

# An Improved MPC With Reduced CMV and Current Distortion for PMSM Drives Under Variable DC-Bus Voltage Condition in Electric Vehicles

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**Abstract**—The conventional reduced-common-mode-voltage model predictive control (RCMV-MPC) faces the challenges of low control accuracy and high switching frequency at low speeds. To reduce CMV, improve steady-state performance and lower switching frequency, an improved MPC is proposed for permanent magnet synchronous motor (PMSM) drives with variable dc-bus voltage in electric vehicles (EVs). First, the virtual vectors with low CMV and switching frequency are defined, the optimal virtual vector and its duty cycle are determined. Then, the limitation of designed virtual vectors with fixed dc-bus voltage is illustrated. Furthermore, based on the analysis of the effect of dc-bus voltage on current distortion, the optimal reference dc-bus voltage is adopted to minimize the current distortion. At last, the dc-bus voltage is adjusted to track the reference value by dc-dc converter. An experimental comparison of the conventional methods and the proposed scheme is carried out. The results have verified that the proposed scheme can reduce CMV, current harmonics and switching frequency, especially in low-speed regions. As dc-dc converter has become more popular in motor drives of EVs, the proposed scheme could have a promising application perspective.

**Index Terms**—Common-mode voltage (CMV), current distortion, model predicted control (MPC), permanent magnet synchronous motors (PMSMs).

## I. INTRODUCTION

**D**UE to several salient advantages, such as small size, light weight and high power density, permanent magnet synchronous motors (PMSMs) have been widely employed in motor drive systems [1], [2]. With the rapid development of modern control theory and digital controllers, great attention has been attracted to model predictive control (MPC) for decades because of its fast dynamic response, simple control structure and ease

of handling nonlinear constraints [3], [4], [5]. According to different control variables, the finite-control-set MPC (FCS-MPC) methods applied to PMSMs are mainly composed of model predictive current control (MPCC) [6] and model predictive torque control [7]. Among them, MPCC is easier to implement in practical applications without weighting factor adjustments because the control variables are both currents [8].

The FCS-MPC is simple and intuitive to implement for constrained nonlinear systems and can consider the discrete nature of the power converter. In [6], eight discrete voltage vectors are acted on the inverter to realize MPCC. However, the current and torque ripples are relatively large for only single vector acts during one sampling interval. Therefore, the MPC with duty cycle control is proposed to improve the steady-state performance [9]. To reduce the current harmonics further, multi-vector MPC methods are proposed in [10], [11]. However, the computational burden increases significantly as the number of vector combinations increases. To release the computational burden, deadbeat MPC (DB-MPC) methods are proposed in [12], [13]. Thereby, better steady-state performance and lower computational burden are obtained.

Regardless of which MPC method is employed, the vectors that generate large common-mode voltage (CMV) will be used inevitably. The CMV in PMSMs drives is known to destroy winding insulations and generate common-mode current, which will cause severe electromagnetic interference (EMI) and undesired damage to motor bearings [14], [15]. To decrease the effects of CMV and improve system reliability, a lot of works have been reported to suppress the CMV of voltage source inverters (VSIs).

In the MPC methods for multilevel and multiphase VSIs, the virtual vectors constructed by the vectors with small CMV are usually defined as the candidates to reduce the CMV [16], [17]. Besides, additional CMV items are included in the cost function to penalize unexpected vectors with large CMV in multiphase VSIs [18], [19]. In the system consisting of a three-phase two-level inverter and PMSM, the zero vectors with large CMV are usually discarded to achieve CMV suppression. In [20], three adjacent nonzero vectors and one nonadjacent vector are utilized to evaluate the cost function during each sampling interval. However, the CMV reduction causes the increase of current distortion for the deprecation of zero vectors. In [21], the zero vectors are replaced by two opposite nonzero vectors to improve the

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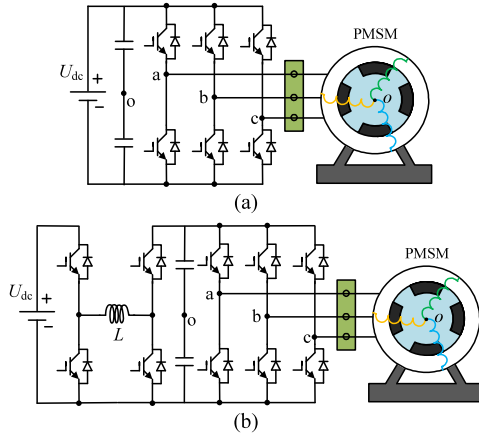


Fig. 1. Circuit topology of PMSM drive system. (a) Classic topology of three-phase VSI with PMSM. (b) Cascade topology formed by buck-boost converter and VSI with PMSM.

control accuracy. Furthermore, the vectors preselection strategy based on the current sector is proposed to eliminate CMV spikes caused by the dead-time effect. Nevertheless, the steady-state performance is still not satisfactory. To improve the steady-state performance further, a reduced-common-mode-voltage MPC (RCMV-MPC) is proposed in [22]. By adopting two nonzero vectors in each sampling interval, the synthesized vectors are closer to the reference vector. Thereby, the control precision is improved effectively. However, more opposite and nonadjacent vectors are used in the low-speed region, which increases the switching frequency and generates additional heat loss [22]. According to the above analysis, these CMV reduction schemes inevitably deteriorate the steady-state performance and increase the switching frequency.

Nowadays, PMSMs have achieved a lot of applications and development in the field of electric vehicles (EVs). With regard to the propulsion system in EVs, the following two basic configurations are used: the battery is connected to the dc input of VSI directly and a boost converter is placed between the battery and VSI. As shown in Fig. 1(a), the battery with constant voltage is connected directly to the dc-bus of the VSI in the classic topology of motor drives. Thanks to its single-stage conversion, the architecture in Fig. 1(a) is cheap, easy to manufacture and requires simple control, thereby this classic topology is widely used in EVs over the past decades [23]. At present, the drive system with higher supply voltage has become more popular due to its superior efficiency [24], [25]. Employing a boost converter followed by a dc-ac stage enables to enhance the dc-bus voltage of VSI, which can reduce the cost and size of the battery, and allow extensions of the speed range without field weakening [28]. In [26], [27], the applications of bidirectional buck-boost converter in EVs are further studied for its wider output voltage range, the cascade topology is shown in Fig. 1(b). By adopting the cascaded topology shown in Fig. 1(b), the dc-bus voltage can be adjusted by the dc-dc converter to adapt to more conditions. In this article, the possibilities to reduce CMV and current harmonics by using the topology shown in Fig. 1(b) are explored.

TABLE I  
EIGHT VOLTAGE VECTORS AND THEIR CMV

vectors	$S_a S_b S_c$	CMV	vectors	$S_a S_b S_c$	CMV
$u_0$	000	$-U_{dc}/2$	$u_4$	011	$U_{dc}/6$
$u_1$	100	$-U_{dc}/6$	$u_5$	001	$-U_{dc}/6$
$u_2$	110	$U_{dc}/6$	$u_6$	101	$U_{dc}/6$
$u_3$	010	$-U_{dc}/6$	$u_7$	111	$U_{dc}/2$

To suppress the CMV, improve the control accuracy and reduce the switching frequency, an improved MPC method for PMSM drives with variable dc-bus voltage is proposed in this article. First, the virtual vectors with lower CMV and switching frequency are defined, the optimal virtual vector is selected and its duty cycle is calculated. Then, the limitation of the fixed dc-bus voltage is analyzed. Furthermore, the effects of the dc-bus voltage on current distortion are investigated, and the optimal reference dc-bus voltage is determined to minimize the current harmonics. Finally, the dc-dc converter is adopted to track the reference voltage. The main contributions of this article are summarized as follows.

- 1) By defining the virtual vectors with low CMV and switching frequency, the proposed method can reduce the CMV from  $\pm U_{dc}/2$  to  $\pm U_{dc}/6$  compared with DB-MPC in [12], and lower the switching frequency effectively compared with RCMV-MPC in [22].
- 2) By presenting the missing distribution of defined virtual vectors, the poor control accuracy at low speeds with fixed dc-bus voltage is illustrated. To overcome this limitation, the variability of dc-bus voltage is utilized fully in the proposed method to adjust the coverage of virtual vectors, thereby the control precision is improved significantly.
- 3) By establishing the model of peak-to-peak values of stator flux error, the effect of the dc-bus voltage on current distortion is analyzed in detail, and the optimal reference dc-bus voltage is determined to minimize the current distortion. Thereby, the steady-state performance is improved significantly compared with RCMV-MPC, and similar excellent compared with DB-MPC.

The rest of this article is structured as follows. Section II illustrates the model of the PMSM and conventional RCMV-MPC. The proposed method is described in Section III. Experimental results and conclusion are presented in Sections IV and V.

## II. SYSTEM MODELING AND CONVENTIONAL RCMV-MPC

### A. System Mathematical Model

The CMV in three-phase VSI can be expressed as [21]

$$u_{CM} = \frac{U_{dc}}{3}(S_a + S_b + S_c) - \frac{U_{dc}}{2} \quad (1)$$

where  $U_{dc}$  denotes the dc-bus voltage of VSI;  $S_a$ ,  $S_b$ , and  $S_c$  represent the switching signals of three bridge arms. There are eight voltage vectors in three-phase VSI, and the CMV values of all vectors are given in Table I.

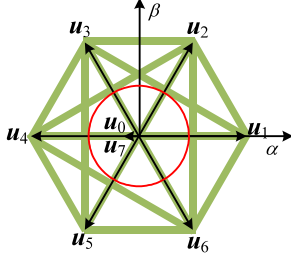


Fig. 2. Virtual vectors distribution in RCMV-MPC.

The mathematical model of PMSM in the  $dq$ -frame can be expressed as [6]

$$\begin{cases} \frac{di_d}{dt} = \frac{1}{L_d}(-Ri_d + u_d + L_q\omega_e i_q) \\ \frac{di_q}{dt} = \frac{1}{L_q}(-Ri_q + u_q - L_d\omega_e i_d - \omega_e\psi_f) \end{cases} \quad (2)$$

$$T_e = \frac{3}{2}n_p i_q [\psi_f + (L_d - L_q)i_d] \quad (3)$$

where  $u_d$ ,  $u_q$ , and  $i_d$ ,  $i_q$  represent  $dq$ -axis output voltages and currents;  $\omega_e$  denotes rotor electrical angular velocity;  $\psi_f$  is permanent magnet flux linkage;  $L_d$ ,  $L_q$ , and  $R$  represent the  $dq$ -axis stator inductances and winding resistance respectively;  $T_e$  is electromagnetic torque and  $n_p$  denotes the number of poles pairs.

The forward Euler method is utilized to discretize (2), then the current prediction model can be expressed as

$$\begin{cases} i_d^{k+1} = i_d^k + \frac{T_s}{L_d}(u_d^k - Ri_d^k + \omega_e L_q i_q^k) \\ i_q^{k+1} = i_q^k + \frac{T_s}{L_q}(u_q^k - Ri_q^k - \omega_e L_d i_d^k - \omega_e\psi_f) \end{cases} \quad (4)$$

where  $T_s$  is the sampling interval, the superscripts  $k$  and  $k+1$  represent  $k$ th and  $(k+1)$ th sampling instants.

### B. Analysis of Conventional RCMV-MPC

To suppress the CMV amplitude, an RCMV-MPC method is reported in [22]. The specific steps are as follows: First, the initial vector is obtained from six nonzero vectors by cost function minimization. Second, six nonzero vectors are selected as second candidate vectors, and the duty cycles of all virtual vectors composed of initial vector and second candidate vectors are calculated respectively. Finally, the virtual vector that minimizes the cost function is selected as the best virtual vector to generate switching pulses.

Fig. 2 presents the distribution of virtual vectors consisting of two non-zero vectors in RCMV-MPC. As shown in Fig. 2, the endpoints of the virtual vectors are distributed on the connecting line of every two nonzero vectors, that is, the green shaded area. Obviously, the distribution of virtual vectors is discontinuous, which may result in the loss of control accuracy. In addition, the candidate virtual vectors within the red circle are all composed of vectors in opposite directions, the higher switching frequency will be inevitable. Therefore, RCMV-MPC has the disadvantages of insufficient steady-state control accuracy and higher switching frequency at low speeds.

TABLE II  
SWITCHING PULSE SEQUENCES OF SIX VIRTUAL VOLTAGE VECTORS

Initial vector	Optimal virtual vector	Pulse sequence of $\mathbf{u}_{vi}$
$\mathbf{u}_1$	$\mathbf{u}_{v1}$	$\mathbf{u}_6-\mathbf{u}_1-\mathbf{u}_2-\mathbf{u}_1-\mathbf{u}_6$
$\mathbf{u}_2$	$\mathbf{u}_{v2}$	$\mathbf{u}_1-\mathbf{u}_2-\mathbf{u}_3-\mathbf{u}_2-\mathbf{u}_1$
$\mathbf{u}_3$	$\mathbf{u}_{v3}$	$\mathbf{u}_2-\mathbf{u}_3-\mathbf{u}_4-\mathbf{u}_3-\mathbf{u}_2$
$\mathbf{u}_4$	$\mathbf{u}_{v4}$	$\mathbf{u}_3-\mathbf{u}_4-\mathbf{u}_5-\mathbf{u}_4-\mathbf{u}_3$
$\mathbf{u}_5$	$\mathbf{u}_{v5}$	$\mathbf{u}_4-\mathbf{u}_5-\mathbf{u}_6-\mathbf{u}_5-\mathbf{u}_4$
$\mathbf{u}_6$	$\mathbf{u}_{v6}$	$\mathbf{u}_5-\mathbf{u}_6-\mathbf{u}_1-\mathbf{u}_6-\mathbf{u}_5$

### III. PROPOSED METHOD

Aiming at the aforementioned issues of RCMV-MPC, an improved MPC method with variable dc-bus voltage is proposed in this article. The principle and implementation of the proposed scheme are illustrated in this section.

#### A. Virtual Vector Selection and Duty Cycle Determination

To compensate for the one-step delay in MPC, the current values at  $(k+1)$ th sampling instant in (4) are usually regarded as the initial values for the next prediction. Then, the current values at  $(k+2)$ th sampling instant can be expressed as

$$\begin{cases} i_d^{k+2} = i_d^{k+1} + \frac{T_s}{L_d}[u_d^{k+1} - Ri_d^{k+1} + \omega_e L_q i_q^{k+1}] \\ i_q^{k+2} = i_q^{k+1} + \frac{T_s}{L_q}[u_q^{k+1} - Ri_q^{k+1} - \omega_e L_d i_d^{k+1} - \omega_e\psi_f] \end{cases} \quad (5)$$

where superscripts  $k+2$  represents the  $(k+2)$ th sampling instant;  $u_d^{k+1}$  and  $u_q^{k+1}$  denote the  $dq$ -axis components of nonzero vectors  $\mathbf{u}_i$  ( $i = 1-6$ ). Furthermore, the cost function is

$$G = (i_d^* - i_d^{k+2})^2 + (i_q^* - i_q^{k+2})^2 \quad (6)$$

where  $i_d^*$  and  $i_q^*$  denote the  $dq$ -axis components of reference current values. The initial vector  $\mathbf{u}_{opt}$  can be selected by the cost function minimization.

As given in Table I, zero vectors  $\mathbf{u}_0$  and  $\mathbf{u}_7$  have the largest CMV,  $-U_{dc}/2$  and  $U_{dc}/2$ , respectively. To suppress the CMV, the zero vectors are discarded in this article. All the virtual vectors designed in the proposed method are named  $\mathbf{u}_{v1}-\mathbf{u}_{v6}$ , which are composed of three adjacent nonzero vectors. When the  $\mathbf{u}_i$  is selected as the initial vector, the  $\mathbf{u}_{vi}$  ( $i = 1-6$ ) will be chosen as the optimal virtual vector. The pulse sequences of all virtual vectors are given in Table II.

As given in Table II, the optimal virtual vector  $\mathbf{u}_{vi}$  is composed of  $\mathbf{u}_i$  and two adjacent vectors  $\mathbf{u}_x$  and  $\mathbf{u}_y$ . When the  $\mathbf{u}_{vi}$  applied, the predicted current values at  $(k+2)$ th sampling instant can be obtained as

$$\begin{cases} i_d^{k+2} = i_d^{k+1} + s_{di}t_i + s_{dx}t_x + s_{dy}t_y \\ i_q^{k+2} = i_q^{k+1} + s_{di}t_i + s_{qx}t_x + s_{qy}t_y \\ T_s = t_i + t_x + t_y \end{cases} \quad (7)$$

where  $t_i$ ,  $t_x$ , and  $t_y$  are the action times of  $\mathbf{u}_i$ ,  $\mathbf{u}_x$  and  $\mathbf{u}_y$ ;  $s_{di}$ ,  $s_{dx}$ ,  $s_{dy}$  and  $s_{qi}$ ,  $s_{qx}$ ,  $s_{qy}$  are the  $dq$ -axis current slopes of  $\mathbf{u}_i$ ,  $\mathbf{u}_x$ , and  $\mathbf{u}_y$ , their values can be obtained according to (2). Assuming the predicted currents shown in (7) are equal to the  $i_d^*$  and  $i_q^*$ , then the durations of  $\mathbf{u}_i$ ,  $\mathbf{u}_x$ , and  $\mathbf{u}_y$  can be obtained.

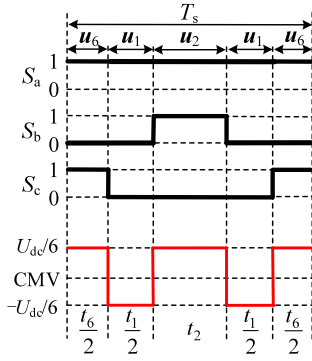


Fig. 3. Switching pulses and CMV of  $u_{v1}$ .

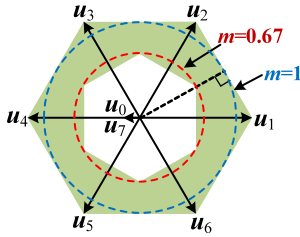


Fig. 4. Distribution of designed virtual vectors with fixed dc-bus voltage.

Taking  $u_{v1}$  as an example, its switching pulses and CMV are shown in Fig. 3, where  $t_6$ ,  $t_1$ , and  $t_2$  are the durations of  $u_6$ ,  $u_1$ , and  $u_2$ , respectively. In Fig. 3, the CMV is limited  $-U_{dc}/6$  to  $U_{dc}/6$ , and only two-phase arms turn ON and turn OFF during one sampling interval. Therefore, the defined virtual vectors have a lower CMV and switching frequency.

### B. Limitations of Fixed DC-Bus Voltage

The derivative of the currents in steady-state can be ignored in (2), thereby the  $dq$ -axis components of reference voltage  $u_d^*$  and  $u_q^*$  can be obtained as

$$\begin{cases} u_d^* = R i_d^* - \omega_e L_q i_q^* \\ u_q^* = R i_q^* + \omega_e L_d i_d^* + \omega_e \psi_f \end{cases} \quad (8)$$

Then, the modulation index of the inverter is [28]

$$m = \frac{\sqrt{3} |u^*|}{U_{dc}} \quad (9)$$

where  $|u^*|$  is the magnitude of reference vector  $u^*$ , its value is

$$|u^*| = \sqrt{u_d^{*2} + u_q^{*2}}. \quad (10)$$

As shown in Fig. 1(a), the dc-bus voltage in the classic topology is constant. Fig. 4 presents the distribution of designed virtual vectors with fixed dc voltage. In Fig. 4, the modulation index at the blue circle and red circle are 1 and 0.67, respectively [28]. The green area is the coverage of virtual vectors and all virtual vectors in green area are continuous. However, the control accuracy may be not satisfactory when  $m < 0.67$  because the virtual vectors are discrete or even missing within the red circle.

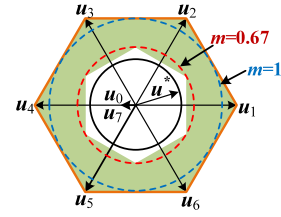


Fig. 5. Diagrams of hexagon and circles.

Therefore, the designed virtual vectors are not applicable under the fixed dc-bus voltage.

In addition, the freedom of dc-bus voltage is not utilized fully in Fig. 1(a). For example, the length of  $u^*$  will be short and a higher dc voltage is not necessary when the motor is running at low speed. Similarly, the length of  $u^*$  is so long that the supply voltage is not enough when the motor is running at high speed. By adopting the cascaded structure shown in Fig. 1(b), the dc-bus voltage can be adjusted to meet the requirements of more operating conditions, such as running at higher speed conditions without field weakening. The main purpose of this article is to use the adjustability of dc-bus voltage to reduce CMV and current distortion simultaneously.

### C. Optimal Reference DC-Bus Voltage Calculation

As shown in Fig. 5, the endpoints of  $u_i$  ( $i = 1-6$ ) constitute an orange hexagon. Since the length of  $u_i$  is  $2U_{dc}/3$ , the hexagon will shrink and expand with the change of dc-bus voltage. Assuming  $u^*$  is constant, the endpoint of  $u^*$  will form a black circle as the motor rotates. Change the hexagon by adjusting the dc-bus voltage, so that the black circle will fall in the green area. Consequently, the error between virtual vectors and the reference vector will be effectively reduced. In other words, the control precision can be improved when  $0.67 \leq m \leq 1$ .

According to (9), the reference dc-bus voltage of VSI can be obtained as

$$U_{dcref} = \frac{\sqrt{3} |u^*|}{m}. \quad (11)$$

However, the optional range of  $U_{dcref}$  is relatively large when  $0.67 \leq m \leq 1$  according to (11). The durations of applied voltages are different with diverse  $U_{dcref}$ , which will lead to different current distortion. Therefore, the effect of dc-bus voltage on current distortion needs to be investigated, and the optimal  $U_{dcref}$  should be determined to minimize the current harmonics.

As given in Table II, the optimal virtual vector is applied in each sampling interval. During each sampling interval, the voltage errors must be generated when the instantaneous voltages are different from the constant reference voltage, which will cause distortion of the line current. Take the virtual vector  $u_{v2}$  as an example, the instantaneous error voltages of  $u_{v2}$  can be expressed as

$$\begin{cases} u_{err1} = u_1 - u^* \\ u_{err2} = u_2 - u^* \\ u_{err3} = u_3 - u^* \end{cases} \quad (12)$$

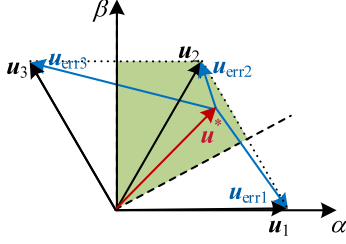
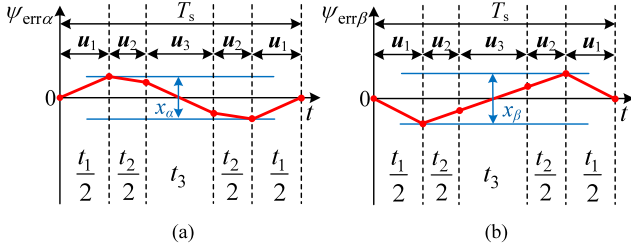
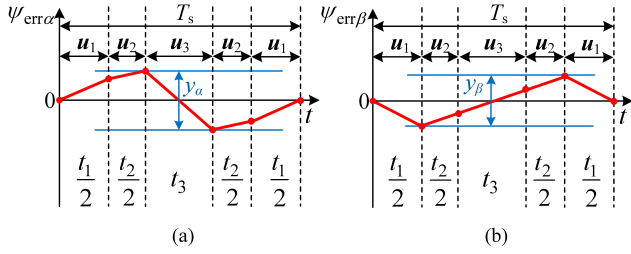


Fig. 6. Distribution of error voltage vectors.


 Fig. 7. Variation of stator flux error of  $\mathbf{u}_{v2}$  when  $u_{err2\alpha} \leq 0$ . (a)  $\alpha$ -axis. (b)  $\beta$ -axis.

 Fig. 8. Variation of stator flux error of  $\mathbf{u}_{v2}$  when  $u_{err2\alpha} \leq 0$ . (a)  $\alpha$ -axis. (b)  $\beta$ -axis.

where  $\mathbf{u}_{err1}$ ,  $\mathbf{u}_{err2}$ , and  $\mathbf{u}_{err3}$  represent the error voltage vectors corresponding to  $\mathbf{u}_1$ ,  $\mathbf{u}_2$ , and  $\mathbf{u}_3$ . Fig. 6 presents the distribution of the error voltage vectors. According to Table II, the initial vector is  $\mathbf{u}_2$  and the  $\mathbf{u}^*$  is located in the green area when the  $\mathbf{u}_{v2}$  is taken as an example [29], as shown in Fig. 6.

Since the length of  $\mathbf{u}_i$  ( $i=1-6$ ) is  $2U_{dc}/3$ , the  $\alpha\beta$ -components of the error voltage vectors can be expressed as (13) according to Fig. 6, where  $u_\alpha^*$  and  $u_\beta^*$  are the  $\alpha\beta$ -axis components of  $\mathbf{u}^*$ .

$$\begin{cases} u_{err1\alpha} = \frac{2U_{dc}}{3} - |u_\alpha^*| \\ u_{err1\beta} = -|u_\beta^*| \\ u_{err2\alpha} = \frac{U_{dc}}{3} - |u_\alpha^*| \\ u_{err2\beta} = \frac{\sqrt{3}U_{dc}}{3} - |u_\beta^*| \\ u_{err3\alpha} = -\frac{U_{dc}}{3} - |u_\alpha^*| \\ u_{err3\beta} = \frac{\sqrt{3}U_{dc}}{3} - |u_\beta^*| \end{cases} \quad (13)$$

According to Fig. 6 and (13), it can be determined whether the other  $\alpha\beta$ -components of  $\mathbf{u}_{err1}$ ,  $\mathbf{u}_{err2}$ , and  $\mathbf{u}_{err3}$  are positive

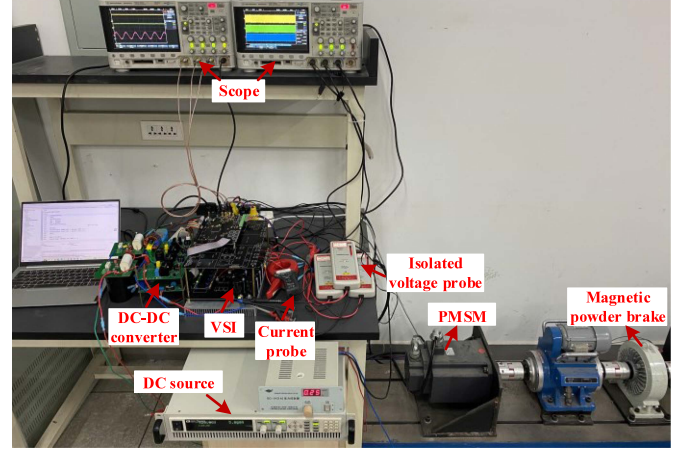


Fig. 9. Photo of experimental platform.

 TABLE III  
 POSITIVE AND NEGATIVE OF COMPONENTS OF ERROR VOLTAGES

$\alpha$ -axis error voltages	Values	$\beta$ -axis error voltages	Values
$u_{err1\alpha}$	positive	$u_{err1\beta}$	negative
$u_{err2\alpha}$	positive or negative	$u_{err2\beta}$	positive
$u_{err3\alpha}$	negative	$u_{err3\beta}$	positive

or negative, except for  $u_{err2\alpha}$ . The positive and negative of  $\alpha\beta$ -components of  $\mathbf{u}_{err1}$ ,  $\mathbf{u}_{err2}$  and  $\mathbf{u}_{err3}$  are given in Table III.

The time integral of the error voltage vector is termed as stator flux error vector [30]. When it satisfies  $u_{err2\alpha} \leq 0$ , the variation of stator flux error of  $\mathbf{u}_{v2}$  within a sampling period is shown in Fig. 7, where  $\psi_{err\alpha}$  and  $\psi_{err\beta}$  denote the  $\alpha\beta$ -axis components of stator flux error vector,  $x_\alpha$  and  $x_\beta$  are the peak-to-peak values of  $\psi_{err\alpha}$  and  $\psi_{err\beta}$ .

The  $t_1$ ,  $t_2$ , and  $t_3$  shown in Fig. 7 are the durations of  $\mathbf{u}_1$ ,  $\mathbf{u}_2$ , and  $\mathbf{u}_3$ . By establishing the volt-second balance, the  $t_1$ ,  $t_2$  and  $t_3$  can be expressed as

$$\begin{cases} t_1 = \frac{U_{dc} - \sqrt{3}u_\beta^*}{U_{dc}} T_s \\ t_2 = \frac{-U_{dc} + 1.5u_\alpha^* + 1.5\sqrt{3}u_\beta^*}{U_{dc}} T_s \\ t_3 = \frac{U_{dc} - 1.5u_\alpha^* - 0.5\sqrt{3}u_\beta^*}{U_{dc}} T_s \end{cases} \quad (14)$$

It can be known from Fig. 7 that the vector sequence and waveforms of  $\psi_{err\alpha}$  and  $\psi_{err\beta}$  are symmetrical. Therefore, the  $\alpha$ -axis stator flux error of  $\mathbf{u}_{v2}$  within a half sampling period can be expressed as

$$\begin{aligned} \psi_{err\alpha} &= \begin{cases} u_{err1\alpha}t & 0 \leq t \leq 0.5t_1 \\ 0.5u_{err1\alpha}t_1 + u_{err2\alpha}t & 0 \leq t \leq 0.5t_2 \\ 0.5u_{err1\alpha}t_1 + 0.5u_{err2\alpha}t_2 + u_{err3\alpha}t & 0 \leq t \leq 0.5t_3 \end{cases} \end{aligned} \quad (15)$$

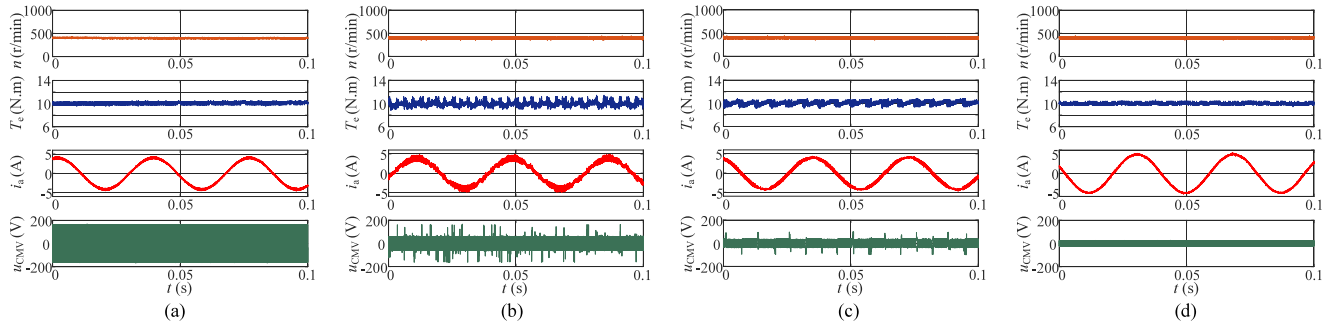


Fig. 10. Steady-state experimental waveforms of four control methods at 400 r/min (from top to bottom, waveforms are rotor speed, electromagnetic torque, a-phase current and CMV). (a) Deadbeat MPC. (b) RCMV-MPC. (c) Proposed method with  $m = 0.67$ . (d) Proposed method with  $m = 1$ .

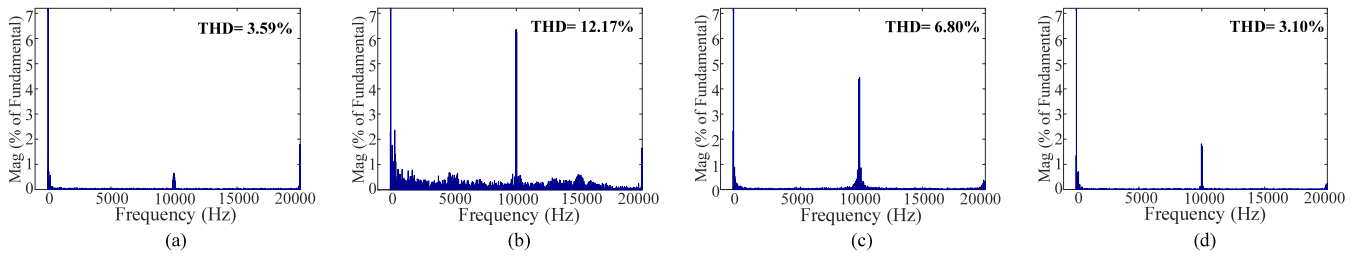


Fig. 11. THD values of  $i_a$  in four control methods at 400 r/min. (a) Deadbeat MPC. (b) Reduced-common-mode-voltage MPC. (c) Proposed method with  $m = 0.67$ . (d) Proposed method with  $m = 1$ .

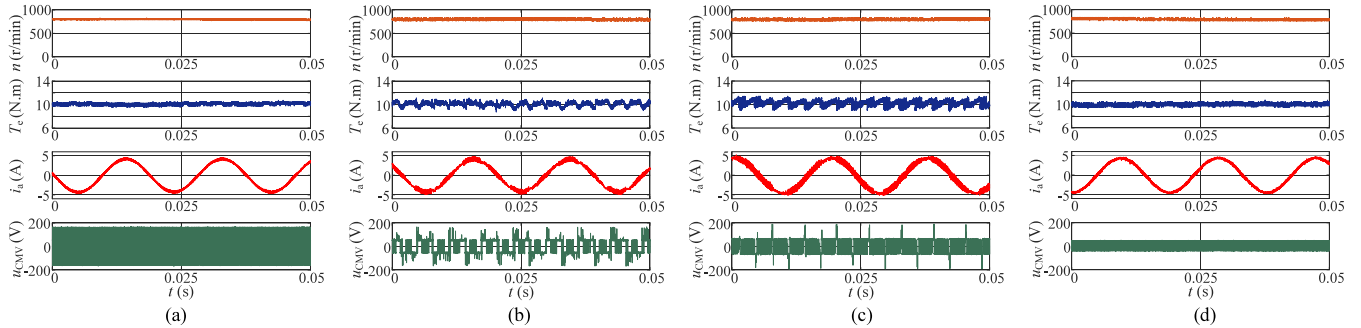


Fig. 12. Steady-state experimental waveforms of four control methods at 800 r/min (from top to bottom, waveforms are rotor speed, electromagnetic torque, a-phase current and CMV). (a) Deadbeat MPC. (b) Reduced-common-mode-voltage MPC. (c) Proposed method with  $m = 0.67$ . (d) Proposed method with  $m = 1$ .

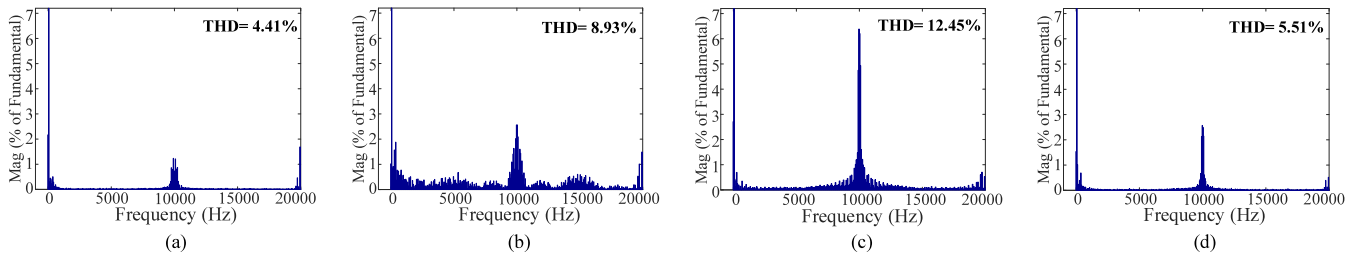


Fig. 13. THD values of  $i_a$  in four control methods at 800 r/min. (a) Deadbeat MPC. (b) Reduced-common-mode-voltage MPC. (c) Proposed method with  $m = 0.67$ . (d) Proposed method with  $m = 1$ .

Similarly, the  $\beta$ -axis stator flux error of  $\mathbf{u}_{v2}$  within a half sampling period can be expressed as

$$\psi_{\text{err}\beta} = \begin{cases} u_{\text{err}1\beta}t & 0 \leq t \leq 0.5t_1 \\ 0.5u_{\text{err}1\beta}t_1 + u_{\text{err}2\beta}t & 0 \leq t \leq 0.5t_2 \\ 0.5u_{\text{err}1\beta}t_1 + 0.5u_{\text{err}2\beta}t_2 + u_{\text{err}3\beta}t & 0 \leq t \leq 0.5t_3 \end{cases} \quad (16)$$

In this article, the peak-to-peak values of  $\psi_{\text{err}\alpha}$  and  $\psi_{\text{err}\beta}$  are utilized to evaluate current distortion. To obtain minimum current distortion, the peak-to-peak values should be minimum. As shown in Fig. 7, the peak-to-peak values of  $\psi_{\text{err}\alpha}$  and  $\psi_{\text{err}\beta}$  when  $u_{\text{err}2\alpha} \leq 0$  can be expressed as

$$\begin{cases} x_\alpha = u_{\text{err}1\alpha}t_1 \\ x_\beta = u_{\text{err}2\beta}(t_2 + t_3) \end{cases} \quad (17)$$

To analyze the relationship between peak-to-peak values  $x_\alpha$ ,  $x_\beta$  and dc-bus voltage, the derivative of (17) is obtained as

$$\begin{cases} \frac{\partial x_\alpha}{\partial U_{\text{dc}}} = \frac{\sqrt{3}(2U_{\text{dc}} - |u_\alpha^*|)(\frac{\sqrt{3}U_{\text{dc}}}{3} - |u_\beta^*|)}{U_{\text{dc}}^2} \geq 0 \\ \frac{\partial x_\beta}{\partial U_{\text{dc}}} = \frac{\sqrt{3}|u_\beta^*|^2 T_s}{U_{\text{dc}}^2} \geq 0 \end{cases} \quad (18)$$

Therefore,  $x_\alpha$  and  $x_\beta$  are the increasing functions of  $U_{\text{dc}}$ , which means that if  $U_{\text{dc}}$  is smaller, the values of  $x_\alpha$  and  $x_\beta$  are smaller.

When it satisfies  $u_{\text{err}2\alpha} \leq 0$ , the variation of stator flux error of  $\mathbf{u}_{v2}$  within a sampling period is shown in Fig. 8, where  $y_\alpha$  and  $y_\beta$  are the peak-to-peak values of  $\psi_{\text{err}\alpha}$  and  $\psi_{\text{err}\beta}$ .

As shown in Fig 8, the peak-to-peak values of  $\psi_{\text{err}\alpha}$  and  $\psi_{\text{err}\beta}$  when  $u_{\text{err}2\alpha} \leq 0$  can be expressed as

$$\begin{cases} y_\alpha = u_{\text{err}1\alpha}t_1 + u_{\text{err}2\alpha}t_2 \\ y_\beta = x_\beta \end{cases} \quad (19)$$

To analyze the relationship between peak-to-peak values  $y_\alpha$ ,  $y_\beta$  and dc-bus voltage, the derivative of (19) is obtained as

$$\begin{cases} \frac{\partial y_\alpha}{\partial U_{\text{dc}}} = \frac{U_{\text{dc}}^2 + \frac{\sqrt{3}}{2}|u_\alpha^*||u_\beta^*| + \frac{3}{2}|u_\alpha^*|^2}{U_{\text{dc}}^2} \geq 0 \\ \frac{\partial y_\beta}{\partial U_{\text{dc}}} = \frac{\partial x_\beta}{\partial U_{\text{dc}}} \geq 0 \end{cases} \quad (20)$$

Therefore,  $y_\alpha$  and  $y_\beta$  are also the increasing functions of  $U_{\text{dc}}$ , which means that if  $U_{\text{dc}}$  is smaller, the values of  $y_\alpha$  and  $y_\beta$  are smaller as well. The above analysis shows that no matter whether  $u_{\text{err}2\alpha}$  is positive or negative, the peak-to-peak values of flux error and current distortion decrease with the decrease of  $U_{\text{dc}}$ . Similarly, the same conclusion can be obtained when the optimal virtual vector is a different one. To minimize the current distortion, the dc-bus voltage of VSI should be as small as possible. It can be known from (11) that if  $m$  is bigger when  $0.67 \leq m \leq 1$ , the reference dc-bus voltage  $U_{\text{dcref}}$  is smaller. To obtain the minimum possible  $U_{\text{dc}}$ , the value of  $m$  should be set to 1. Thereby, the optimal  $U_{\text{dcref}}$  is obtained as

$$U_{\text{dcref}} = \sqrt{3}|u^*|. \quad (21)$$

TABLE IV  
PARAMETERS OF EXPERIMENTAL PLATFORM

Parameter	Symbol	Value
Rated speed	$n$	1500 r/min
$d$ -axis inductance	$L_d$	6.24 mH
$q$ -axis inductance	$L_q$	6.24 mH
Stator resistance	$R$	0.71 $\Omega$
PM flux linkage	$\psi_f$	0.421 Wb
Pole pairs	$n_p$	4

To avoid the torque oscillation caused by insufficient dc-bus voltage in dynamic conditions, the reference dc-bus voltage with compensation is further modified as

$$U_{\text{dcref}} = \begin{cases} \sqrt{3}|u^*| & n^* - n \leq 50 \text{ r/min} \\ \frac{\sqrt{3}|u^*|}{0.9} & n^* - n > 50 \text{ r/min} \end{cases} \quad (22)$$

where  $n^*$  and  $n$  are reference rotor speed and real speed, respectively. As shown in (22), it satisfies  $m = 1$  when  $n^* - n \leq 50$  r/min and  $m = 0.9$  when  $n^* - n > 50$  r/min, which means  $U_{\text{dcref}}$  remains minimum in steady state and has a slight increase in the dynamic state.

Furthermore, the dc-bus voltage of inverter can be adjusted to track  $U_{\text{dcref}}$  by adopting dc-dc converters, which is widely used in the next-generation 800 V-level EVs. The control method of dc-dc converter is described in detail in [31], which will not be repeated in this article.

#### IV. EXPERIMENTAL RESULTS

Fig. 9 shows a scale-down experimental platform of three phase VSI with PMSM. In this platform, the control methods are programmed and implemented in TI DSP TMS320F28335.

The output voltage  $u_{ao}$ ,  $u_{bo}$ , and  $u_{co}$  shown in Fig. 1 are measured by isolated voltage probes, and the CMV is obtained by [20]

$$u_{\text{CMV}} = \frac{1}{3}(u_{ao} + u_{bo} + u_{co}). \quad (23)$$

The parameters of PMSM are given in Table IV. In this Section, the DB-MPC in [12], RCMV-MPC in [22] are compared, as well as the proposed methods with different  $m$  values, where different values of  $m$  lead to different reference dc-bus voltage. The fix dc-bus voltage of VSI in DB-MPC and RCMV-MPC is 320 V, which ensures that the PMSM runs in the speed range of 0 to 1000 r/min. The dc input voltage of the buck-boost converter adopted in proposed method are 200 V, and the dc-bus voltage of the VSI is adjusted according to (22). The sampling frequencies of studied methods are all 10 kHz.

##### A. Steady-State Performance Comparison

To compare the steady-state performance of different control methods, Fig. 10 presents the rotor speed, torque, a-phase current and CMV waveforms, Fig. 11 shows the fast Fourier transform (FFT) analysis of a-phase current  $i_a$ , where the load torque and the speed are 10 N.m and 400 r/min, respectively.

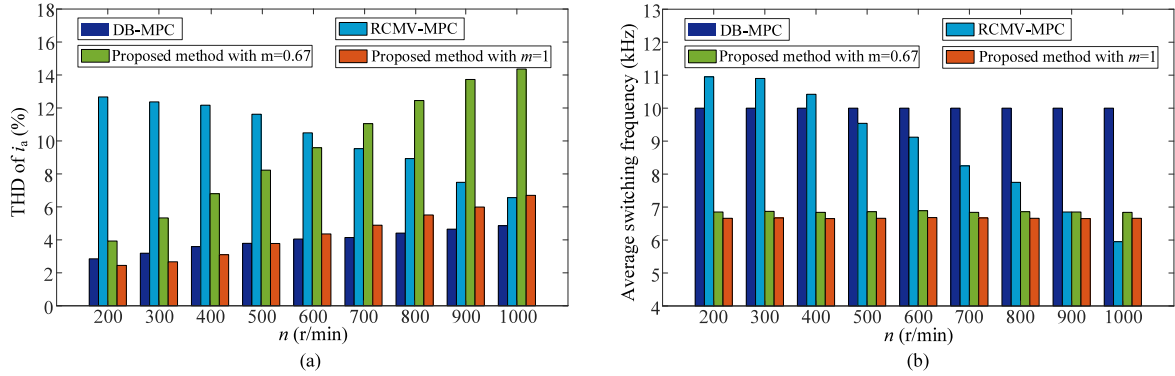


Fig. 14. Current THD and average switching frequency of four methods at different speeds. (a) THD values of  $i_a$ . (b) Average switching frequency.

As shown in Figs. 10 and 11, the DB-MPC has smaller torque ripple and current distortion than RCMV-MPC and the proposed method with  $m = 0.67$ , however, the CMV amplitude is  $\pm U_{dc}/2$  due to the utilization of zero vectors. The RCMV-MPC reduced the CMV amplitude to  $\pm U_{dc}/6$  effectively, although there are some CMV spikes, which is due to the effect of dead times in the real experimental setup [32], [32], and is not discussed in this article. Nevertheless, severe torque ripple and current distortion are inevitable in RCMV-MPC because the candidate vectors are discontinuous. On the contrary, the candidate vectors in the proposed method are continuous. Consequently, the steady-state performances are improved. Meanwhile, the CMV reduction is achieved simultaneously. As illustrated in Section III-C, the reference dc-bus voltages are different with diverse  $m$ , which will lead to different current distortion. As shown in Figs. 10 and 11, the proposed method with  $m = 1$  has lower current distortion than the proposed method with  $m = 0.67$ , which verifies the correctness of the theoretical analysis in Section III-C. In addition, by taking full advantage of the variability of dc-bus voltage, the proposed method with  $m = 1$  has similar excellent steady-state performance similar to DB-MPC.

Figs. 12 and 13 present the steady-state experimental waveforms and the FFT analysis of  $i_a$ , where the load torque and the speed are 10 N.m and 800 r/min, respectively. As shown in Figs. 12 and 13, the CMV reduction can be achieved both in RCMV-MPC and the proposed methods, yet the proposed method with  $m = 1$  has the lower current harmonics and torque ripple than RCMV-MPC.

To compare the steady-state performances at different speeds, Fig. 14(a) and (b) show the current THD and average switching frequencies of four methods, where the load torque is 10 N.m. The average switching frequency is defined as

$$f_{sw} = \frac{1}{3T_w} \sum_{k=a}^c N_k \quad (24)$$

where  $T_w$  is the time window for counting the ON-OFF times of IGBTs, and  $T_w$  is set to 1 s in this test.  $N_k$  is the ON-OFF times of leg  $k$  ( $k = a, b, c$ ).

As shown in Fig. 14(a), the current THD values of proposed method with  $m = 1$  are closed to DB-MPC, and much lower than

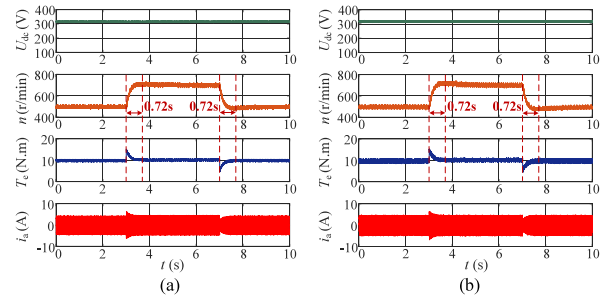


Fig. 15. Dynamic waveforms of two conventional methods when speed steps up and down (from top to bottom, waveforms are DC-bus voltage, rotor speed, electromagnetic torque, a-phase current). (a) Deadbeat MPC. (b) Reduced-common-mode-voltage MPC.

RCMV-MPC and proposed method with  $m = 0.67$ . As shown in Fig. 14(b), the average switching frequencies of proposed method with  $m = 1$  are closed to proposed method with  $m = 0.67$ , and lower than DB-MPC and RCMV-MPC, especially in the low-speed conditions.

## B. Dynamic Performance Comparison

As shown in Fig. 14, the current harmonics of the proposed method with  $m = 1$  is lower than the proposed method with  $m = 0.67$ , and their average switching frequencies are similar. Therefore, the proposed method with  $m = 1$  has better performance. To simplify the analysis, only the dynamic performances of DB-MPC, RCMV-MPC and the proposed method with  $m = 1$  have been compared in this article. Fig. 15 shows the dynamic waveforms of DB-MPC and RCMV-MPC when the speed steps up from 500 to 700 r/min at 3 s and steps down from 700 to 500 r/min at 7 s, where the load torque is 10 N.m. Figs. 16 and 17 show the dynamic waveforms of the proposed method with  $m = 1$ . It should be noticed that the reference dc-bus voltage in Fig. 16 is obtained by (21) and without any additional compensation. On the contrary, the reference dc-bus voltage in Fig. 17 is obtained by (22) and with compensation.

As shown in Figs. 15–17, the dc-bus voltage of DB-MPC and RCMV-MPC are constant, while the dc-bus voltage of the proposed method with  $m = 1$  varies with speed and torque. In

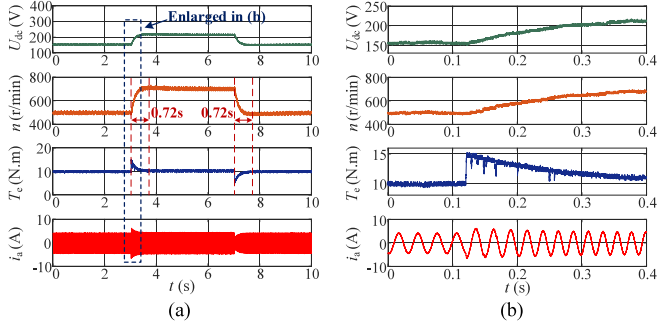


Fig. 16. Dynamic waveforms of the proposed method with  $m = 1$  without compensation when speed steps up and down (from top to bottom, waveforms are DC-bus voltage, rotor speed, electromagnetic torque, a-phase current).

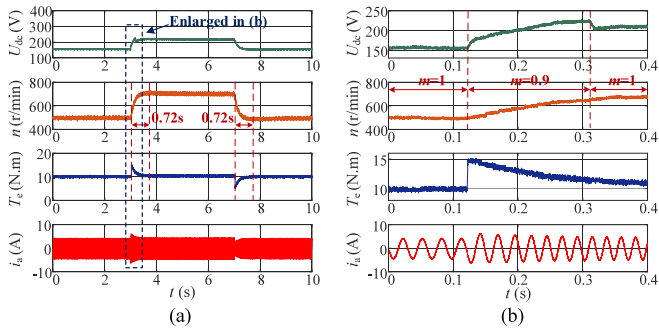


Fig. 17. Dynamic waveforms of the proposed method with  $m = 1$  with compensation when speed steps up and down (from top to bottom, waveforms are DC-bus voltage, rotor speed, electromagnetic torque, and a-phase current).

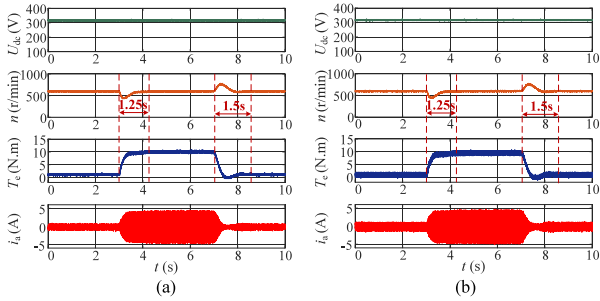


Fig. 18. Dynamic waveforms of two conventional methods when load torque steps up and down (from top to bottom, waveforms are DC-bus voltage, rotor speed, electromagnetic torque, a-phase current). (a) Deadbeat MPC. (b) Reduced-common-mode-voltage MPC.

addition, the settling times of the speed and torque corresponding to the studied methods are nearly the same. In Fig.16, a slight torque oscillation exists in the proposed method without compensation when the speed steps up. The reason for this problem is that the dc-bus voltage is not large enough when speed steps up. By adding a certain compensation, the dc-bus voltage has a slight increase when speed steps up and the torque oscillation is effectively eliminated, as shown in Fig. 17.

Figs. 18 and 19 show the dynamic waveforms of DB-MPC, RCMV-MPC and the proposed method with  $m = 1$  with compensation, where the load torque steps up from 1 to 10 N.m at

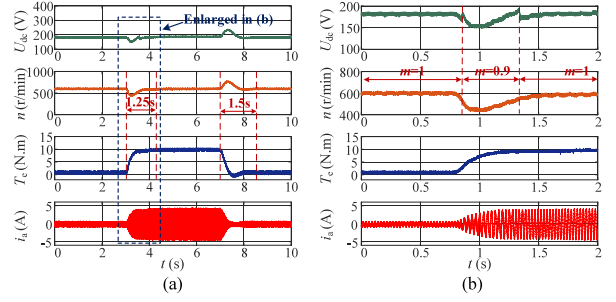


Fig. 19. Dynamic waveforms of the proposed method with  $m = 1$  with compensation when load torque steps up and down (from top to bottom, waveforms are DC-bus voltage, rotor speed, electromagnetic torque, a-phase current).

TABLE V  
COMPARISON BETWEEN PROPOSED METHOD AND CONVENTIONAL METHODS

Method	CMV Reduction	Steady-state Performance	Dynamic Performance	Switching Frequency
DB-MPC	No	good	fast	high
RCMV-MPC	Yes	worse	fast	high
Proposed method with $m=0.67$	Yes	worse	fast	low
Proposed method with $m=1$	Yes	good	fast	low

3 s and steps down from 10 to 1 N.m at 7 s. As shown in Figs. 18 and 19, the dc-bus voltage of DB-MPC and RCMV-MPC are constant, while the dc-bus voltage of the proposed method with  $m = 1$  varies with speed and torque. In addition, the settling times of the speed and torque corresponding to the three methods are nearly the same, and no torque oscillation occurs in the proposed method with  $m = 1$  with compensation when the load torque steps up and steps down.

### C. Overall Comparison of Four Control Methods

Finally, in order to present a clear evaluation of the studied methods, a comprehensive comparison is given in Table IV. In Table V, DB-MPC has excellent steady-state performance, while the CMV reduction is not considered. The CMV reduction is achieved both in RCMV-MPC and the proposed method. However, the RCMV-MPC shows the worse steady-state performance and higher average switching frequency in low-speed region. By redefining the virtual vectors, the proposed method reduces the CMV and switching frequency effectively, where the different values of  $m$  correspond to different reference dc-bus voltages. By taking full advantage of the variability of dc-bus voltage, the proposed method with  $m = 1$  has better steady-state performance than RCMV-MPC and the proposed method with  $m = 0.67$ , and similar excellent to DB-MPC.

## V. CONCLUSION

This article proposes an improved MPC method for PMSM drives with variable dc-bus voltage, to suppress the CMV, improve the control accuracy and reduce the switching frequency. The virtual vectors with lower CMV and switching frequency

are designed. Then, the limitation of designed virtual vectors with fixed dc-bus voltage is investigated. On the basis of analyzing the effects of dc-bus voltage on current distortion, the optimal reference dc-bus voltage is calculated to minimize the current harmonics. Finally, the dc–dc converter is adopted to adjust the dc-bus voltage according to the reference voltage. An experimental comparison of the conventional methods and the proposed scheme is implemented. From the experimental analysis, the conclusions can be summarized as follows.

- 1) The proposed method can reduce the CMV to  $\pm U_{dc}/6$ , which is lower than DB-MPC and equal to RCMV-MPC.
- 2) Compared with RCMV-MPC, the proposed method can significantly reduce the current distortion and switching frequency, especially in the low-speed conditions.
- 3) Compared with DB-MPC, the proposed method with  $m = 1$  has the similar excellent steady-state performance.
- 4) The current harmonics of the proposed method decrease with the decrease of dc-bus voltage, and the optimal dc-bus reference voltage calculated by  $m = 1$  can minimize the current harmonics.

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