

# A Clamped IPT System With Adaptive Mode Switching Against Large Coupling Variations

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**Abstract**—Misalignment issue is almost inevitable in an inductive power transfer (IPT) system, leading to unstable power transfer due to the coupling variations. In order to improve the flexibility of the IPT system, the misalignment range of stable power output is desired to be as large as possible. This article proposes a clamped IPT system to improve antimisalignment ability based on the dual-mode operation. The clamped circuit is constructed with a coil and a rectifier connected to the input dc terminal of the inverter. With the effect of the clamped circuit, the operating mode of the system can be adaptively switched to match the required coupling variation region without coupling identification, output detection, or feedback communication. Then, the analysis and parametric design of the system are elaborated. Finally, a 480-W experimental setup was built to verify the feasibility of the proposed method. Experimental results show that the proposed method can maintain stable output power between 440 and 480 W with the coupling varying from 0.14 to 0.39, while the efficiency is from 83.22% to 93.55%.

**Index Terms**—Clamped circuit, coupling variation, inductive power transfer (IPT), parameters design, stable power transfer.

## I. INTRODUCTION

CURRENTLY, the inductive power transfer (IPT) technique has been used in many applications due to its attractive advantages, such as flexibility, convenience, safety, and user-friendliness. As one of the key indicators to evaluate system reliability, the misalignment tolerance ability of the IPT system has drawn much attention from researchers.

To restrain the fluctuation of the power, a common method is to introduce a control strategy into the IPT system so that the dc-dc converter, full-bridge inverter, and active rectifier can realize the desired misalignment insensitive output [1], [2], [3]. Besides, a variable inductor is proposed to keep the output stable versus misalignment [4], [5]. However, the controller may suffer from an extensive range of modulation depth with a large coupling variation, resulting in a decline in stability and efficiency [6].

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Moreover, multivariable control strategies are proposed to improve the antimisalignment performance [7]. However, more control variables increase the system's complexity. Although the control strategy is an effective and active approach to addressing the misalignment problem, output detection and wireless communication are required.

In order to simplify the complexity of the system, many researchers have advocated improving misalignment tolerance by employing the inherent characteristic of the IPT system, including the design of coils [8], [9], [10] and topologies [11], [12], [13], [14], [15], [16], [17], [18], [19], [20], [21], [22]. For the design of coils, many magnetic couplers are proposed to stabilize the system output when misalignment occurs, such as the asymmetric coil [8], three-coil structure [9], and double-D coil [10]. The principle of coils design is to maintain the coupling coefficient stable so that the misalignment ability of the system is improved in one or two directions.

As an alternative solution, topology design methods are proposed, including hybrid topologies, and detuned topologies. The concept of hybrid topology was previously introduced by Zhao et al. [11]. With the interaction of two topologies with opposite output trends to pad misalignment, the total transfer power can maintain relatively constant. Similar approaches were proposed and expanded in [12] and [13]. Furthermore, Qu et al. [14] construct a family of hybrid topologies and synthetically analyze the design principles and characteristics for all hybrid topology systems. Usually, the hybrid topologies formed by LCC-LCC and S-S topologies [11] or S-LCC and LCC-S topologies [12] are employed to achieve a higher misalignment tolerance. Since the unique feature of merging with two compensation topologies, the complexity and high cost are inevitable. By contrast, the detuned circuit is simpler. Through the special design of compensation parameters, the primary current can be adaptively adjusted to obtain stable transfer power versus the coupling variation. There are a lot of works recording the antimisalignment performance of different detuned circuits. And a series of high-order compensation topologies with optimized parameters are proposed to ensure high misalignment tolerance, such as S-S [7], S-SP [15], LCC-S [16], S-CLC [17], double-T [18], and X-type topology [19]. Besides, a family of compensation topologies with secondary parallel compensation is proven to have strong misalignment tolerances [20]. However, the allowable coupling variation of this method needs to be further developed.

As we know, the profile of transfer power versus coupling variation ( $P$ - $k$  profile) is determined once the parameters of the

circuit are designed. To extend the misalignment distance, the reconfigurable IPT system with multimode operation is proposed [21], [22], [23], [24]. With the assistance of extra coils or reactive elements with active switching devices, the circuit structure can be changed to adjust the  $P$ - $k$  profile so that the desired output power can be obtained within a larger coupling range. A detuned reconfigurable topology is proposed in [21], which utilizes a switch to convert between the detuned LCC-S topology and the detuned S-S topology so that stable power can be obtained within the coupling range of (0.1–0.25). In [22], a reconfigurable resonant coil is employed to widen the range of coupling based on the complementary power profile of different coils. Besides, a reconfigurable topology combining the S-S and LCCC-S topologies is proposed to enhance power transfer capability and tolerate weak couplings [23]. Moreover, a reconfigurable rectifier-based detuned S-S compensated IPT system is proposed to tolerate an extensive coupling [24]. Although stable power transfer is achieved chiefly, accurate coupling identification (or output detection) and feedback communication are required, increasing control circuit complexity and reducing the system reliability. If the system can match the operation mode adaptively according to the coupling, the system's reliability, ruggedness, and applicability will be further enhanced.

In the past, the diode clamping circuit has attracted the attention of some scholars due to its adaptive on-and-off characteristics. In [25], a half-bridge CLC-S IPT system with clamping diodes is used for primary coil disconnection protection, soft-start, and short-circuit protection. Moreover, The IPT system with primary [26] and secondary [27] diode clamping circuit were proposed to adaptively regulate the operation mode for battery charging. However, these methods are only proposed on the condition of a fixed coupling coefficient.

To address the above-mentioned issue, a clamped IPT system is proposed to enhance the misalignment tolerance in this article. With the assistance of the primary clamp circuit, the operation modes of the system can adaptively alter from one to the other without detection or feedback communication devices. Besides, a parameter design method taking account of dual-mode is proposed to maintain stable power output in the misalignment case. With the cooperation of different operation modes, the system can obtain a strong antimisalignment capacity.

The rest of this article is organized as follows. The analysis of the clamped IPT system is described in Section II. A parametric design criterion is presented in Section III. In Section IV, a 480 W prototype was constructed to verify the theoretical analysis. Finally, the conclusion is drawn in Section V.

## II. THEORETICAL ANALYSIS

The proposed clamped IPT system is shown in Fig. 1, consisting of a power input loop, a power output loop, and a clamp loop. The corresponding current is expressed in each loop by  $I_p$ ,  $I_s$ , and  $I_c$ , respectively.  $X_p$ ,  $X_s$ , and  $X_c$  are the equivalent reactance of each loop, which are given as follows:

$$\begin{cases} X_p = \omega L_{cp} + \omega L_p - 1/\omega C_p \\ X_s = \omega L_s - 1/\omega C_s \\ X_c = \omega L_{cc} - 1/\omega C_c \end{cases} \quad (1)$$

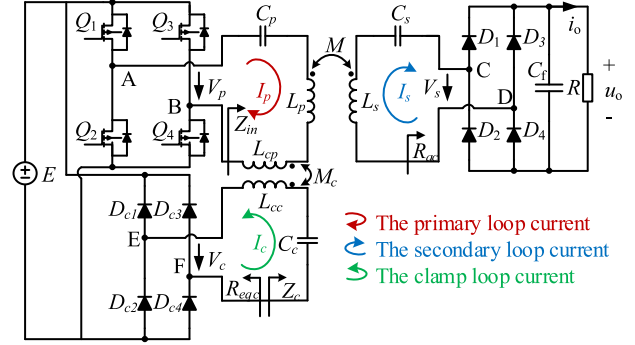


Fig. 1. Clamped IPT system.

where  $\omega$  is the angular frequency,  $C_p$ ,  $C_s$ , and  $C_c$  are the compensation capacitor of each loop,  $L_p$  ( $L_{cp}$ ) and  $L_s$  ( $L_{cc}$ ) are the self-inductances of the loosely coupled transformer (clamp transformer). And  $C_s$  is used to compensate the self-inductance  $L_s$  fully, i.e.,  $X_s = 0$ .

$E$  is the input dc voltage of the inverter ( $Q_{p1} - Q_{p4}$ ) and the output dc voltage of the rectifier ( $D_{c1} - D_{c4}$ ).  $V_p$  is the output ac voltage of the inverter ( $Q_{p1} - Q_{p4}$ ).  $V_s$  ( $R_{ac}$ ) and  $V_c$  ( $R_{eqc}$ ) are used to represent the ac input voltage (the equivalent ac loads) of the rectifier constituted by ( $D_{s1} - D_{s4}$ ) and ( $D_{c1} - D_{c4}$ ).  $Z_c$  is the output impedance of the system reflected in the clamped circuit.  $R$  is the dc load of the rectifier ( $D_{s1} - D_{s4}$ ). According to Kirchhoff's voltage law, the system can be described as follows:

$$\begin{cases} V_p = jX_p I_p - j\omega M I_s + j\omega M_c I_c \\ V_s = R_{ac} I_s = j\omega M I_p - jX_s I_s \\ V_c = R_{eqc} I_c = j\omega M_c I_p + jX_c I_c \end{cases} \quad (2)$$

where  $M$  ( $M_c$ ) is the mutual inductance of the loosely coupled transformer (clamp transformer), which can be expressed by  $M = k\sqrt{L_p L_s}$  and  $k$  represents the coupling coefficient of the loosely coupled transformer.

The relationship between  $E$  and  $V_p$ ,  $R$  and  $R_{ac}$  can be expressed as follows [21]:

$$E = V_p \sqrt{2\pi}/4, R_{ac} = 8R/\pi^2. \quad (3)$$

For the clamped loop, there are three operation modes [26]: the turned-OFF mode, the partly activated mode, and the fully active mode. The analysis of the different modes is given as follows.

### A. Analysis of Turned-Off or Partly Activated Mode

Assumed that the clamped loop is turned OFF, the rectifier bridge ( $D_{c1} - D_{c4}$ ) cannot be conducted, and the current  $I_c$  in the clamp loop will be considered as zero, as follows:

$$I_c = 0 \left( \sqrt{2} |V_c| \leq E \right). \quad (4)$$

In this case, the system can be considered as a detuned S-S topology, as Fig. 2. Then, (2) can be described as follows:

$$\begin{cases} V_p = jX_p I_p - j\omega M I_s \\ 0 = -j\omega M I_p + R_{ac} I_s + jX_s I_s \end{cases} \quad (5)$$

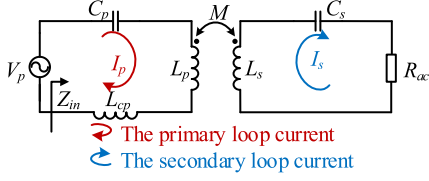


Fig. 2. Detuned S-S topology.

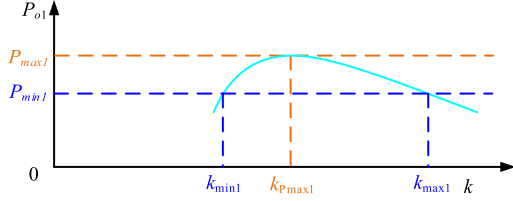


Fig. 3. Curve of the output power  $P_{o1}$  in the turned-OFF or partly activated mode, where  $P_{\max 1}$  is the maximum output power,  $k_{p\max 1}$  is the corresponding coupling coefficient,  $P_{\min 1}$  is presumed minimum output power, and the corresponding couplings are  $k_{\min 1}$  and  $k_{\max 1}$ .

Substituting  $X_s = 0$  and (4) into (5),  $I_p$  and  $I_s$  can be obtained as follows:

$$\begin{cases} I_p = \frac{V_p R_{ac} (L_p L_s \omega^2 k^2 - j X_p R_{ac})}{X_p^2 R_{ac}^2 + L_p^2 L_s^2 \omega^4 k^4} \\ I_s = \frac{V_p \sqrt{L_p L_s} \omega k (X_p R_{ac} + j L_p L_s \omega^2 k^2)}{X_p^2 R_{ac}^2 + L_p^2 L_s^2 \omega^4 k^4} \end{cases} \quad (6)$$

From (6), the input impedance  $Z_{in}$  and the input impedance angle  $\theta$  can be derived as follows:

$$\begin{cases} Z_{in} = \frac{V_p}{I_p} = \frac{L_p L_s \omega^2 k^2}{R_{ac}} + j X_p \\ \theta = \arctan \left( \frac{X_p R_{ac}}{L_p L_s \omega^2 k^2} \right) \end{cases} \quad (7)$$

Moreover, the output power  $P_{o1}$  can be calculated as (8), which can be viewed as a function of the coupling  $k$ , and the corresponding curve is depicted in Fig. 3.

$$P_{o1}(k) = |I_s|^2 R_{ac} = \frac{V_p^2 R_{ac} \omega^2 L_p L_s k^2}{X_p^2 R_{ac}^2 + L_p^2 L_s^2 \omega^4 k^4} \quad (8)$$

Setting the derivative of  $P_{o1}$  to zero, i.e.,  $dP_{o1}/dk = 0$ , the coupling coefficient  $k_{p\max 1}$  corresponding to the maximum output power  $P_{\max 1}$  can be solved as follows:

$$k_{p\max 1} = \sqrt{\frac{X_p R_{ac}}{\omega^2 L_p L_s}} \quad (9)$$

Substituting (9) into (8), the maximum output power  $P_{\max 1}$  can be given as follows:

$$P_{\max 1} = \frac{V_p^2}{2X_p} \quad (10)$$

Then, the presumed minimum output power  $P_{\min 1}$  satisfies

$$P_{\min 1} = P_{o1}(k_{\min 1}) = P_{o1}(k_{\max 1}) \quad (11)$$

A variable  $\beta$  is defined to describe the power fluctuation, i.e.,

$$\beta = \frac{P_{\max 1} - P_{\min 1}}{P_{\max 1} + P_{\min 1}} \quad (12)$$

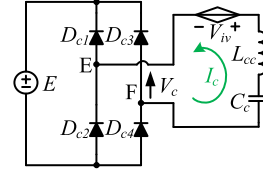
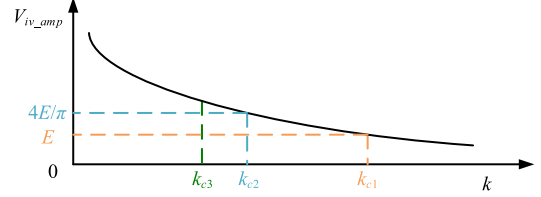


Fig. 4. Controlled source equivalent circuit of the clamp loop.

Fig. 5.  $V_{iv\_amp}$  profile versus the coupling  $k$ .

Substituting (12) into (10),  $P_{\min 1}$  can be calculated as follows:

$$P_{\min 1} = \frac{V_p^2 (1 - \beta)}{2X_p (1 + \beta)} \quad (13)$$

Substituting (13) into (8),  $k_{\min 1}$  and  $k_{\max 1}$  can be obtained as follows:

$$\begin{cases} k_{\min 1} = \sqrt{\frac{X_p R_{ac} (1 - \sqrt{\beta})}{\omega^2 L_p L_s (1 + \sqrt{\beta})}} \\ k_{\max 1} = \sqrt{\frac{X_p R_{ac} (1 + \sqrt{\beta})}{\omega^2 L_p L_s (1 - \sqrt{\beta})}} \end{cases} \quad (14)$$

## B. Analysis of the Transformation Process

1) *First Critical Coupling Coefficient*: Fig. 4 shows the controlled source equivalent circuit of the clamp loop in the clamped IPT system. With the effect of the clamp transformer, the induced voltage  $V_{iv}$  generated from the primary loop current, and the corresponding amplitude  $V_{iv\_amp}$  can be calculated as shown in the following equation:

$$\begin{cases} V_{iv} = j M_c I_p = -\frac{V_p \omega M_c R_{ac} (X_p R_{ac} + j L_p L_s \omega^2 k^2)}{X_p^2 R_{ac}^2 + L_p^2 L_s^2 \omega^4 k^4} \\ V_{iv\_amp} = \sqrt{2} |V_{iv}| = \sqrt{\frac{2V_p^2 \omega^2 M_c^2 R_{ac}^2}{X_p^2 R_{ac}^2 + L_p^2 L_s^2 \omega^4 k^4}} \end{cases} \quad (15)$$

Because the clamp loop is in a turn-OFF state,  $V_{iv}$  and  $V_{iv\_amp}$  are also equal to  $V_c$  and the corresponding amplitude  $V_c \cdot amp$ . When the IPT system has the misalignment issue, the coupling coefficient  $k$  will decrease, and  $V_{iv\_amp}$  will increase according to (15), which can be drawn in Fig. 5. Once  $V_{iv\_amp}(V_c \cdot amp)$  is more than  $E$ , the rectifier ( $D_{c1} - D_{c4}$ ) will be activated. Hence, letting  $V_{iv\_amp} = E$  and combining (3) and (15), the corresponding critical coupling coefficient  $k_{c1}$  can be calculated as follows:

$$k_{c1} = \sqrt[4]{\frac{16M_c^2 R_{ac}^2}{\pi^2 \omega^2 L_p^2 L_s^2} - \frac{X_p^2 R_{ac}^2}{\omega^4 L_p^2 L_s^2}} \quad (16)$$

2) *Second Critical Coupling Coefficient*: Assumed that the clamped loop is opportunely fully activated, the relationship

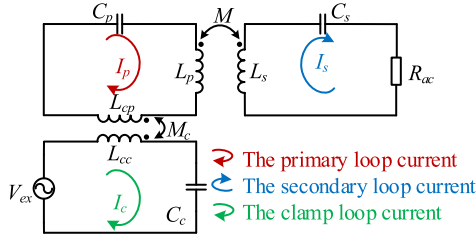


Fig. 6. Equivalent circuit with the external power.

between  $E$  and  $V_c$  satisfies

$$V_c = V_p = 2\sqrt{2}E/\pi. \quad (17)$$

And the corresponding amplitude  $V_{c\_amp}$  can be expressed as follows:

$$V_{c\_amp} = \sqrt{2}V_p = 4E/\pi. \quad (18)$$

Theoretically, under ideal conditions where there are no harmonics in the system, the clamped circuit can be fully activated when  $V_{iv\_amp} \geq 4E/\pi$ . Substituting (18) into (15), the second critical coupling coefficient  $k_{c2}$  can be expressed as follows:

$$k_{c2} = \sqrt[4]{\frac{M_c^2 R_{ac}^2}{\omega^2 L_p^2 L_s^2} - \frac{X_p^2 R_{ac}^2}{\omega^4 L_p^2 L_s^2}}. \quad (19)$$

However, the harmonics are not evitable because of the nonsinusoidal inverter output voltage and rectifier input voltage. Due to the effect of harmonic current [28], [29], the rectifier bridge ( $D_{c1} - D_{c4}$ ) may operate in a discontinuous conduction mode (DCM) even  $V_{iv\_amp} \geq 4E/\pi$ . Namely, suppose the coupling coefficient  $k$  is slightly less than  $k_{c2}$  in practice, the clamped circuit may still be partly activated.

3) *Third Critical Coupling Coefficient*: According to the work in [28] and [29], the boundary of the critical mode between DCM and continuous conduction mode (CCM) can be given as follows:

$$\pi R_{eqc}/4 = \omega \lim_{m \rightarrow \infty} Z_{c(2m+1)}/(2m+1)\omega \quad (20)$$

where  $R_{eqc}$  is the critical equivalent ac load of the rectifier constituted by  $D_{c1} - D_{c4}$  between DCM and CCM,  $Z_{c(2m+1)}$  is the high-frequency output impedance of the clamped IPT system reflected in the clamped circuit, which can be obtained as follows.

Because the output impedance is the same as the Thevenin equivalent at the output terminals, thus, we can simplify the circuit to solve the output impedance based on the external excitation method [30]. First, the independent power should be set to zero, namely the independent square wave voltage source of the primary loop should be short-circuited. Then, we can add an external power  $V_{ex}$  to calculate the input impedance at different frequencies  $\omega$ . Finally, the corresponding equivalent circuit with external power can be described in Fig. 6, which

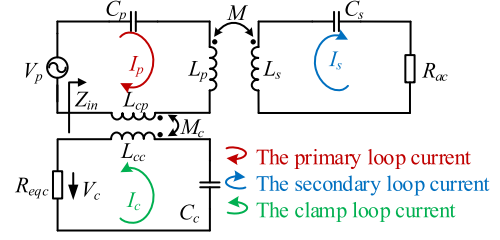


Fig. 7. Simplified circuit.

can be described as follows:

$$\begin{cases} 0 = jX_{p(2m+1)}I_p - j(2m+1)\omega MI_s \\ \quad + j(2m+1)\omega M_c I_c \\ 0 = -j(2m+1)\omega MI_p + jX_{s(2m+1)}I_s + R_{ac}I_s \\ V_{ex} = j(2m+1)\omega M_c I_p + jX_{c(2m+1)}I_c \end{cases} \quad (21)$$

where  $X_{p(2m+1)}$ ,  $X_{s(2m+1)}$ , and  $X_{c(2m+1)}$  are the equivalent reactance of each loop when the angular frequency is  $(2m+1)\omega$ .

Then,  $Z_{c(2m+1)}$  can be calculated as given in (22) shown at the bottom of the next page, by solving (21). Substituting (20) into (2), the third critical coupling coefficient  $k_{c3}$  can be calculated as (23) shown at the bottom of the next page.

Therefore, when the coupling coefficient  $k$  satisfies  $k_{c3} < k < k_{c1}$ , the clamped circuit is partly activated. In this process, the clamped loop current  $I_c$  can be considered a very small value [26]. We can approximatively regard the system as a detuned S-S topology.

### C. Analysis of Fully Activated Mode

When  $k \leq k_{c3}$ , the clamped circuit is fully activated, and the system can be simplified as shown in Fig. 7. Combining (2) and (17), the system can be rewritten as

$$\begin{cases} V_p = jX_p I_p - j\omega M I_s + j\omega M_c I_c \\ V_s = R_{ac} I_s = j\omega M I_p - jX_s I_s \\ V_p = R_{eqc} I_c = j\omega M_c I_p + jX_c I_c \end{cases} \quad (24)$$

Similarly, substituting  $X_s = 0$  into (24), the input impedance, the input impedance angle, and the output power can be obtained as follows:

$$\begin{cases} Z_{in} = \frac{V_p}{I_p} = \frac{L_p L_s \omega^2 k^2}{R_{ac}} + \frac{\omega^2 M_c^2 (R_{eqc} - jX_c)}{X_c^2 + R_{eqc}^2} + jX_p \\ \theta = \arctan\left(\frac{R_{ac}(X_p X_c + X_p R_{eqc}^2 - \omega^2 M_c^2 X_c)}{L_p L_s \omega^2 k^2 (X_c^2 + R_{eqc}^2) + R_{ac} R_{eqc} \omega^2 M_c^2}\right) \end{cases} \quad (25)$$

$$\begin{aligned} P_{o2}(k) &= |I_s|^2 R_{ac} \\ &= \frac{V_p^2 R_{ac} L_p L_s \omega^2 k^2 (X_c - \omega M_c)^2}{R_{ac}^2 (X_p X_c - \omega^2 M_c^2)^2 + L_p^2 L_s^2 \omega^4 k^4 X_c^2}. \end{aligned} \quad (26)$$

From (26), the variation tendency of the output power  $P_{o2}$  is similar to  $P_{o1}$ , which can be depicted in Fig. 8 to distinguish  $P_{o1}$ . Setting the derivative of  $P_{o2}$  to zero, the maximum output power  $P_{max2}$  and the corresponding coupling coefficient  $k_{pmax2}$

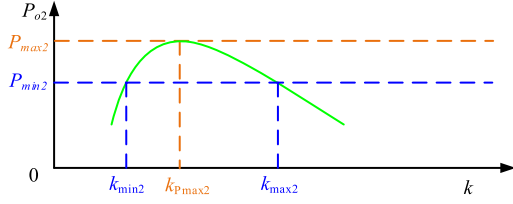


Fig. 8. Curve of the output power  $P_{o2}$  in the fully activated mode, where  $P_{max2}$  is the maximum output power,  $k_{pmax2}$  is the corresponding coupling coefficient,  $P_{min2}$  is presumed minimum output power, and the corresponding couplings are  $k_{min2}$  and  $k_{max2}$ .

can be calculated as follows:

$$\begin{cases} k_{pmax2} = \sqrt{\frac{R_{ac}(X_p X_c - \omega^2 M_c^2)}{\omega^2 X_c L_p L_s}} \\ P_{max2} = \frac{V_p^2 (X_c - \omega M_c)^2}{2X_p X_c^2 - 2X_c \omega^2 M_c^2} \end{cases} \quad (27)$$

Moreover, the presumed minimum output power  $P_{min2}$  satisfies

$$P_{min2} = P_{o2}(k_{min2}) = P_{o2}(k_{max2}). \quad (28)$$

Then,  $\beta$  also can be employed to describe the power fluctuation in this case, namely

$$\beta = \frac{P_{max2} - P_{min2}}{P_{max2} + P_{min2}}. \quad (29)$$

Similarly,  $P_{min2}$ ,  $k_{min2}$ , and  $k_{max2}$  can be calculated as follows:

$$\begin{cases} P_{min2} = \frac{V_p^2 (1-\beta)(X_c - \omega M_c)^2}{2(1+\beta)(X_p X_c^2 - X_c \omega^2 M_c^2)} \\ k_{min2} = \sqrt{\frac{R_{ac}(X_p X_c - \omega^2 M_c^2)(1-\sqrt{\beta})}{\omega^2 L_p L_s X_c (1+\sqrt{\beta})}} \\ k_{max2} = \sqrt{\frac{R_{ac}(X_p X_c - \omega^2 M_c^2)(1+\sqrt{\beta})}{\omega^2 L_p L_s X_c (1-\sqrt{\beta})}} \end{cases} \quad (30)$$

Compared with the traditional detuned circuit, the proposed IPT system has two maximum power points according to (10) and (27), i.e.,  $P_{max1}$  and  $P_{max2}$ . If the parameters are reasonably designed, the two top power points can be employed so that the system has a wide coupling range with stable output power in misalignment conditions.

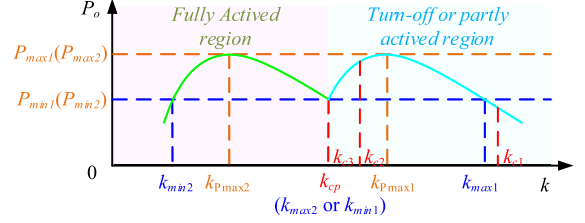


Fig. 9. Output power curve versus coupling.

### III. SYSTEM DESIGN

#### A. Circuit Parameters Design

In order to achieve stable power transfer versus a large coupling variation, the output power curves of the two modes should overlap at the minimum output power  $P_{min}$ , as shown in Fig. 9. For readability, a variable  $k_{cp}$  is used to express the coupling coefficient of the coincidence point. Ideally, the maximum output power should be the same in the two modes. Then, the constraints can be concluded as follows [21]:

$$\begin{cases} k_{min1} = k_{max2} = k_{cp} \\ P_{max1} = P_{max2} \\ P_{min1} = P_{min2} \end{cases} \quad (31)$$

Substituting (10), (13), (14), (27), and (30) into (31), the constraints can be rewritten as follows:

$$\begin{cases} \sqrt{\frac{X_p R_{ac}(1-\sqrt{\beta})}{\omega^2 L_p L_s (1+\sqrt{\beta})}} = k_{cp} \\ \sqrt{\frac{R_{ac}(X_p X_c - \omega^2 M_c^2)(1+\sqrt{\beta})}{\omega^2 L_p L_s X_c (1-\sqrt{\beta})}} = k_{cp} \\ \frac{X_p X_c^2 - X_c \omega^2 M_c^2}{X_p (X_c - \omega M_c)^2} = 1 \end{cases} \quad (32)$$

Solving (32),  $X_p$ ,  $X_c$ , and  $M_c$  can be calculated as follows:

$$\begin{cases} X_p = \frac{L_p L_s \omega^2 k_{cp}^2 (1+\sqrt{\beta})}{R_{ac}(1-\sqrt{\beta})} \\ X_c = \frac{L_p L_s \omega^2 k_{cp}^2 (1-\beta)}{R_{ac} \sqrt{\beta} (1-\sqrt{\beta})^2} \\ M_c = \frac{2L_p L_s \omega k_{cp}^2}{R_{ac}(1-\sqrt{\beta})} \end{cases} \quad (33)$$

$$Z_{c(2m+1)} =$$

$$\frac{V_{ex}}{I_c} = jX_{c(2m+1)} + \frac{(2m+1)^2 \omega^2 M_c^2 \left( (2m+1)^2 \omega^2 k^2 L_p L_s (R_{ac} + jX_{s(2m+1)}) - jX_{p(2m+1)} R_{ac}^2 - jX_{p(2m+1)} X_{s(2m+1)}^2 \right)}{\left( X_{p(2m+1)} X_{s(2m+1)} - (2m+1)^2 \omega^2 k^2 L_p L_s \right)^2 + X_{p(2m+1)} R_{ac}^2} \quad (22)$$

$$k_{c3} =$$

$$\sqrt{\frac{R_{ac} \left( \sqrt{(X_c^2 + R_{eqcc}^2)} (\omega^2 M_c^2 R_{eqcc}^2 - X_p^2 X_c^2) - (X_p R_{eqcc}^2 - \omega^2 M_c^2 X_c)^2 + X_p X_c^2 (2X_c \omega^2 M_c^2 - X_p R_{eqcc}^2) - \omega^2 M_c^2 R_{eqcc} \right)}{L_p L_s \omega^2 (X_c^2 + R_{eqcc}^2)}} \quad (23)$$

TABLE I  
 PARAMETER VALUES

Parameter	Value	Parameter	Value
$\omega$	$2 \times \pi \times 250$ kHz	$R$	20 $\Omega$
$\beta$	5.6%	$k_{cp}$	0.25
$L_p$	48.87 $\mu$ H	$L_s$	45.77 $\mu$ H
$X_p$	34.47 $\Omega$	$X_c$	145.66 $\Omega$
$M_c$	35.49 $\mu$ H		

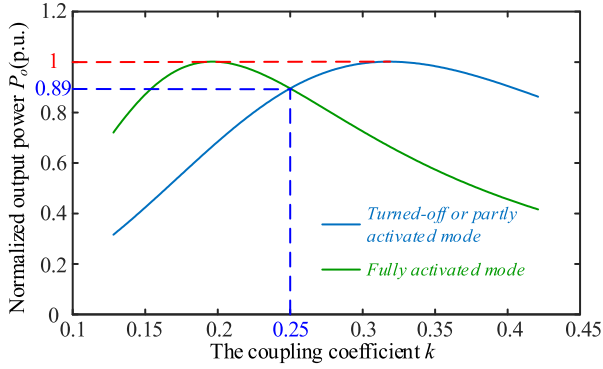


Fig. 10. Theoretical transfer power curve.

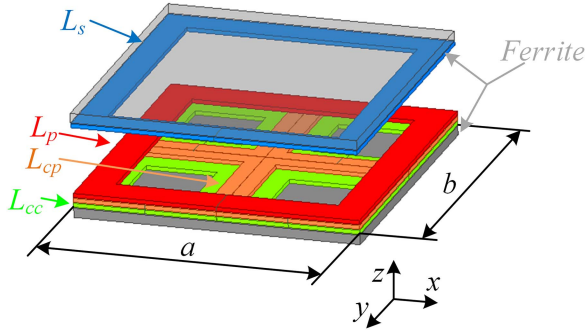


Fig. 11. Magnetic coupler using QDQP structure.

As an example, we can substitute the parameters listed in Table I into (33),  $X_p$ ,  $X_c$ , and  $M_c$  can be calculated and the corresponding results are listed in Table I. Substituting the parameters of Table I into (8) and (26), the transfer power can be depicted as Fig. 10. The power curves accord with our expectations.

Through the above circuit parameter design method, we can create the desired power curve. However, the transition between the different modes is still uncertain. According to the analysis of Section II, the conversion between the two modes depends on  $k_{c3}$ . Hence,  $k_{cp}$  should be equal to  $k_{c3}$  so that one mode can be smoothly switched to another, as Fig. 9. From (20) to (23),  $k_{c3}$  is related to all circuit parameters. Thus, we can design the clamp transformer to make  $k_{c3}$  reach the predetermined value.

### B. Coupled Structure Design

To eliminate the coupling between the clamp loop and the secondary side loop, a quadruple D quadrate pad (QDQP) [12], [31], [32] is adopted, as shown in Fig. 11. It is noted that the stand-alone inductor has almost identical electrical performance

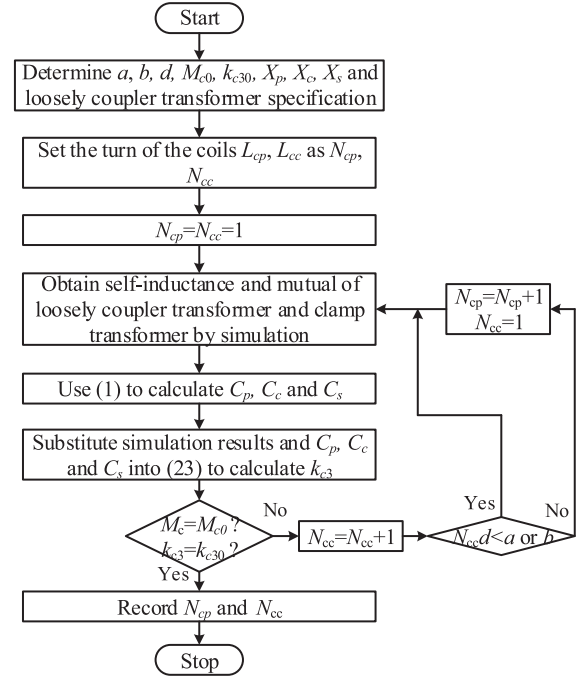


Fig. 12. Flowchart for the design of clamp transformer, where  $a$  and  $b$  are length and width,  $d$  is Litz wire diameter,  $M_{c0}$  and  $k_{c30}$  are the predetermined mutual inductance of clamp transformer and critical coupling coefficient of the loosely coupled transformer.

as the integrated inductor [31]. Hence, a tightly coupled transformer can also be used to form a clamp transformer [33]. However, the hardware volume is increased inevitably. Thus, this work uses a compact magnetic coupler scheme, i.e., QDQP structure. Similar to the coil structure of the conventional IPT system, two quadrate pads (QP) are placed on the primary and secondary sides to form the loosely coupled transformer. The difference is that two quadruple D pads (QDP) on the primary and clamp loop form the clamp transformer. Hence, the magnetic design of this work is focused on the clamp transformer. For the QDP, the direction of the current in the adjacent coils should be opposite to create the orthogonal magnetic flux with QP [12]. Due to the symmetrical, the magnetic flux passing from QDP (QP) to QP (QDP) is zero in ideal conditions, so the loosely coupled transformer and clamp transformer can be decoupled.

After obtaining the design value of  $M_c$ , the clamp coil can be designed to meet the requirements of the mutual inductor while adjusting the self-inductance of the clamp coil so that  $k_{c3}$  reaches the preset value. The detailed design procedures are given in Fig. 12. First, we can predetermine the length  $a$  and width  $b$  of clamp coils, the Litz wire diameter  $d$ , the mutual inductance  $M_{c0}$  of clamp transformer, the third critical coupling coefficient  $k_{c30}$ , the primary loop equivalent reactance  $X_p$ , the clamp loop equivalent reactance  $X_c$ , the secondary loop equivalent reactance  $X_s$ , and loosely coupled transformer specification. Then, the turn of clamp coils is initialized. Next, we can obtain the coil parameters (self-inductance and mutual) of the loosely coupled transformer and clamp transformer by Maxwell. Subsequently,  $C_p$ ,  $C_c$ , and  $C_s$  can be calculated according to (1). Next, the third critical

TABLE II  
COILS' SELF-INDUCTANCES AND CAPACITOR

Parameter	Design value	Parameter	Design value
$L_p$	48.87 $\mu\text{H}$	$L_s$	45.77 $\mu\text{H}$
$L_{cc}$	98.47 $\mu\text{H}$	$L_{cp}$	27.33 $\mu\text{H}$
$C_p$	7.47 nF	$C_c$	70.06 nF
$C_s$	8.85 nF		

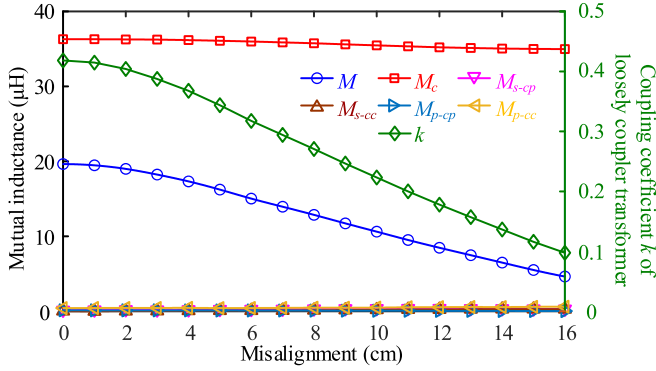


Fig. 13. Mutual inductance between coils with x-misalignment.

coupling can be calculated by substituting simulation results and  $C_p$ ,  $C_c$ , and  $C_s$  into (23). Finally, the mutual inductance of the clamp transformer and the third critical coupling can be evaluated to determine whether they are equal to the preset value  $M_{c0}$  and  $k_{c30}$ . If yes, the turn of clamp coils will be recorded. Otherwise, the turn of clamp coils will be regulated to repeat the above procedures.

As an example, the length and width of the clamp transformer are set to be the same as the loosely coupled transformer, namely  $a = b = 300$  mm. Besides, according to the design results of circuit parameters,  $M_{c0}$  and  $k_{c30}$  are designed as 35.49  $\mu\text{H}$  and 0.25.  $X_p$ ,  $X_c$ , and  $X_s$  are defined as 34.47, 145.66, and 0  $\Omega$ . As a result,  $N_{cp}$  and  $N_{cc}$  are iterated as 4 and 9, respectively. Then, the measured coils' self-inductances and the calculated capacitor are given in Table II. And the mutual inductance is depicted in Fig. 13 with x-misalignment. It is obvious that the mutual inductance ( $M$ ) and the coupling coefficient ( $k$ ) of the loosely coupled transformer have large variations with misalignments, while the mutual inductance ( $M_c$ ) of the clamp transformer is almost constant. Besides, the cross-couplings ( $M_{p-cp}$ ,  $M_{p-cc}$ ,  $M_{s-cp}$ , and  $M_{s-cc}$ ) between the loosely coupled transformer and clamp transformer are very small and can be ignored. The results of xy-misalignment are offered in Fig. 14. The variation trends of  $M$ ,  $k$ ,  $M_c$ ,  $M_{p-cp}$ , and  $M_{p-cc}$  are similar to x-misalignment, while the cross-couplings ( $M_{s-cp}$  and  $M_{s-cc}$ ) between clamp coils ( $L_{cc}$  and  $L_{cp}$ ) and the secondary coil ( $L_s$ ) cannot be neglected once the diagonal misalignment is larger than 5 cm, which may affect the misalignment performance.

#### IV. EXPERIMENTAL RESULTS

To demonstrate the validity of the proposed method, a 480 W experimental prototype was built, as shown in Fig. 15(a). The coils structure is given in Fig. 15(b), where the quadruple-D

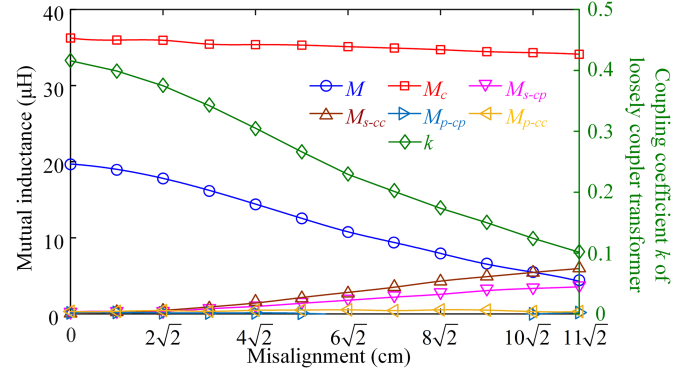


Fig. 14. Mutual inductance between coils with xy-misalignment.

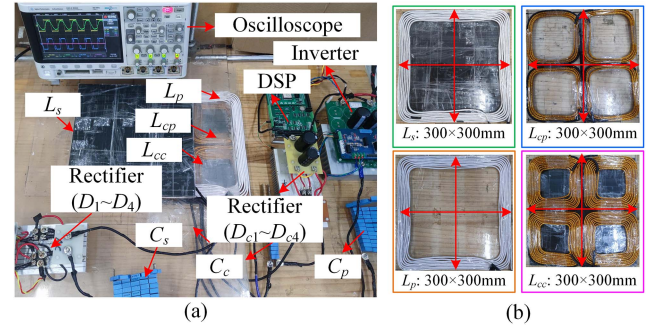


Fig. 15. Experimental prototype. (a) Overall setup. (b) Coils structure.

TABLE III  
PARAMETER VALUES

Parameter	Value	Parameter	Value
$E$	230 V	$\omega$	$2 \times \pi \times 250$ kHz
$L_p$	48.87 $\mu\text{H}$	$L_s$	45.77 $\mu\text{H}$
$L_{cc}$	98.47 $\mu\text{H}$	$L_{cp}$	27.33 $\mu\text{H}$
$M_c$	35.49 $\mu\text{H}$	$C_p$	7.73 nF
$C_c$	70.17 nF	$C_s$	9.02 nF
$k_{c3}$	0.25	$R$	20 $\Omega$
$R_{cp}$	12 m $\Omega$	$R_{cs}$	21 m $\Omega$
$R_{cc}$	18 m $\Omega$	$R_{lp}$	102 m $\Omega$
$R_{lcp}$	57 m $\Omega$	$R_{ls}$	114 m $\Omega$
$R_{lcc}$	172 m $\Omega$		

TABLE IV  
DEVICE'S MODELS

Device	Model
DC power source	Chroma 62150H-600
MOSFETs $Q_1$ - $Q_4$	C2M0080120D
Rectifier diodes $D_1$ - $D_4$	DSEI2 $\times$ 61-06C
Clamp diodes $D_{c1}$ - $D_{c2}$	DSEI2 $\times$ 61-06C
Electronic load	ITECH IT8816B

quadrature pads are used as the clamp transformer to eliminate the cross-coupling with the loosely coupled transformer [12]. According to the proposed parameter design method, a set of parameters are listed in Table III, and the corresponding devices are given in Table IV.

The transfer power and efficiency against coupling variation are given in Fig. 16. The output power is depicted in Fig. 16(a).

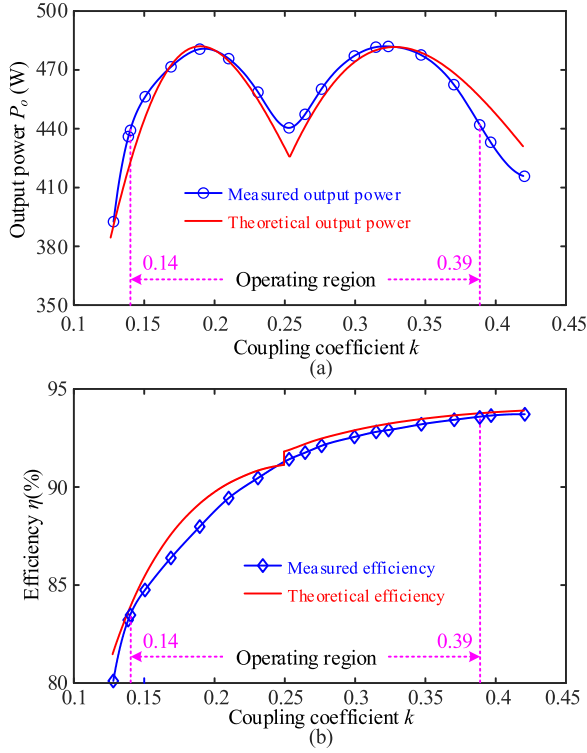


Fig. 16. Experimental and theoretical results of (a) output power and (b) efficiency with x-misalignment.

It can be seen that the output power varies between 440 and 480 W with the coupling  $k$  decreasing from 0.39 to 0.14. The fluctuation of power is only 4.3%, which can be calculated by  $(P_{max} - P_{min})/(P_{max} + P_{min})$ . Additionally, the efficiency is drawn in Fig. 16(b), which decreases from 93.55% to 83.22% within the coupling range [0.14, 0.39]. The efficiency decline is mainly attributed to the reduction of coupling and the extra power loss due to the clamp circuit. The theoretical prediction of the output power and the efficiency are also given in Fig. 16. The maximum error of the output power is 15 W when  $k$  is 0.25, while that of the efficiency is 1.27% when  $k$  is equal to 0.19. Meanwhile, the error is inevitable, and it mainly comes from the deviation of the parameters, the resistance of each reactive element, and the insufficient accuracy of the fundamental approximation method in the partly activated mode of the clamp circuit [26]. Nevertheless, the results still are acceptable.

The experimental waveforms at the two maximum power points are displayed in Fig. 17. When the system works in turned-OFF or partly activated mode, the clamp loop current is small, so the system can be approximately regarded as the detuned SS topology, as shown in Fig. 17(a). Besides,  $I_c$  is distorted due to the harmonic current, leading to the rectifier ( $D_{c1} - D_{c4}$ ) operating in a DCM [28], [29]. With the coupling decrease, the system enters the fully activated mode, as Fig. 17(b). In this case, the rectifier ( $D_{c1} - D_{c4}$ ) is fully conducted, and the clamp loop current cannot be ignored. With the effect of the clamp circuit, the output power still maintains stable from Fig. 16. Besides,  $V_s$  and  $I_s$  have almost the same amplitude according to Fig. 17(a) and (b), which verifies the validity of the proposed method.

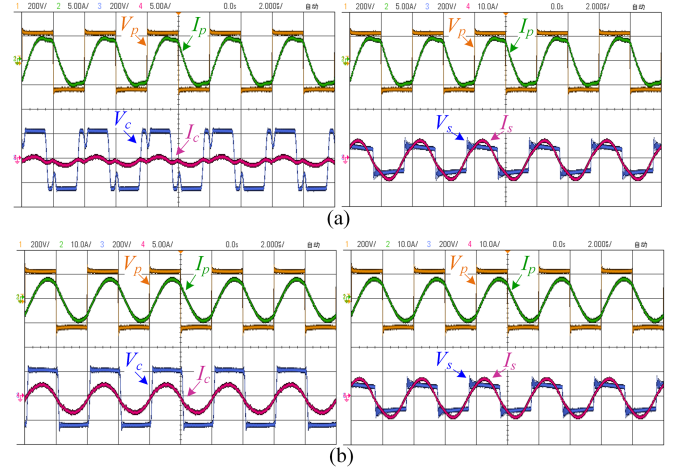


Fig. 17. Waveforms of the inverter output and the input of the rectifier at (a)  $k = 0.32$  and (b)  $k = 0.19$ .

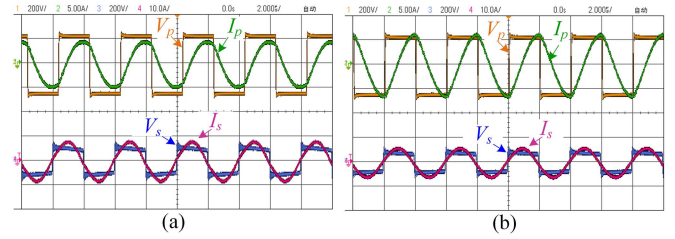


Fig. 18. Measured waveforms of the inverter output and the input of the rectifier for the IPT system without the clamping circuit at (a)  $k = 0.32$  and (b)  $k = 0.19$ .

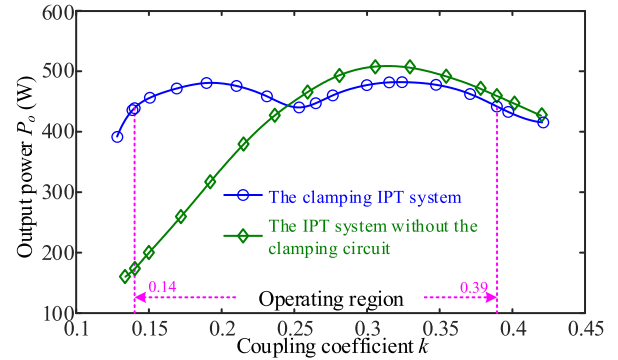


Fig. 19. Measured output power of the clamped IPT system and the IPT system without the clamping circuit.

To show the effectiveness of the proposed method, the clamp circuit is removed. The system can be regarded as the detuned S-S topology [7]. Fig. 18 shows the waveforms of the system without the clamping circuit when the coupling is 0.32 and 0.19. We can see that the output voltage  $V_s$  and current  $I_s$  are significantly reduced with the decrease of the coupling. The output power is measured in Fig. 19. According to the measured results, the power is slightly lower than the IPT system without the clamping circuit when the clamping IPT system works in turned-OFF or partly activated mode, namely the coupling decreases from 0.39 to 0.25. The main reason is the insufficient

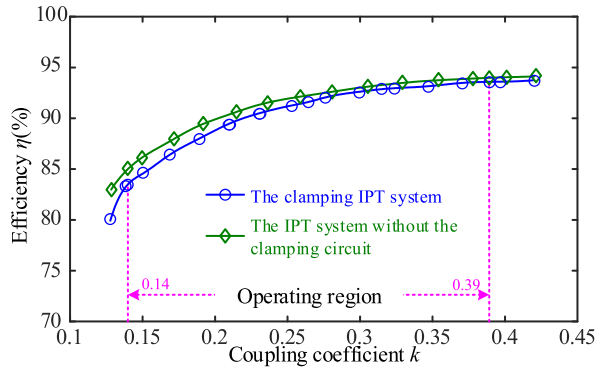


Fig. 20. Measured efficiency of the clamped IPT system and the IPT system without the clamping circuit.

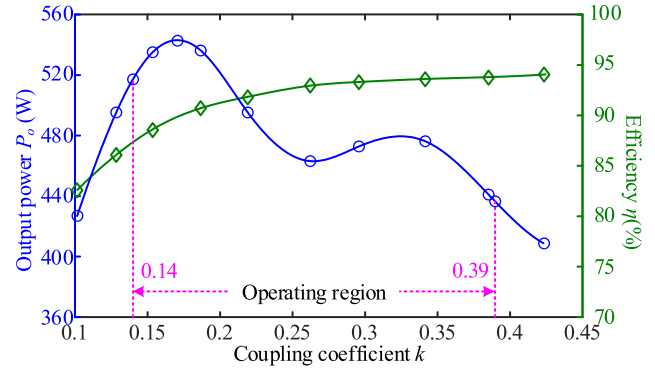


Fig. 22. Measured output power and efficiency with xy-misalignment.

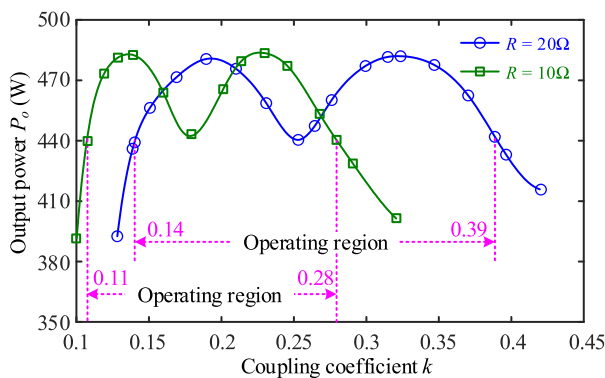


Fig. 21. Output power with different loads.

accuracy of the fundamental approximation method in the partly activated mode of the clamp circuit [26]. With further reduction of the coupling, the power of the IPT system without the clamp circuit declines significantly, while the proposed method output power still is stable. In terms of the overall power variation, the output power of the IPT system without the clamping circuit is between 210 and 505 W when coupling varies from 0.14 to 0.39, and the power fluctuation is 41.26%, which is inferior to the proposed method (4.3%). Moreover, the system efficiency is measured in Fig. 20. Similarly, the efficiency varies from 85.12% to 94.14%, with the coupling increasing from 0.14 to 0.39. Due to the power loss in the clamp circuit, the efficiency of the IPT system without the clamping circuit is slightly higher than that of the proposed method.

When the load is changed,  $P_{\max}$  and  $P_{\min}$  are constant with the load variation based on (10), (13), (27), and (30), while  $k_{c1}$ ,  $k_{c2}$ ,  $k_{c3}$ ,  $k_{pmax1}$ ,  $k_{pmax2}$ ,  $k_{min1}$ ,  $k_{max1}$ ,  $k_{min2}$ , and  $k_{max2}$  are changed concurrently in the same proportion according to (9), (14), (16), (19), (23), (27), and (30). Fig. 21 shows the output power with the different loads. It can be seen the output power moves to the left when the load decreases from 20 to 10  $\Omega$ . Besides, the load variation hardly affects the maximum and minimum output power, but the coupling range with stable power transfer is varied. Hence, the load is better fixed if the system is required to operate within the determined coupling range.

When the secondary side has a xy-misalignment, the results are measured in Fig. 22. With the coupling decrease, the output power deviates from the expected value (480 W) when the coupling is lower than 0.23. The maximum output power reaches 540 W, and the power fluctuation is larger than 10% due to the cross-couplings ( $M_{s-cp}$  and  $M_{s-cc}$ ). It is noted that the stand-alone inductor has almost identical electrical performance as the integrated inductor [31]. Hence, a tightly coupled transformer can also be used to form the clamp transformer to avoid the effects of cross-coupling by compromising the hardware volume in theory [33].

## V. CONCLUSION

A detuned SS-compensated IPT system with a clamped circuit is proposed to improve misalignment tolerance versus the wide coupling variation. Wireless feedback communication or closed-loop control is not required for the proposed method. The operating principle and misalignment characteristics are analyzed in detail. And then, circuit parameters are optimized to obtain high-misalignment tolerance. With the proposed parameter design method, an IPT system was built. Experimental results show that the power fluctuation is only 4.4%, and the maximum efficiency can reach 93.55% with 278.6% coupling variation (0.14–0.39), verifying the feasibility of the proposed method.

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