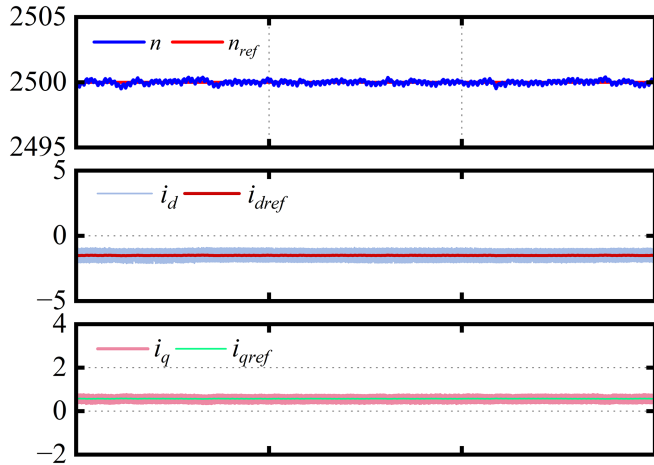


Fig. 20. Experimental results at 2500 r/min under leading angle flux-weakening control.

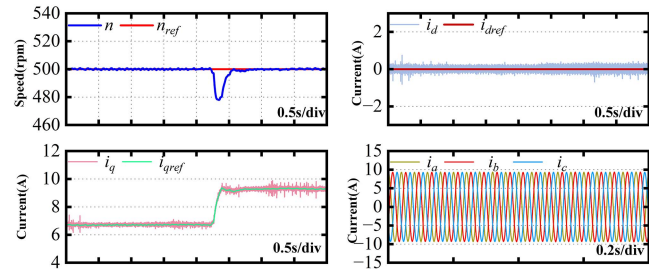


Fig. 21. Overload test performance of the proposed method.

Flux-weakening experiment results are shown in Fig. 20. After applying the flux-weakening algorithm, the motor is able to operate stably at 2500 r/min, with both current and speed achieving excellent tracking performance.

The results of the overload test are shown in Fig. 21, where the motor load torque was increased to 6 N·m, exceeding the rated load by 20%. As observed from the experimental waveforms, the

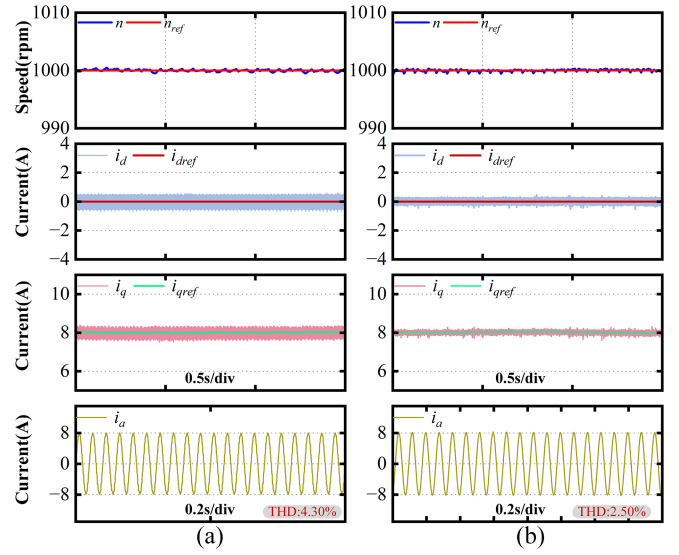


Fig. 22. Experimental results when PMSM operates at 1000 r/min with 5 N·m load. (a) FOC. (b) Proposed method.

proposed method still achieves effective tracking of both speed and current.

#### H. Performance Comparison With FOC

The practical significance of the proposed method is further enhanced by comparing it with the widely implemented field-oriented control (FOC) technique in industrial applications.

Under the same experimental platform with a 1000 r/min rated load, the steady-state performance of both methods is shown in Fig. 22. The experimental results indicate that the proposed method exhibits better steady-state performance and lower current ripple. The THD of the current for FOC is 4.30%, which is close to that of CCS-MPC, while the THD of the proposed method is only 2.50%.

The speed step test for both methods is shown in Fig. 23. When the motor speed increases from 500 to 1000 r/min, the  $dq$ -axis current of the FOC method tracks effectively, but due to the limitation of the current inner loop bandwidth, its response time is 1.07 s, while the proposed method has a faster response time of 0.669 s.

A disturbance of the form  $\rho(t) = A(1+x)\sin(Bt)$ , with amplitude  $A = 0.06$  and frequency  $B = 200\pi$ , is injected into the phase A current sampling loop. When the external load increases from 2 to 5 N·m, both methods can adapt to the load change. However, with external disturbance signals injected, the proposed method shows better control performance, with the current THD before and after the load change being 3.81% and 3.77%, respectively. In contrast, the FOC method, lacking a compensatory loop, shows poorer control performance, with current THD values before and after the load change being 6.39% and 6.45%, respectively.

Additionally, a comparison of computational load and implementation difficulty is also necessary. The proposed method involves the design of a neural network and corresponding

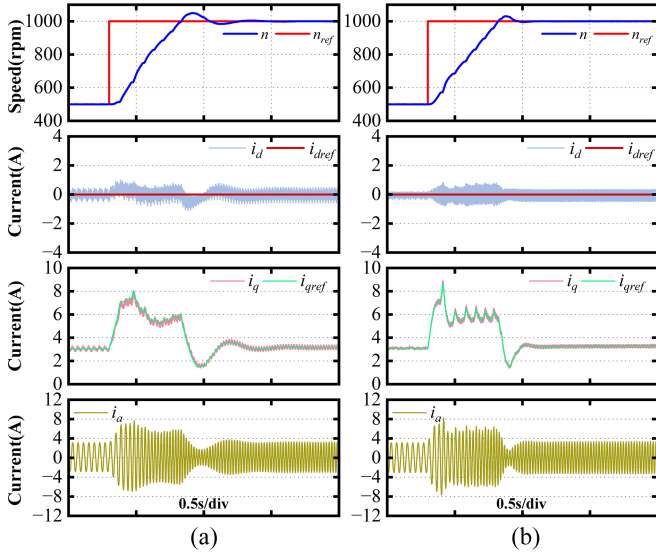


Fig. 23. Control performance when PMSM operates speed increase from 500 to 1000 r/min with 2 N·m load. (a) FOC. (b) Proposed method.

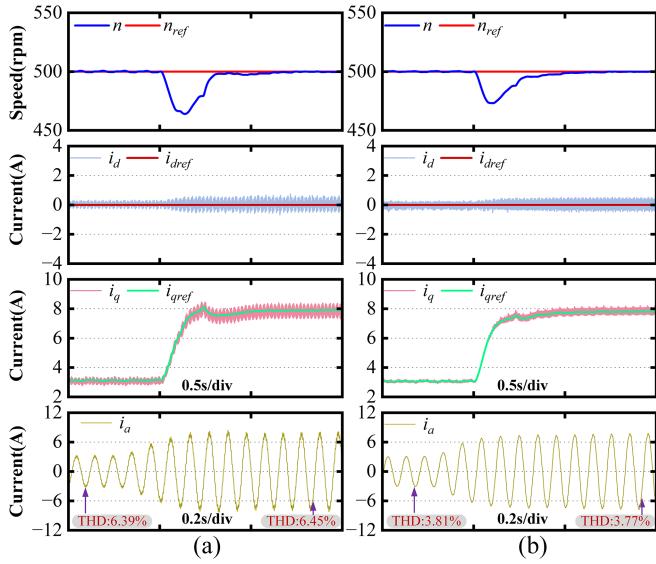


Fig. 24. Control performance when PMSM operates at 500 r/min under sudden load change (2–5 N·m) and disturbance. (a) FOC. (b) Proposed method.

compensation terms, resulting in a computation time of  $26.55 \mu\text{s}$ , while the FOC method only requires a PI regulator, with a computation time of  $20.12 \mu\text{s}$ , making it simpler in structure. Although the proposed method has a slightly increased calculation time and a more complex control structure, the significant improvements in steady-state performance, dynamic response speed, and anti-interference performance make this trade-off worthwhile.

## V. CONCLUSION

A supervised learning-based CCS-MPC approach is proposed in this article for controlling PMSM. The proposed method systematically derives the mapping relationship between tracking

error and state error, incorporating the state error into the weight update law to replace the traditional tracking error term. This approach enables the online adaptive updating of the RBFNN based on current sampling data. To address the inherent error in the neural network approximation process and the impact of external disturbances, a robust compensation term is further designed to enhance the system's control performance. Experimental results indicate that the SLPC approach exhibits enhanced control performance in the presence of parameter mismatches and external disturbances.

## APPENDIX

This appendix section provides a stability proof for the system combining neural networks, robust control term, and the dynamic characteristics of the motor. Under the composite voltage action of the neural network and robust control term, the current prediction equation of the PMSM can be expressed as

$$i_d(k+1) = \left(1 - \frac{R_s T_s}{L_d}\right) i_d(k) + \frac{T_s}{L_d} (\hat{u}_{nn}(k) + u_{rd}(k)) + T_s d(k). \quad (28)$$

Subtracting (11) from (28) yields

$$e(k+1) + \gamma e(k) = \frac{T_s}{L_d} (u_{nn}^*(k) - \hat{u}_{nn}(k) - u_{rd}(k)). \quad (29)$$

Substituting (14) and (19) into (29) yields a simplified expression given as follows:

$$e(k+1) = \frac{(M - \frac{T_s \tau}{L_d \delta} \sigma) e(k)}{(1 + \frac{T_s \tau}{L_d \delta})}. \quad (30)$$

To prove the stability of the entire system, we first define the Lyapunov function of the composite system as

$$V = \frac{1}{2} e^2 + \frac{1}{2} \tilde{u}_{nn}^2. \quad (31)$$

Taking the derivative of (32) yields the following expression:

$$\dot{V} = \frac{e(k+1) - e(k)}{T_s} e(k) + \tilde{u}_{nn}(k) \frac{\partial(\hat{u}_{nn}(k) - u_{nn}^*(k))}{\partial \hat{\mathbf{w}}} \frac{\partial \hat{\mathbf{w}}}{\partial T_s}. \quad (32)$$

Substituting (22) and (30) into (32) yields the simplified expression

$$\begin{aligned} \dot{V} &= \frac{1}{T_s} \left( \frac{(M - \frac{T_s \tau}{L_d \delta} \sigma)}{(1 + \frac{T_s \tau}{L_d \delta})} - 1 \right) e^2(k) - \frac{\eta}{T_s} \tilde{u}_{nn}^2(k) \mathbf{L}^T(\mathbf{X}) \mathbf{L}(\mathbf{X}) \\ &< \frac{1}{T_s} \left( \frac{(1 - \frac{T_s \tau}{L_d \delta})}{(1 + \frac{T_s \tau}{L_d \delta})} - 1 \right) e^2(k) - \frac{\eta}{T_s} \tilde{u}_{nn}^2(k) \mathbf{L}^T(\mathbf{X}) \mathbf{L}(\mathbf{X}) \\ &= \frac{1}{T_s} \frac{-2 \frac{T_s \tau}{L_d \delta}}{(1 + \frac{T_s \tau}{L_d \delta})} e^2(k) - \frac{\eta}{T_s} \tilde{u}_{nn}^2(k) \mathbf{L}^T(\mathbf{X}) \mathbf{L}(\mathbf{X}) < 0. \end{aligned} \quad (33)$$

In (33), the  $d$ -axis inductance  $L_d$ , the interruption period  $T_s$ , the learning rate  $\eta$ , and the parameters  $\delta$  and  $\tau$  of the robust control term are all positive. Therefore, it follows that  $\dot{V} < 0$ . Furthermore, since  $V > 0$ , according to the Lyapunov stability

criterion, the overall motor system can achieve bounded stability under the combined action of the neural network input and the robust control component.

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**Sen Hong** was born in Chongqing, China, in 2002. He received the B.S. degree in electrical engineering from Sichuan University, Chengdu, China, in 2024. He is currently working toward the M.S. degree in electrical engineering with Huazhong University of Science and Technology, Wuhan, China.

His research interests include permanent magnet motor drives and power electronics.



**Yixiao Luo** (Member, IEEE) was born in Hubei, China, in 1991. He received the B.Eng. degree in electrical engineering from Wuhan University, Wuhan, China, in 2013, the M.Eng. degree in electrical engineering from Hanyang University, Seoul, South Korea, in 2015, and the Ph.D. degree in electrical engineering from the City University of Hong Kong, Hong Kong, in 2019.

Since 2022, he has been an Associate Professor with the School of Electrical and Electronic Engineering, Huazhong University of Science and Technology,

Wuhan, China. His research interests include permanent magnet motor drives, renewable energy sources, and microgrids.



**Kai Yang** (Senior Member, IEEE) received the B.S., M.S., and Ph.D. degrees in electrical engineering from Huazhong University of Science and Technology (HUST), Wuhan, China, in 1998, 2000, and 2003, respectively.

In 2005, he was with the Department of Electrical Machine and Control Engineering, School of Electrical and Electronic Engineering, HUST. He is currently a Professor with the School of Electrical and Electronic Engineering, HUST. He has authored and coauthored more than 100 technical papers on IEEE conferences and journals, and has 30 authorized Chinese patents. His research interests include functional-material actuators, design, and control of ac motors.

Dr. Yang has been a Fellow of the IET since 2023. He is a technical reviewer for IEEE TRANSACTIONS ON POWER ELECTRONICS, IEEE TRANSACTIONS ON INDUSTRIAL ELECTRONICS, and IEEE TRANSACTIONS ON INDUSTRY APPLICATIONS. He was the Secretary General for ICEMS 2008 and the Topic Chair for ICEMS 2016/2017/2018/2019.



**Shuangxia Niu** (Senior Member, IEEE) received the B.Sc. and M.Sc. degrees in electrical engineering from Tianjin University, Tianjin, China, in 2002 and 2005, respectively, and the Ph.D. degree in electrical engineering from The University of Hong Kong, Hong Kong, in 2009.

She is currently working as a Professor with the Department of Electrical and Electronic Engineering, The Hong Kong Polytechnic University, Hong Kong, SAR. Her research interests include electric vehicle technologies, renewable energy systems, machines and drives, power electronics technology, applied electromagnetic, numerical methods, and optimization.



**Jincheng Yu** (Member, IEEE) received the B.E. degree in electrical engineering from Beijing Jiaotong University, Beijing, China, in 2016, and the Ph.D. degree in electrical and electronic engineering from the School of Energy and Environment, City University of Hong Kong, Hong Kong, in 2020.

She is currently an Assistant Professor with the Department of Electrical Engineering, Harbin Institute of Technology, Shenzhen, China. Her research interests include machine design and control and sustainable energy conversion technologies.