

# Dynamic Decoupling Current Control of Boost and Buck Multiple Converters

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**Abstract**—A dc–dc converter is widely used in various applications for energy conversion systems. This article focuses on a home energy management system that uses boost and buck converters connected to the same dc link voltage, treating the system as a multiinput multioutput (MIMO) system. A state-space averaging model analysis is used to model the system. The proposed dynamic current decoupling control compensates the dc link voltage at each input. The proposed approach calculates that the elements of the off-diagonal terms become zero. The diagonal terms are first-order systems. The model analysis suggests that the compensation of the duty error needs to be stable in the dc link voltage. The experimental test bench system is constructed and tested to verify the proposed control. By system identification, the model represents the major dynamics of the actual system. Nyquist stability analysis for the MIMO system depicts that the conventional control might be unstable due to MIMO interaction. Step responses also verify that the proposed control suppresses the overshoot voltage and converges faster compared to conventional voltage control.

**Index Terms**—Current control, dc-dc power converters, decoupling control, multiinput multioutput (MIMO), Nyquist stability analysis, voltage control.

## I. INTRODUCTION

DC–DC converters are widely used in dc microgrids, photovoltaics (PV) converters, and battery chargers. In addition, power electronics progress integration, miniaturization, and enable high efficiency. Multiple converters are connected to the same dc bus to reduce cost and increase efficiency. This configuration is seen in many applications, such as dc microgrids [1], ships [2], electric vehicle (EV)s [3], data centers, and home energy management systems (EMSs) [4].

The EMS is composed of many converters, which include the home EMS [5], building EMS [6], factory EMS [7], and a vehicle to home application [8]. These EMSs optimize the

balance of the power demand and supply between subsystems, which consist of renewable energy sources, such as PV and wind turbines, battery storage, and the grid. Designing and testing the system of multiple converters individually takes time. However, the development speed is accelerating as the sector coupling of EMSs increases. To solve this problem, the power electronics building block (PEBB) has been proposed [9]. PEBB integrates power devices, gate drivers, sensors, etc. toward plug-and-play power electronics. PEBB also reduces cost, time, and maintenance, and enables integration. PEBB is adapted to a variety of applications, such as high (medium) grid voltage [10], wireless power transfer [11], aircraft propulsion [12], DAB converter [13], and EMSs [14]. Since their systems are multiinput multioutput (MIMO) systems, a controller is designed or analyzed as a single-input single-output (SISO) system, considering interferences between converters as a disturbance or feedforward signal.

A constant power load (CPL) (e.g., a motor drive) is often connected to the dc bus of a system. When the CPL subsystem increases in input voltage, the input current decreases and vice versa [3], which results in a negative incremental impedance. This CPL generates limit cycles, which increase current and voltage ripples and cause semiconductor device degradation. Many methods have been proposed to resolve this voltage instability. Nonlinear PWM control has been introduced in [15], which is based on the estimation of output power. Passivity-based control has been developed to stabilize the dc link voltage and combine the disturbance observer, i.e., nonlinear observer [16] and extended Kalman filter [17]. Another approach is an impedance specification method of parameter-based Bode and Nyquist plot [18]. However, the experimental approaches to the instability have not yet been clarified and these methods are focused on a single converter for the improvement of followability.

Droop control offers absolute stability as long as its gain remains within stable operating boundaries, which is widely used in grid-connected systems. Its stability for ac grid-connected inverters has been analyzed [19]. Despite its robustness, droop control is unsuitable for precise current control because it inherently contains an error with respect to the command value; even at exceptionally high gains, it consistently results in residual errors in the command value after the system converges.

There are several applications of research using MIMO theory. Two-input-two-output torque difference amplification motor drive system of electrified vehicles installs a summation-differential mode transformation, which suppresses the vibration

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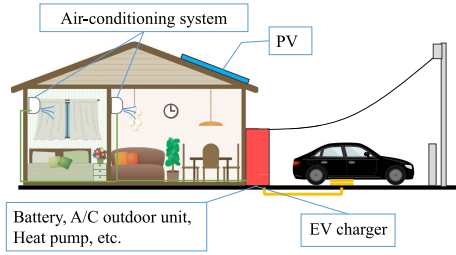


Fig. 1. Concept of our proposed EMS.

of the vehicle [20]. A semiconductor vertical furnace heats a 100 300 mm silicon wafers in the same batch on rapid and precise thermal control using frequency response data [21]. Low-noise error signals for controlling the mirror positions of gravitational wave detectors are crucial for attaining the highest possible sensitivity in the low-frequency detection range. MIMO stability analysis and decoupling matrix suppress large transients and interaction of three angles of mirror [22].

Some papers consider output decoupling for dc–dc converters. One method involves solving a nonlinear function using model predictive control [23]. Another approach achieves decoupling by installing a precompensator [24]. In addition, a MIMO converter can be controlled using sliding mode control for each current [25]. In all these cases, the effectiveness of decoupling would likely be reduced if model errors occur, and stability analysis is not discussed.

Although multiple converters are connected to a dc link, each converter causes voltage instability. Widening the control bandwidth is not an essential solution due to the interference present between converters. This article considers multiple converters combined as one system. The system is treated as a MIMO system. The main contributions of this article are as follows:

- C1) Control each input independently for improved tracking performance, which does not affect other voltage outputs.
- C2) Propose a system design that allows each component to be added stability as a MIMO system when adding additional components.
- C3) Improve the followability desired for the input and output pair, regardless of the behavior of other inputs.

To verify the above, a system that combines a boost converter and a buck converter is designed, and the MIMO stability analysis is conducted in the Nyquist diagram with generalized Gershgorin band. The stability is confirmed using a SISO Nyquist diagram with the generalized Gershgorin bands. Also, confirmed that the current is not affected by other inputs and that the voltage is not affected by other outputs for evaluation of the four-step response.

## II. MODELING AND CONVENTIONAL CONTROLLER OF MULTIPLE CONVERTER SYSTEM

Fig. 1 displays the proposed concept of an EMS. This EMS integrates systems that use relatively large-rated power (i.e., over 1 kW) of electric devices at home, such as PV panels, battery systems, air conditioners, grid-connected inverters, and

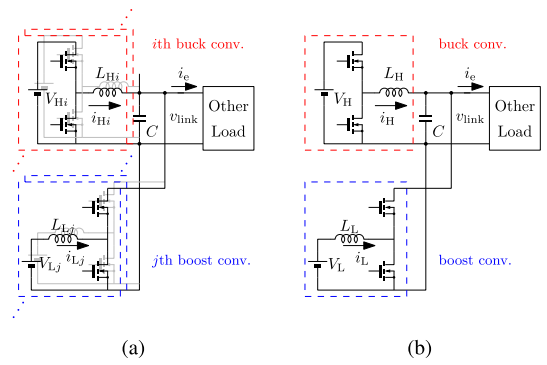


Fig. 2. Circuit configuration of the multiple converter system with buck and boost converters. (a)  $m$  boost converters and  $n$  buck converters. (b) Minimum units of the multiple system are  $m = 1$  and  $n = 1$ .

EV chargers, into a single box and controls them as an integrated unit. This article aims to validate the stability and improve the responsiveness of this EMS. Generally, the PV converter is used for a buck converter and the battery converter is for a boost converter.

Fig. 2(a) generalizes this EMS as a system in which  $m$  boost converters,  $n$  buck converters, and other loads are connected to a dc link capacitor  $C$  whose voltage is  $v_{\text{link}}$ . The dc voltage sources of the  $i$ th buck converter,  $j$ th boost converter are defined as  $V_{Hi}$  and  $V_{Lj}$ , respectively. Also, the inductances and parasitic resistances of the  $i$ th buck and  $j$ th boost inductors are  $L_{Hi}$ ,  $r_{Hi}$ ,  $L_{Lj}$ , and  $r_{Lj}$ . The disturbance current is  $i_e$ .

Fig. 2(b) shows the circuit configuration of the proposed system. Still, for the sake of simplicity, the system is evaluated that connects two different converters  $m = 1$  and  $n = 1$ : one boost converter and one buck converter, as shown in Fig. 2(a). The voltages are defined high-side and low-side dc constant voltage sources and dc link voltage  $V_H$ ,  $V_L$ , and  $v_{\text{link}}$ , as shown in Fig. 2. Also, the currents are high and low-side inductor and disturbance currents as  $i_H$ ,  $i_L$ , and  $i_e$ , respectively. Note that small symbols represent instantaneous values and capital symbols are rms values except for constant values. The inductances and parasitic resistances of the inductors are also defined as  $L_H$  and  $L_L$ , and  $r_H$  and  $r_L$ , respectively. The converters are controlled by a synchronous rectification. This article assumes  $i_e = 0$  in the analysis focused on the basic characteristics of the multiple converter system.

### A. Modeling Using State-Space Averaging Method

Applying Kirchoff's law to the system in Fig. 2(b) gives the following:

$$\frac{d}{dt}x = f(x) = \begin{pmatrix} \frac{d_H}{L_H}V_H - \frac{r_H}{L_H}i_H - \frac{v_{\text{link}}}{L_H} \\ -\frac{r_L}{L_L}i_L - \frac{(1-d_L)}{L_L}v_{\text{link}} + \frac{v_{\text{link}}}{L_L} \\ \frac{i_H}{C} + \frac{(1-d_L)}{C}i_L - \frac{i_e}{C} \end{pmatrix} \quad (1)$$

where  $x = \frac{d}{dt} \begin{pmatrix} i_H & i_L & v_{\text{link}} \end{pmatrix}^T$ .

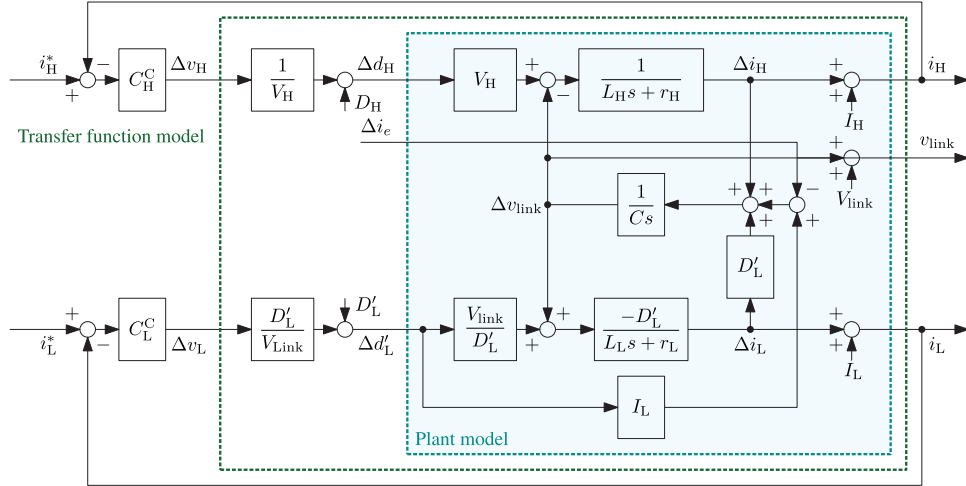


Fig. 3. Conventional control diagrams of the multiple converter system.

By linearizing (1) around the steady-state condition, small-signal response state-space representation (2) and (3) are

$$\frac{d}{dt}\Delta x = \tilde{A}\Delta x + \tilde{B}\Delta d \quad (2)$$

$$\Delta y = \tilde{C}\Delta x \quad (3)$$

where  $\Delta x = \Delta y = (\Delta i_H \quad \Delta i_L \quad \Delta v_{\text{link}})^T$

$$\tilde{A} = \frac{\partial f}{\partial x_k} = \begin{pmatrix} \frac{r_H}{L_H} & 0 & -\frac{1}{L_H} \\ 0 & -\frac{r_L}{L_L} & -\frac{D'_L}{L_L} \\ \frac{1}{C} & \frac{D'_L}{C} & 0 \end{pmatrix}$$

$$\tilde{B} = \frac{\partial f}{\partial d_k} = \begin{pmatrix} \frac{V_H}{L_H} & 0 \\ 0 & -\frac{V_{\text{link}}}{L_L} \\ 0 & \frac{I_L}{C} \end{pmatrix}$$

$$\Delta d = (\Delta d_H \quad \Delta d'_L)^T$$

$$\tilde{C} = I.$$

The lower duty is defined by  $d'_L = (1 - d_L)$ . The Laplace transformation of (2) are given by

$$\Delta i_H = \frac{1}{L_H s + r_H} (V_H \Delta d_H - \Delta v_{\text{link}}) \quad (4)$$

$$\Delta i_L = -\frac{D'_L}{L_L s + r_L} \left( \frac{V_L}{D'_L} \Delta d'_L + \Delta v_{\text{link}} \right)$$

$$\Delta v_{\text{link}} = \frac{1}{sC} (\Delta i_H + D'_L \Delta i_L + I_L \Delta d'_L - \Delta i_e).$$

Steady-state conditions are calculated by (1) = 0

$$D'_L I_L = I_e - I_H \quad (5)$$

$$D_H = \frac{V_{\text{link}} + r_H I_H}{V_H}$$

$$D'_L = \frac{V_L + \sqrt{V_L^2 - 4V_{\text{link}} r_L I_L}}{2V_{\text{link}}}.$$

### B. Conventional Controller Design

Fig. 3 shows overall conventional control diagrams of the proposed system. The cyan box indicates the small-signal model of the plant. The current controllers  $C_H^C$  and  $C_L^C$  are proportional and integral (PI) controllers in this article. The current controllers are designed by considering the plant as a first-order system and are the pole placement detailed equations shown later in Section IV-B.

The state-space equation of the green box in Fig. 3 is expressed as

$$\frac{d}{dt}\Delta x = \tilde{A}^C \Delta x + \tilde{B}^C \Delta u^C \quad (6)$$

$$\Delta y = \tilde{C} \Delta x$$

where

$$\tilde{A}^C = \tilde{A}$$

$$\tilde{B}^C = \begin{pmatrix} \frac{1}{L_H} & 0 \\ 0 & -\frac{1}{L_L} \\ 0 & \frac{I_L}{C V_{\text{link}}} \end{pmatrix}$$

$$\Delta u^C = (\Delta v_H^C \quad \Delta v_L^C)^T.$$

The transfer functions  $G^C$  from inputs  $\Delta u^C$  to outputs  $\Delta y$  are as follows:

$$\Delta y = \tilde{C}(sI - \tilde{A}^C)^{-1} \tilde{B}^C \Delta u^C = G^C \Delta u^C \quad (7)$$

where

$$G^C = \begin{pmatrix} G_{11}^C & G_{12}^C \\ G_{21}^C & G_{22}^C \\ G_{31}^C & G_{32}^C \end{pmatrix} \quad (8)$$

$$G_{11}^C = \frac{\left(s + \frac{r_L}{L_L}\right)s + \frac{D_L^2}{C L_L}}{L_H \Phi}$$

$$G_{12}^C = \frac{-\frac{I_L}{V_{\text{link}}}\left(s + \frac{r_L}{L_L}\right) - \frac{D'_L}{L_L}}{C L_H \Phi}$$

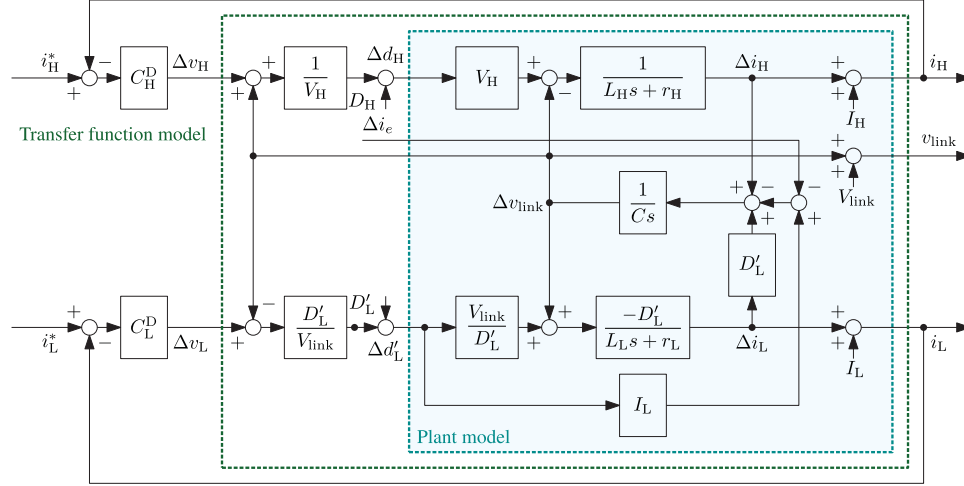


Fig. 4. Proposed control diagrams of the multiple converter system.

$$G_{21}^C = \frac{D_L'}{CL_H L_L \Phi}$$

$$G_{22}^C = \frac{-\left(s + \frac{r_H}{L_H}\right) \left(s + \frac{D_L' I_L}{C V_{link}}\right) - \frac{1}{C L_H}}{L_L \Phi}$$

$$G_{31}^C = \frac{s + \frac{r_L}{L_L}}{C L_H \Phi}$$

$$G_{32}^C = \frac{\frac{I_L}{C} \left(s + \frac{r_H}{L_H}\right) \left(s - \frac{D_L' V_{link} - r_L I_L}{L_L I_L}\right)}{V_{link} \Phi}$$

$$\Phi = s^3 + \left(\frac{r_H}{L_H} + \frac{r_L}{L_L}\right) s^2 + \left(\frac{r_H r_L}{L_H L_L} + \frac{D_L'^2}{C L_L} + \frac{1}{C L_H}\right) s + \frac{r_H D_L'^2 + r_L}{C L_H L_L}.$$

$G_{32}^C$  is from  $\Delta v_L$  to  $v_{link}$ . The numerator of  $G_{32}^C$  has a nonminimum-phase zero [26]. This nonminimum-phase zero is the same as a single boost converter except for the coefficient [27].  $G_{21}^C$  and  $G_{12}^C$  are not equal to zero, and these transfer functions are affected by another output.

### III. PROPOSED CONTROL DESIGN BASED ON DECOUPLING AND COMPENSATION

This chapter first presents the proposed method for a  $2 \times 2$  MIMO converter, and then Section III-B describes the method for a generalized  $m$  boost converter and  $n$  buck converter.

#### A. Proposed MIMO Current Decoupling Control

Fig. 4 represents the overall proposed controller of the proposed system. The next part is the current controller, which contains the proposed input decoupling method shown in this section. The green box of Fig. 4 can be seen that the response from the input to the output current becomes a first-order system by adding and subtracting  $\Delta v_{link}$  in each input, respectively. In other words, disturbance compensation is performed by voltage

fluctuation. This can be expressed analytically as follows:

$$\Delta d = \begin{pmatrix} \frac{1}{V_H} (\Delta v_H^D + \Delta v_{link}) \\ \frac{D_L'}{V_{link}} (\Delta v_L^D - \Delta v_{link}) \end{pmatrix}. \quad (9)$$

Substituting (9) into (2), the proposed decoupled state-space representation (10) is given by

$$\frac{d}{dt} \Delta x = \tilde{A}^D \Delta x + \tilde{B}^D \Delta u^D \quad (10)$$

$$\Delta y = \tilde{C} \Delta x$$

$$\tilde{A}^D = \begin{pmatrix} \frac{r_H}{L_H} & 0 & 0 \\ 0 & -\frac{r_L}{L_L} & 0 \\ \frac{1}{C} & \frac{D_L'}{C} & -\frac{D_L' I_L}{C V_{link}} \end{pmatrix}$$

$$\tilde{B}^D = \begin{pmatrix} \frac{1}{L_H} & 0 \\ 0 & -\frac{D_L'}{L_L} \\ 0 & -\frac{D_L' I_L}{C V_{link}} \end{pmatrix}$$

$$\Delta u^D = \begin{pmatrix} \Delta v_H^D & \Delta v_L^D \end{pmatrix}^T.$$

The transfer function matrix from decoupled inputs  $\Delta u^D$  to outputs  $\Delta y$  is calculated as

$$\Delta y = \tilde{C} (sI - \tilde{A}^D)^{-1} \tilde{B}^D \Delta u^D = G^D \Delta u^D \quad (11)$$

where

$$G^D = \begin{pmatrix} G_{11}^D & G_{12}^D \\ G_{21}^D & G_{22}^D \\ G_{31}^D & G_{32}^D \end{pmatrix} \quad (12)$$

$$G_{11}^D = \frac{1}{L_H s + r_H}$$

$$G_{12}^D = G_{21}^D = 0$$

$$G_{22}^D = -\frac{D_L'}{L_L s + r_L}$$



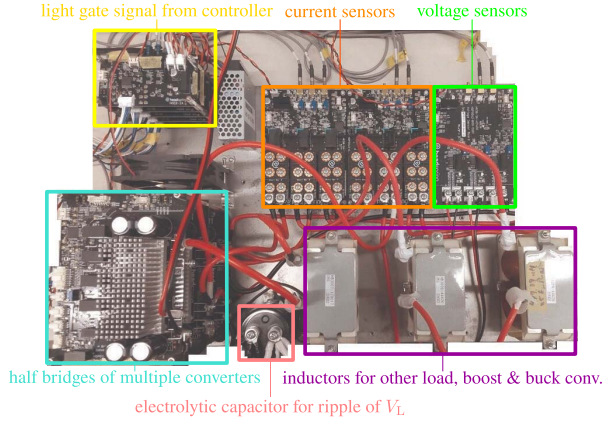


Fig. 5. Experimental setup of the system.

TABLE I  
EXPERIMENTAL PARAMETERS OF THE BENCH SYSTEM

Parameter	Value	Parameter	Value
$L_H$	1.23 mH	$r_H$	0.328 $\Omega$
$L_L$	438 $\mu$ H	$r_L$	0.206 $\Omega$
$C_{link}$	712 nF	$V_L$	100 V
$V_H$	200 V	$f_{sw}$	20 kHz
Dead time	500 ns		

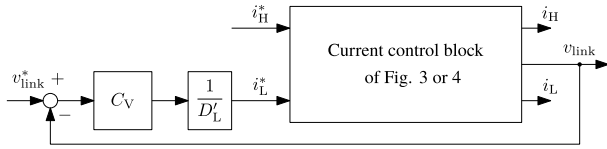


Fig. 6. Block diagram of the experiment for the closed-loop system identification.

### A. Experimental Setup

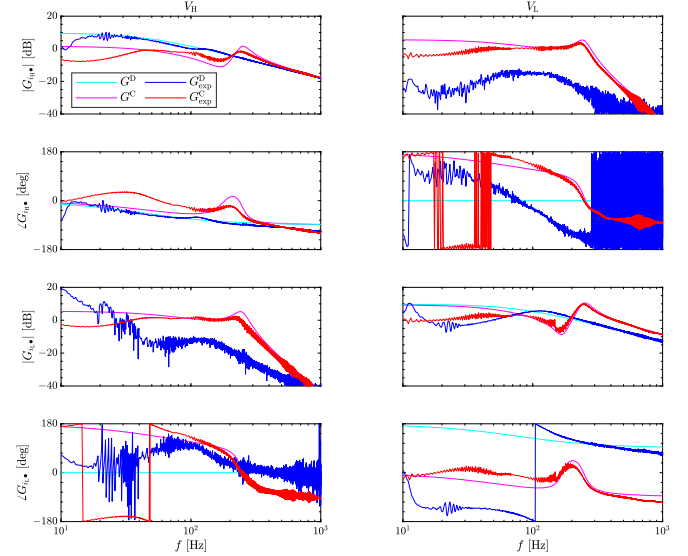
Fig. 5 illustrates the experimental setup used in the experiment. The circuit configurations are shown in Fig. 2(b). Table I summarizes the circuit parameters of the system. The circuit parameters of the system are measured at the same converter carrier frequency  $f_{sw}$  of 20 kHz. The dc link capacitor consists of a combination of electrolytic capacitors and ceramic capacitors to reduce the switching surges of the converters. The controller is used for MWPE4-PEV of PE-Expert4 made by Myway Plus in all experiments. Calculation period is the same carrier frequency  $f_{sw}$ . The controller is installed one sample delay of 50  $\mu$ s, which is a classic implementation. The data also collect the analog-to-digital (AD) converter of MWPE4-PEV by using the sensor boards, which consist of F02P050S05 L made by Tamura Corp, whose conversion time is 500 ns.

### B. System Identification of the MIMO Current Decoupling Control System

Fig. 6 shows block diagram of the overall control for system identification. System identification is often performed using an open loop. However, in this article, system identification with weak feedback was employed to facilitate comparison with a theoretical transfer functions (8) and (13) at a fixed

TABLE II  
CONTROLLER CONDITIONS USED IN SYSTEM IDENTIFICATION

Parameter	Value	Parameter	Value
$\omega_H$	21 Hz	$\omega_L$	21 Hz
$\omega_V$	7 Hz		
$I_H^*$	4 A	$V_{link}^*$	160 V

Fig. 7. Bode diagrams of the system w/o and w/ decoupling in state-space model  $G^C$  in (8) and  $G^D$  in (13), frequency response data w/o and w/ decoupling  $G^C_{exp}$  and  $G^D_{exp}$ .

operating point. This article installed the voltage controller at the lower boost converter. The closed-loop system identification is separately done by the chirp signal  $V_C$  from 1 to 1500 Hz adding each input  $\Delta v$  as shown in Figs. 3 or 4. PI gains of the current controller are designed by pole placement

$$C_H^C = C_H^D = K_{PH} + \frac{K_{IH}}{s} = 2\omega_H L_H - R_H + \frac{\omega_H^2 L_H}{s}$$

$$C_L^C = C_L^D = K_{PL} + \frac{K_{IL}}{s} = \frac{2\omega_L L_L - R_L}{D'_L} + \frac{\omega_H^2 L_H}{D'_L s}. \quad (18)$$

Here,  $\omega_H$  and  $\omega_L$  are angular frequencies of the pole. The pole placement method is more stable than the pole-zero cancellation even when there is a modeling error in the control plant. The boost converter contains the  $D'_L$  but the conventional method included  $D'_L$  before the duty input  $d'_L$ ; this coefficient cancels out and the gain design is the same as that of the buck converter.  $C_V$  is the voltage PI controller to maintain the dc link voltage, whose gain is also designed by pole placement

$$C_V = K_{PV} + \frac{K_{IV}}{s} = 2\omega_V C + \frac{\omega_V^2 C}{s}. \quad (19)$$

Table II summarizes the control parameters for the system identification of the conventional and proposed methods in the currents. Mentioned above, the system identification with weak feedback was employed to avoid affecting.

Fig. 7 shows the Bode diagrams of the proposed system with the conventional method and the proposed decoupling method.

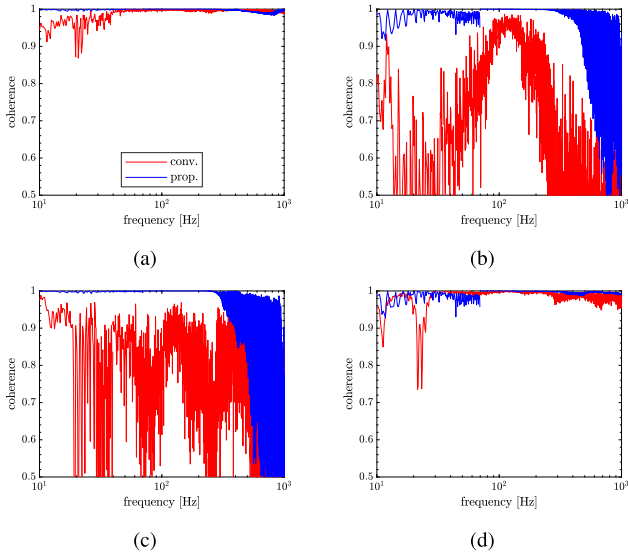


Fig. 8. Coherence of the experimental identification between inputs and outputs. (a) From  $v_H$  to  $i_H$ . (b) From  $v_H$  to  $i_L$ . (c) From  $v_L$  to  $i_H$ . (d) From  $v_L$  to  $i_L$ .

The experimental frequency response data contain the sensor noise, error, quantizations, and controller delay. The lower frequency range is not matched due to the internal impedance of the experimental voltage source. These differences are due to the input impedance of the constant voltage sources  $V_H$  and  $V_L$ . However, the controller can be suppressed by the higher frequency feedback loop. The conventional experimental result fits the simulation result of the resonant and antiresonant frequency in each input and output except for the lower frequency range. Besides, the experimental proposed method matches the model-based calculation of (13) in the diagonal elements. The off-diagonal elements of the experimental proposed method remain around  $-20$  dB since the measuring noise contains the outputs.

Fig. 8 plots the coherence of the system identification. Coherence is a function that takes values between 0 and 1 and has the property of taking a value of 1 when two signals are perfectly linear. By utilizing this property and checking the value of the coherence function for each frequency of the input or output data used in the frequency response measurement, it is possible to determine whether the frequency response data have high linearity. The off-diagonal terms of the coherence in the conventional method are lower compared to the diagonal terms, which is due to the lower output signal. However, the diagonal terms exhibit high coherence and good agreement with the model, allowing for the simultaneous acquisition of data for the off-diagonal terms.

Relative gain array (RGA) is a useful tool in practical applications and provides a measure of interaction [26]. RGA  $\Lambda$  is calculated as

$$\Lambda = G \circ (G^{-1})^T \quad (20)$$

$$\Lambda_{ij} = \lambda_{ij} = [G]_{ij} [G^{-1}]_{ji}.$$

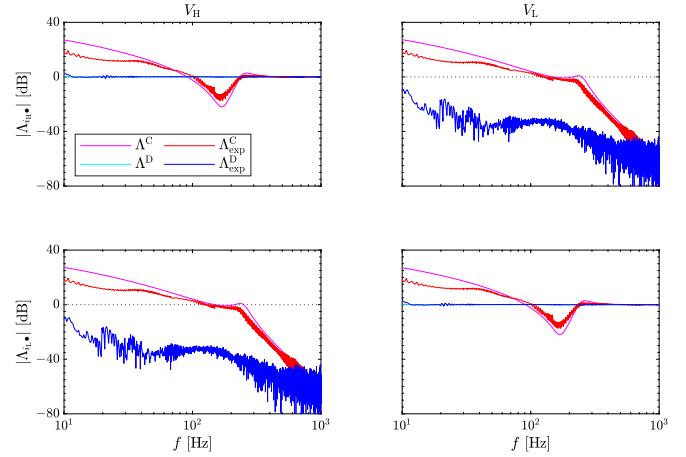


Fig. 9. RGA of the model-based and experimental results with conventional and decoupled methods,  $G^C$ ,  $G^D$ ,  $G_{\text{exp}}^C$ , and  $G_{\text{exp}}^D$ , respectively.

Here, “ $\circ$ ” denotes Hadamard product, which means element-by-element multiplication. RGA is independent of input and output scaling.

Fig. 9 shows the RGA of the model-based and experimental results with the conventional and decoupled methods. Note that dominant input and output pairs have 0 dB of RGA and other pair is  $-\infty$  dB; in other words, they decouple. The conventional experimental results are the same as the model-based calculations except for the lower frequencies.  $\Lambda_{11}$  and  $\Lambda_{22}$  of the model-based decoupling method are 0 dB, and the off-diagonal terms are not displayed since the interrelations are extremely low in the all-frequency range shown in (13), respectively. The experimental decoupling results show similar trend to the model-based result. From the above results, the proposed method achieved the decoupling of currents in the system identification.

### C. MIMO Nyquist Stability Analysis With Experimental Frequency Response Data

The Nyquist diagram is one of the determining stability and is performed by plotting the vector locus of the open-loop transfer function  $L$  using the transfer functions  $G$  and controller  $C$

$$L(j\omega) = G(j\omega)C(j\omega). \quad (21)$$

The MIMO system may become unstable due to interactions between inputs, even if each individual SISO system is stable. MIMO stability is assessed using the direct Nyquist array (DNA) method with generalized Gershgorin bands. By applying the DNA theorem, the stability condition is satisfied when the band locus (which is called a generalized Gershgorin band) drawn by a circle with radius  $r_{gq}$  shown in (22), centered on the  $q$ th diagonal element  $L_{qq}$  of  $L$  at all frequencies, turns around the critical point the same number of times as the number of unstable poles of the target plant  $G$

$$r_{gq}(j\omega_k) = \lambda(j\omega_k) |L_{qq}(j\omega_k)| \quad (22)$$

where  $\lambda(j\omega_k) = \max \text{eig} \{M(j\omega_k)\}$

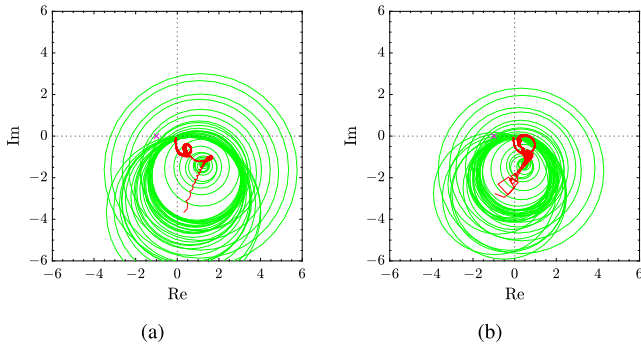


Fig. 10. Nyquist diagrams with generalized Gershgorin bands of experimental conventional current control from experimental frequency response data  $\exp G^C$  of Fig. 7 shown in Fig. 3. Generalized Gershgorin bands plotted at 50 points of the same intervals on a log scale from 10 Hz to 1 kHz. (a) From  $V_H^C$  to  $\Delta i_H$ . (b) From  $V_L^C$  to  $\Delta i_L$ .

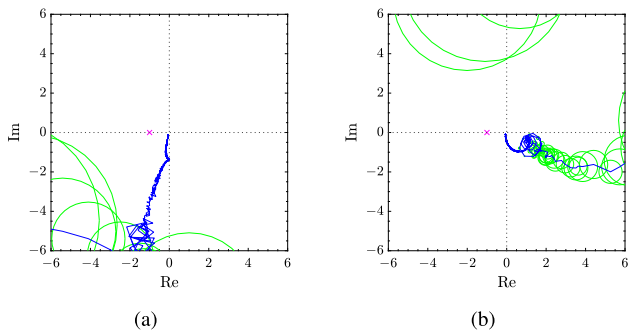


Fig. 11. Nyquist diagrams with generalized Gershgorin bands of the proposed current control from experimental frequency response data  $\exp G^D$  shown in Fig. 4. Generalized Gershgorin bands are plotted at 50 points of the same intervals on a log scale from 10 Hz to 1 kHz. (a) from  $\Delta v_H^D$  to  $\Delta i_H$ . (b) from  $\Delta v_L^D$  to  $\Delta i_L$ .

TABLE III  
PARAMETERS OF PI CONTROL IN THE NYQUIST PLOT SHOWN IN (18)

Parameter	Value	Parameter	Value
$\omega_H$	100 Hz	$\omega_L$	100 Hz

$$M(j\omega) = \begin{cases} 0 & (p = q) \\ \frac{G_{ij}(j\omega_k)}{G_{ii}(j\omega_k)} & (p \neq q) \end{cases}$$

Here, eig is an eigenvalue calculation of the matrix. In a normal case, the generalized Gershgorin bands do not include the point of  $(-1, j0)$  on the Nyquist diagram, the system satisfies a MIMO stability condition with the interaction between each input.

Figs. 10 and 11 illustrate the Nyquist diagrams of open-loop frequency response data from voltage command value to output current, respectively. These calculations were done from experimental transfer function data  $G$ , as shown in Fig. 7, including a sensor noise, error, quantizations, and controller delay and the ideal PI controllers  $C_H$  and  $C_L$  obtained by (18) with the parameter of the angular frequency shown in Table III. The black lines mean the SISO Nyquist plots of the current control systems. The open-loop frequency response of each axis may move within the radius of the generalized Gershgorin bands at each frequency point on the Nyquist diagram when MIMO

TABLE IV  
EXPERIMENTAL PARAMETERS OF THE STEP RESPONSES

Parameter	Value	Parameter	Value
$V_e$	200 V	$V_V$	100 V
$L_e$	404 $\mu$ H	$r_e$	0.422 $\Omega$
$L_V$	447 $\mu$ H	$r_V$	0.253 $\Omega$
$\omega_H$	21 Hz	$\omega_L$	21 Hz
$\omega_{VC}$	21 Hz	$\omega_{VV}$	7 Hz
$\omega_e$	800 Hz		
Initial condition of the command value			
$I_H^*$	4 A	$I_L^*$	5 A
$I_e^*$	0 A	$V_{link}^*$	160 V

Other parameter are in Table I.

TABLE V  
COMPARISON BETWEEN CONVENTIONAL AND PROPOSED METHOD

Step		maximum error			converged time [ms]		
		$i_H$ [A]	$i_L$ [A]	$v_{link}$ [V]	$i_H$	$i_L$	$v_{link}$
$i_H$	conv.	0.7	1.4	9.4	70	22	40
	prop.	0.3	0.4	12	12	19	35
$i_L$	conv.	8.1	1.0	9.5	65	50	60
	prop.	1.6	NA	11	3	20	60
$i_e$	conv.	1.2	1.8	12	60	40	60
	prop.	0.3	1.1	16	4	50	60
$v_{link}$	conv.	0.6	1.1	3.1	60	60	60
	prop.	0.1	0.3	2.5	5	20	35

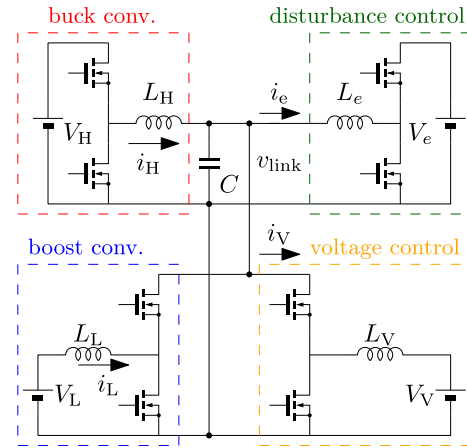


Fig. 12. Circuit diagram of the experiment for the step response.

systems interact between each axis. The conventional current control method in Fig. 10 is stable, as shown in the SISO Nyquist plots. However, the generalized Gershgorin bands conclude that the overall current control system may be unstable because these bands contain  $(-1, j0)$  in each axis. In contrast, the proposed current control method in Fig. 11 is stable from both the SISO Nyquist diagrams and the generalized Gershgorin bands, but the band remains a width due to sensor noise and dc link voltage sample delay. The smaller generalized Gershgorin bands depict the better decoupling performance with the proposed method. Although the generalized Gershgorin band is a sufficient MIMO stability condition, the MIMO stability guarantee is necessary to analyze the multiple converter applications.

The proposed method is only used for the dc link voltage  $\Delta v_{link}$  and does not use the circuit parameter, because  $\Delta v_{link}$  contains the information of circuit parameters shown in Fig. 4. In other words, the circuit parameter and steady-state condition

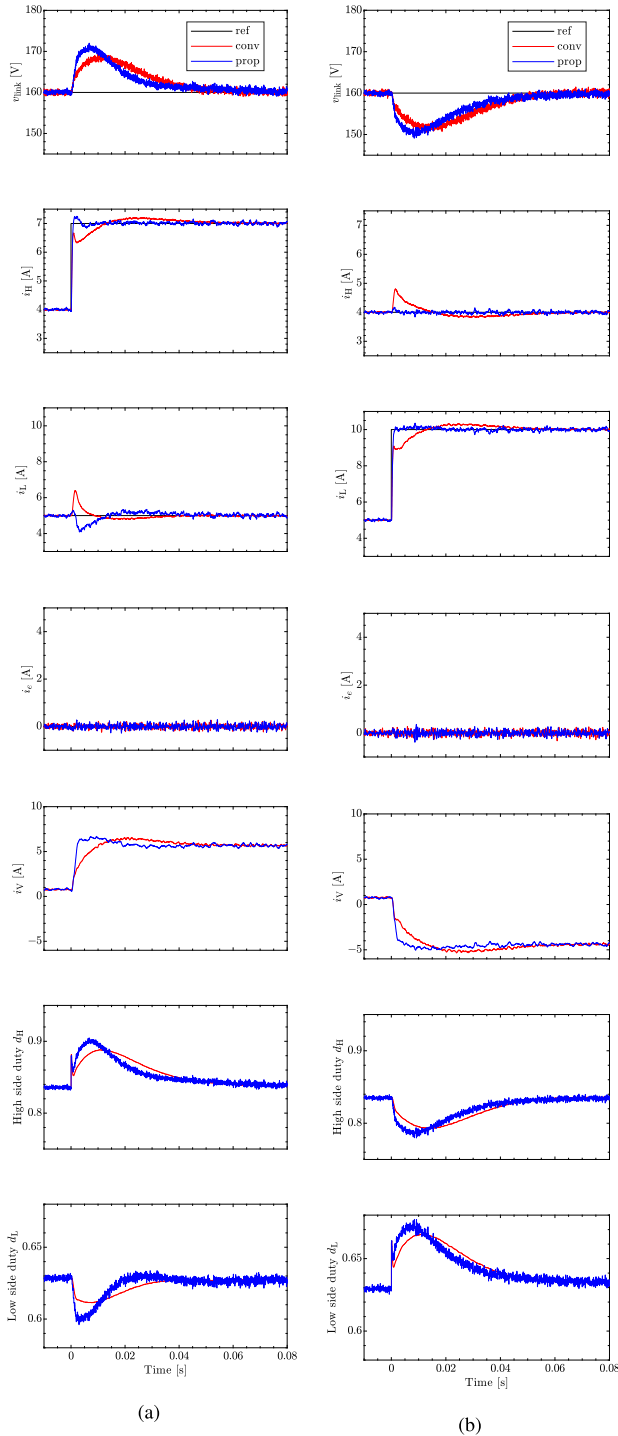


Fig. 13. Current step responses of the system with Fig. 12 when  $I_e = 0$ . (a)  $i_V$ ,  $i_H$ ,  $i_L$ ,  $i_e$ ,  $i_V$ ,  $d_H$ , and  $d_L$  of  $i_H^*$  step from 4 to 7 A. (b)  $i_V$ ,  $i_H$ ,  $i_L$ ,  $i_e$ ,  $i_V$ ,  $d_H$ , and  $d_L$  of  $i_L^*$  step from 5 to 10 A.

are only used for plotting the Bode. For the reasons stated above, the proposed method is not affected by changes in the circuit parameters.

#### D. Tracking Performance in Various Step Responses

This section examines the step response of the system. The four cases of the experiments were done, which are  $i_H$ ,  $i_L$ ,  $i_e$ ,

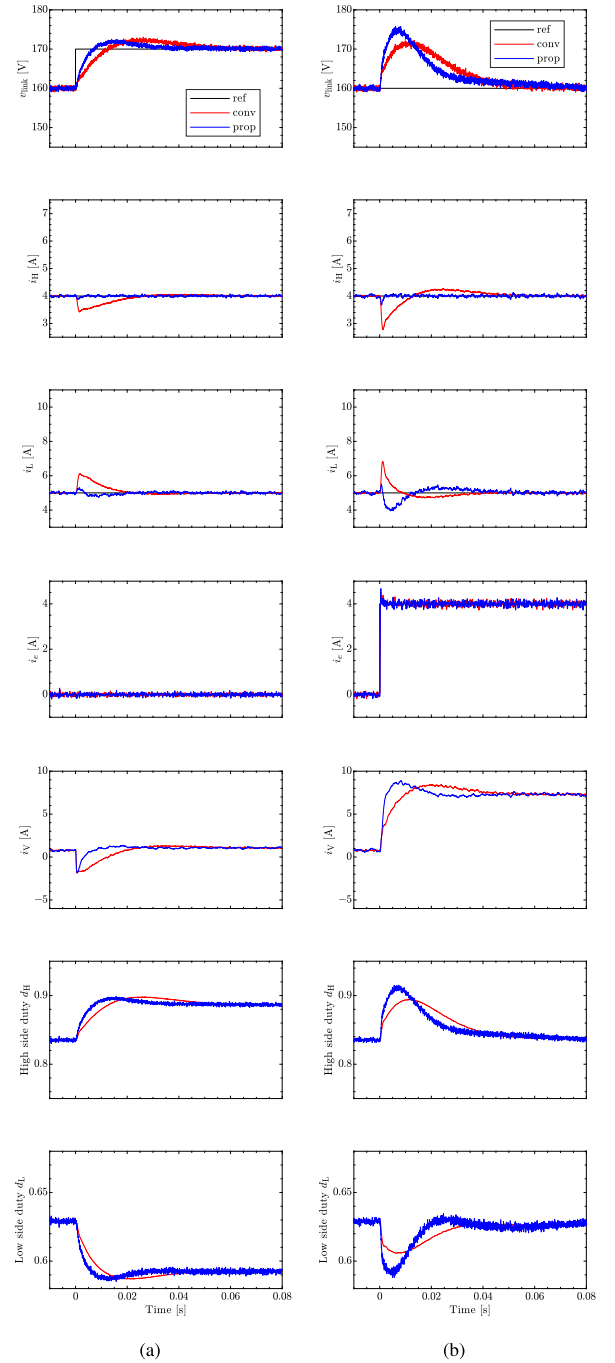


Fig. 14. Disturbance step responses of the system with Fig. 12 when  $I_H^* = 4$  A and  $I_L^* = 5$  A. (a)  $i_V$ ,  $i_H$ ,  $i_L$ ,  $i_e$ ,  $i_V$ ,  $d_H$ , and  $d_L$  of  $v_{link}^*$  step from 160 to 170 V. (b)  $i_V$ ,  $i_H$ ,  $i_L$ ,  $i_e$ ,  $i_V$ ,  $d_H$ , and  $d_L$  of  $i_e^*$  step from 0 to 4 A.

and  $v_{link}$  of the step responses to test the effects of the disturbance current and voltage.

Fig. 12 shows the experimental circuit diagram of the system. The system consists of four converters. Two converters are the proposed system, which is a boost converter and a buck converter. Other converters are a current disturbance converter and a voltage controlled converter. The parameters of the system are listed in Table IV. The controller of the current disturbance converter is designed in the same equations as (18) except for angular frequency. The angular frequency of the current disturbance converter  $\omega_e$  is 800 Hz, and the controller is installed with

the proposed method for the sake of following the disturbance current command value. The voltage converter controller is also designed according to (19), and the current controller is the same in the lower boost converter.

Fig. 13 shows the current step responses of the system. The overshoot or undershoot currents and settling time are higher and longer than the conventional method in both current step responses in Fig. 13(a) and (b). The dc link voltage also shows shorter convergence in Fig. 13, but the overshoot or undershoot voltage is higher than the conventional method, which results from the excessive injection current to the dc link capacitors compared to the conventional method. The fluctuation of the  $i_L$  in Fig. 13(a) is observed for the linearizing error of the state-space equations and the remaining low frequency response of Fig. 7. These phenomena are also observed in higher response in  $i_V$ . The duty command of the proposed method has resulted in the compensation of the dc link voltage. However, the output currents show little fluctuation of the converged state compared to the duty noise. To eliminate the fluctuation, a noise filter should be implemented after the voltage sensor considering the delay. This delay may reduce the effectiveness of active decoupling and affect stability and characteristics. Even in such cases, stability and characteristics can be evaluated by verifying the Bode diagram and Nyquist diagram shown in Sections IV-B and IV-C. The proposed method is decoupled between each current; for this reason, the converged time of the currents and voltage is short.

Fig. 14 shows the disturbance step responses of the system. The overshoot currents  $i_H$  and  $i_L$  are significantly reduced compared to the conventional method. The converged time of the currents and the dc link voltage is also decreased for the same reason as in Fig. 13.

Table V summarizes the comparisons between the conventional and the proposed method. Both the converged time and overshoot or undershoot of the currents decrease in all step responses. Also, the converged time of the voltages is shorter than the conventional method due to faster current responses.

## V. CONCLUSION

This article has proposed multiple converters connecting to the same dc link voltage. First of all, the dynamic current decoupling method of the MIMO system has been proposed. The model-based analysis concludes that the first-order systems were obtained by compensating the dc link voltage at the inputs. The proposed method only uses the dc link voltage and does not use the system parameters. The bench system has been tested to verify the decoupling performance by the Bode plots, Nyquist plots, and step response. The experimental Bode diagrams obtained by system identification confirmed that the conventional and proposed methods were consistent with the analytical results. Furthermore, the proposed method suppresses the interference of off-diagonal terms by approximately  $-20$  dB. In addition, the RGA calculation from the experimental Bode diagrams confirmed that the diagonal terms were almost linear and the off-diagonal terms were decoupled by  $-40$  dB. Nyquist plots have also confirmed that the conventional control might deteriorate the stability for the Gershgorin bands analysis, and

the proposed method is stable in both the SISO Nyquist diagrams and the Gershgorin bands. Step responses have also verified that the proposed control suppresses the overshoot voltage and currents compared with the conventional control and suppresses the converged time faster than the conventional control. Future work would remain on the periodic fluctuation and the large current change resulting from grid current, as well as designing the voltage controller considering the grid current, and the high-frequency converter used in gallium nitride (GaN) devices.

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