

# Effect of the Sampling Parameters in FOCV-MPPT Circuits for Fast-Varying EH Sources

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**Abstract**—The fractional open-circuit voltage (FOCV) method is extensively used in low-power energy harvesting (EH) sources to extract maximum power. For fast-varying EH sources, a fast sampling rate is required. This work theoretically analyzes the influence of the sampling time and period on the harvested power of sinusoidal EH sources. In addition, the circuit limitations to achieve a fast sampling rate are presented and circuits to deal with them proposed and implemented. Furthermore, one of the circuits is based on a novel pseudoFOCV method and achieves the fastest sampling rate. Experimental tests are performed with a 2 Hz, 1 to 3 V sinusoidal source having an output resistance of 127  $\Omega$ , and the results are shown to agree with theoretical predictions. It is shown that the harvested power increases with the sampling rate when the sampling time is negligible (sampling 15 times faster than the source frequency extracts around 99% of the maximum), and for fixed sampling times, there is an optimum sampling rate where the harvested power is maximum. The first result is generic and valid for methods other than the FOCV. Tests were also performed with a small-scale wave energy converter placed in a linear shaker emulating a sea environment. Harvested power increases by 25% with respect using a commercial FOCV unit with a low sampling rate.

**Index Terms**—Energy harvesting (EH), fractional open-circuit voltage (FOCV), maximum power point tracking (MPPT), power management unit (PMU), wave energy converter (WEC), wireless sensor networks (WSN).

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## I. INTRODUCTION

WIRELESS sensor networks (WSN) are becoming ever more prevalent with the implementation of IoT solutions. Supplying power to the sensor nodes is one of the key challenges in WSN design. Batteries have a limited energy and have to be periodically replaced, which can be costly and even unfeasible. In contrast, energy harvesting (EH) can provide unlimited energy. However, EH sources require an additional power management unit (PMU) to convert their variable output to a constant and clean supply to feed the sensor nodes. PMUs should also manage any power mismatch between the source and the load by including an energy storage element (ESE), where energy can be stored or dispatched as required. An additional function of the PMU is maximum power point tracking (MPPT) to continuously ensure the maximum available energy is harvested from the EH source.

One simple MPPT approach, widely used in low-power EH applications and also implemented in commercial chips, such as in [1], is the fractional open-circuit voltage (FOCV) method. This method, thoroughly explained in [2], exploits the nearly linear relationship between the maximum power point (MPP) voltage ( $V_{MPP}$ ) and the open-circuit voltage ( $V_{OC}$ ) of the EH source. Maximum energy is harvested by fixing the output voltage of the EH source to  $V_{MPP}$ , which is a percentage of its  $V_{OC}$ ; this percentage is typically 50% for thermoelectric, piezoelectric (PZT), or radio frequency sources, and 60%–80% for photovoltaic (PV) sources. Typically,  $V_{OC}$  is periodically measured (at a sampling period of  $T_{MPPT}$ ) by momentarily disconnecting the EH source from the PMU during a sampling time ( $t_{SAMP}$ ) and storing the  $V_{OC}$  corresponding to the new environmental conditions.

Some sources, such as wind energy harvesters (WEH) or wave energy converters (WEC), require fast tracking of the MPP because  $V_{OC}$  shows relatively rapid variations. For example, in [3] and [4], a WEH and WEC are presented, respectively, each with  $V_{OC}$  oscillating at around 1.8 Hz; this is fast varying compared with other types of EH sources, such as thermoelectric or PV devices. In [5], it was experimentally demonstrated that, by increasing the sampling rate ( $f_{MPPT} = 1/T_{MPPT}$ ) of a PMU working with a WEC oscillating at 2 Hz, the total harvested energy improved up to 25%. A similar conclusion was reached in [6], where increases of 22% and 44% in the extracted energy were achieved for weakly and strongly coupled PZT vibration harvesters, respectively. In both cases, the increase of energy

TABLE I  
FAST-SAMPLING, RESISTOR-BASED FOCV-MPPT WORKS FOR LOW-POWER  
EH SYSTEMS

Ref.	EH source and frequency	Input voltage	$t_{\text{SAMP}} / T_{\text{MPPT}}$
[7]	Solar PV	2–5 V	5 ms / 100 ms
[8]	Solar PV	2–4 V	33 $\mu$ s / 3.33 ms
[9]	PZT @ 80 Hz	1–3 V	15 ms / 1 s
[10]	Solar PV	> 10 mV	10 ms / 150 ms
[11]	Solar PV	0.1–3 V	Variable ~ - / 25 ms
This work (Config.C)	WEC @ 1.8 Hz	0.08–3.3* V	0.32 $\mu$ s / -

PZT: Piezoelectric device, \*Set by the PMU IC (ADP5092)

captured would help expand the autonomy of EH-powered WSN nodes. However, increasing  $f_{\text{MPPT}}$  can also reduce the harvested energy due to the losses associated with momentarily disconnecting the EH source each sampling event.

There are two approaches for implementing an FOCV-MPPT circuit: resistor based [7], [8], [9], [10], [11] and capacitor based [12], [13], [14]. The former uses a resistor divider to generate the desired fraction of  $V_{\text{OC}}$ , while in the latter, this is achieved by charge sharing. In general, resistor-based circuits offer greater precision in the MPP tracking and require a smaller number of switches. On the other hand, capacitor-based circuits allow a fast charging of the sampling capacitor, leading to a drastic reduction of  $t_{\text{SAMP}}$ .

Implementations of fast-sampling resistor-based FOCV-MPPT methods ( $f_{\text{MPPT}} \geq 1$  Hz) dedicated to low-power EH sources (output power below 10 mW) can be found in the literature. Simjee and Chou [7] and Shao et al. [8] dealt with PV sources achieving sampling times/periods ( $t_{\text{SAMP}}/T_{\text{MPPT}}$ ) of 5/100 ms and 33  $\mu$ s/3.33 ms, respectively. In [9], a vibrational EH source using a PZT device is used, where the PMU refreshes the MPP after the PZT voltage rectification step with  $t_{\text{SAMP}}/T_{\text{MPPT}}$  of 15 ms/1 s. A boost converter was used in [10] to harvest energy from PV cells with very low input voltages and with  $t_{\text{SAMP}}/T_{\text{MPPT}}$  of 10/150 ms. In [11], also dealing with PV applications, changes in the solar irradiance are detected on the input voltage using a custom circuit that makes  $T_{\text{MPPT}}$  variable around 25 ms. Table I summarizes these works, showing in each case the EH source and frequency, input voltage range, and sampling time and period.

Although these works have successfully implemented fast MPPT circuits for low-power applications, the effect of the sampling parameters ( $t_{\text{SAMP}}$  and  $T_{\text{MPPT}}$ ) on the power extraction has not been studied in depth. Balato et al. [15] optimized the parameters of the FOCV method to maximize the power extracted from resonant PZT vibration harvesters after an ac/dc bridge rectification step. However, the parameter  $t_{\text{SAMP}}$  was kept constant to 0.3 s in the analysis and only variations in  $T_{\text{MPPT}}$  were considered. Furthermore, the acceleration amplitude was modulated by a slow 50 s period saw-tooth waveform, so a fast sampling rate was not required since the optimum  $T_{\text{MPPT}}$  value was 16.7 s.

Several companies offer PMU ICs with resistor-based FOCV-MPPT for very low-power EH applications. The BQ25504/5 (Texas Instruments) and the ADP5091/2 (Analog Devices) are

two of the most widely used devices. They both offer efficient power extraction (>80%) from microwatts to milliwatts at a very low input voltage (<100 mV) with ultra-low quiescent currents (<500 nA). However, the  $T_{\text{MPPT}}$  is fixed to 16 s, which is too slow for fast-varying EH sources. The recently launched AEM30330 (e-Peas) is another PMU IC with  $T_{\text{MPPT}}$  down to 18 ms. However,  $t_{\text{SAMP}}$  is 3.8 ms representing up to 20% of the operation time, which drastically reduces its overall efficiency.

This article analyzes the influence of the sampling parameters on the harvested power from a sinusoidal EH source, presents the circuit limitations for achieving fast-sampling, and proposes and tests three circuits to deal with them. Furthermore, one of them is based on a new pseudo-FOCV method. The focus is on resistor-based FOCV, but some analytical results presented are also valid for capacitor-based circuits and even for any MPPT method. Experimental tests are performed, which agree well with the theoretical predictions. One of the tests includes a WEC with accelerations of 2 Hz.

## II. FAST-TRACKING FOCV METHODS: PRINCIPLE, HARVESTED POWER, ARCHITECTURE, AND LIMITATIONS

### A. Principle

For applications with a fast-varying EH source, it is necessary to increase the sampling rate of  $V_{\text{OC}}$  to maintain a good MPPT performance. This can be understood with the aid of Fig. 1 (left-hand side), which shows a sinusoidal  $V_{\text{OC}}$  with offset waveform (top curve), found in some WEC harvesters [4], with the following expression:

$$V_{\text{OC}}(t) = V_{\text{dc}} + V_{\text{ac}} \sin\left(\frac{2\pi t}{T_{\text{EH}}}\right) \quad (1)$$

where  $V_{\text{dc}}$  and  $V_{\text{ac}}$  are the dc offset and sinusoidal amplitude of  $V_{\text{OC}}$ , respectively, and  $T_{\text{EH}}$  is the source period. The loaded EH output voltage under ideal MPP conditions is also shown in Fig. 1:  $V_{\text{MPP}}$  (50% of  $V_{\text{OC}}$  in this example, in the bottom part) and the actual EH output voltage ( $V_{\text{GEN}}$ ) for two different sampling periods and assuming the FOCV-MPPT method. Sampling rates of 12 and three samples per period of the sinusoid are represented with solid ( $V_{\text{GEN}1}$ ) and dashed ( $V_{\text{GEN}2}$ ) staggered lines, respectively.  $V_{\text{GEN}}$  is set equal to 50% of  $V_{\text{OC}}$  at each sampling point, and then held constant until the next sampling event during a time  $t_{\text{HARV}}$ . As can be seen, the faster the sampling rate, the more time  $V_{\text{GEN}}$  spends near  $V_{\text{MPP}}$  and, therefore, the more energy will be extracted. However, as can be seen in more detail in Fig. 1 (right-hand side, inset zoom of the left-hand side), some time is spent in the sampling event ( $t_{\text{SAMP}}$ ), during which the EH source is open circuit and no energy is harvested. During  $t_{\text{SAMP}}$ ,  $V_{\text{GEN}}$  reaches  $V_{\text{OC}}$ , follows it, and finally drops to the new  $V_{\text{MPP}}$  (here  $V_{\text{MPP}1}$  and  $V_{\text{MPP}2}$ ). Note that these positive excursions in  $V_{\text{GEN}}$  during sampling are omitted from the left-hand side figure for clarity.

### B. Harvested Power

Harvested power can be maximized by working at the MPP but it also depends on  $t_{\text{SAMP}}$  and  $T_{\text{MPPT}}$ , as will be shown. For the sake of simplicity, a Thévenin equivalent for the EH

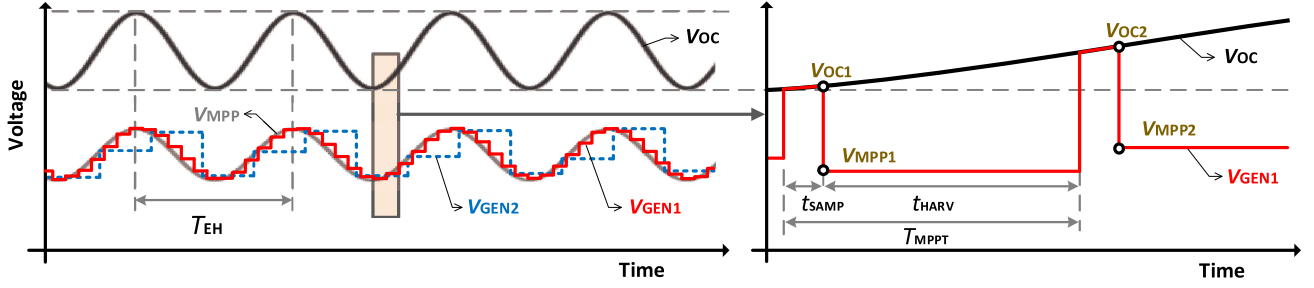


Fig. 1. Left-hand side: sinusoidal  $V_{OC}$  waveform with positive offset for a harvester (top line), the corresponding ideal  $V_{MPP}$  ( $1/2 V_{OC}$ ) and the EH output ( $V_{GEN}$ ) for two sampling periods (solid and dashed staggered lines) using the FOCV-MPPT method. Right-hand side: an inset zoom showing  $V_{OC}$  and  $V_{GEN}$  for the fastest sampling rate.

source is assumed consisting of a voltage source  $V_{OC}$  in series with an internal resistor  $R_G$ . This is the case for several types of EH sources (e.g., thermoelectric, electromagnetic, and radiofrequency), including that used later in Section V-C. For these sources, maximum power is achieved when  $V_{MPP} = 0.5 \cdot V_{OC}$ , as stated by the maximum power transfer theorem [16]. Assuming (1) for  $V_{OC}$ , the maximum average power is given by

$$P_{MPP} = \frac{\overline{V_{OC}^2}}{4R_G} = P_{dc} \left[ 1 + \frac{\alpha^2}{2} \right] \quad (2)$$

where  $P_{dc} = \frac{V_{dc}^2}{4R_G}$ ,  $\alpha = \frac{V_{dc}}{V_{dc}}$ , and the overbar denotes a time average over one source period. However, this result is achieved when no sampling effect is considered. The Appendix presents an analytical derivation for obtaining the approximate power given to a load ( $P_{LOAD}$ ) considering the sampling process, leading to

$$P_{LOAD} \approx P_{dc} \left\{ \left[ (7 + 3r_S) \frac{128}{45} \alpha^2 \right] r_M^4 - \left[ \frac{64}{9} \alpha^2 \right] r_M^2 + \left[ 1 + \frac{8}{15} \alpha^2 \right] (1 - r_S) \right\} \quad (3)$$

where  $r_S = \frac{t_{SAMP}}{T_{MPPT}}$  and  $r_M = \frac{T_{MPPT}}{T_{EH}}$ . The parameter  $r_S$  denotes the time percentage the circuit is sampling and, thus, not harvesting, whereas the inverse of  $r_M$  denotes the number of samples per period of the signal source. The approximate form in (3) is applicable when  $r_S \ll r_M \leq 0.25$ . For  $r_S$ ,  $r_M \rightarrow 0$  (negligible sampling time and infinite sample rate), we get

$$P_{LOAD} = P_{MAX} = P_{dc} \left[ 1 + \frac{8\alpha^2}{15} \right] \quad (4)$$

which slightly differs from (2) because in the Appendix a piecewise quadratic approx. is used for  $V_{OC}$  instead of (1).

Fig. 2 shows  $P_{LOAD}$  normalized to  $P_{MAX}$  versus  $1/r_M$  for several sampling scenarios, according to (3) and using  $\alpha = 0.5$ . When  $r_S$  is constant (square markers), the normalized power rises to a maximum as  $1/r_M$  increases. In addition, the lower the  $r_S$ , the lower the losses due to disconnection of the EH source during sampling, and the higher the power. In fact, for  $1/r_M \rightarrow \infty$ , from (3), the relative power loss is  $r_S$ . For  $r_S \rightarrow 0$ , around 99% of the maximum power is harvested when sampling 15 times faster than the source frequency ( $f_{MPPT} = 15 \cdot f_{EH}$ ). This result is also valid for MPPT methods other than the FOCV. On the other hand, when  $r_S r_M = \frac{t_{SAMP}}{T_{EH}}$  is constant (circle markers), i.e.,  $t_{SAMP}$  and

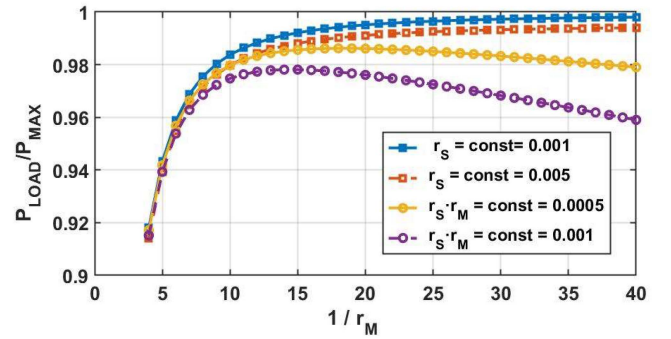


Fig. 2.  $P_{LOAD}$  normalized to  $P_{MAX}$  versus  $1/r_M$  for different sampling scenarios, according to (3) using  $\alpha = 0.5$ .

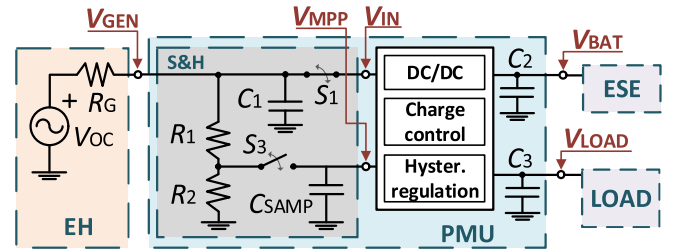


Fig. 3. Standard PMU architecture implementing a resistor-based S&H circuit for a FOCV-MPPT. An EH source (input), ESE, and LOAD (output) are also represented.

$T_{EH}$  are fixed, increasing  $1/r_M$  increases further  $r_S$  and, thus, the percentage of time sampling without harvesting energy from the EH source. In this case, there is an optimum value of  $r_M$  where the normalized power is maximum; this maximum power is higher and the optimum  $r_M$  lower for lower values of  $r_S r_M$ . A similar behavior was observed in [15].

### C. Architecture

In resistor-based FOCV circuits, a resistor divider is used to generate the desired fraction of  $V_{OC}$  and then store it in a sampling capacitor ( $C_{SAMP}$ ).

Fig. 3 shows the block diagram of a standard PMU with this FOCV configuration. An EH source is connected at the input (here, a Thévenin equivalent), whereas an ESE and a load are connected at the output. This work focuses on the sample and hold (S&H) circuit of the MPPT controller, which is highlighted inside the PMU box. However, it is noted that the PMU includes

other functionalities, the most important being dc/dc conversion and control of power flow between the EH source, ESE, and LOAD (e.g., a sensor node) depending on the available harvested power, the load requirements, and the state of charge of the ESE.

At the PMU input ( $V_{\text{GEN}}$ ), a capacitor  $C_1$  is placed as a buffer between the PMU and the EH source. Further, two more capacitors ( $C_2$  and  $C_3$ ) are placed at the ESE ( $V_{\text{BAT}}$ ) and LOAD ( $V_{\text{LOAD}}$ ), respectively. At each sampling event, the PMU IC opens the switch  $S_1$  and closes switch  $S_3$  during  $t_{\text{SAMP}}$ . Thus,  $V_{\text{GEN}}$  rises to  $V_{\text{OC}}$  (see the right-hand side of Fig. 1), the sampled  $V_{\text{MPP}}$  appears at the output of the resistive divider formed by  $R_1$  and  $R_2$  and is stored at  $C_{\text{SAMP}}$ . Then, during  $t_{\text{HARV}}$ ,  $S_1$  closes and  $S_3$  opens, and the PMU forces  $V_{\text{IN}}$  to the last sampled value of  $V_{\text{MPP}}$  by periodically moving energy from  $C_1$  to  $C_2$  and  $C_3$ .

#### D. Limitations

Fig. 2 shows that to increase harvested power both  $r_{\text{S}}$  and  $r_{\text{M}}$  must be small, with  $t_{\text{SAMP}} \ll T_{\text{MPPT}} \ll T_{\text{EH}}$ . During  $t_{\text{SAMP}}$ ,  $C_{\text{SAMP}}$  must be updated to a new value of  $V_{\text{MPP}}$ . In order for the error in the sampled voltage to be, e.g.,  $< 1\%$ , we require the charging ratio  $r_{\text{C}} = \frac{t_{\text{SAMP}}}{\tau}$  to be higher than 4.6. The time constant  $\tau$  is defined as  $\tau = R_{\text{TH}}C_{\text{SAMP}}$  where  $R_{\text{TH}}$  is equivalent to  $R_1$  in parallel with  $R_2$ , assuming the equivalent output resistance of the EH source ( $R_{\text{G}}$ ) negligible. Thus, for a fixed value of  $r_{\text{C}}$ , a reduction of  $t_{\text{SAMP}}$  implies decreasing  $\tau$  and, therefore, either  $R_{\text{TH}}$  or  $C_{\text{SAMP}}$ .

On the one hand,  $R_{\text{TH}}$  can be reduced by reducing the values on the resistor divider. This leads to a reduction of the global efficiency because the resistor divider is always connected to  $V_{\text{GEN}}$  and consuming power. Thus,  $R_1 + R_2 \gg R_{\text{G}}$  is required. In this way, an accurate  $V_{\text{MPP}}$  is also attained. On the other hand, reducing  $C_{\text{SAMP}}$  has two potential limitations. First, it must hold  $V_{\text{MPP}}$  during  $t_{\text{HARV}}$  in spite of any leakage current at the PMU pin connected to  $C_{\text{SAMP}}$ . Second,  $C_{\text{SAMP}}$  must deal with the charge injection produced by  $S_3$ . It is worth noting that the constraints on the  $R$  and  $C$  values resulting from the need for low power consumption and capacitive storage of the sampled voltage are particular to the PMU application; they do not apply to other sampling systems, such as commercial voltage probes, and consequently, these can readily achieve much shorter sampling times.

Several ideas can be found in the literature to deal with these issues. In [10], a third switch is added to the standard resistor-based S&H circuit (see Fig. 3). This switch disconnects the S&H circuit during  $t_{\text{HARV}}$ , leading to a reduction of power losses. Then, the resistor divider values can also be decreased to reduce  $\tau$ , allowing faster sampling rates. A solution to solve the problem of leakage on  $C_{\text{SAMP}}$  has been presented in [11] and [14]. Both works share the same idea even though [11] is resistor based and [14] is capacitor based. It consists of comparing the sampled  $V_{\text{MPP}}$  with a number of fixed voltage references from a resistor string and choosing the one closest to the new  $V_{\text{MPP}}$ . This is a complex solution that also adds the error of the resistor string accuracy. Finally, a solution for the problem of the charge injection on  $C_{\text{SAMP}}$  has been proposed in [12], where a pair of

dummy switches driven in counter phase mitigate the increase of voltage on the sampling capacitor.

Commercial solutions, such as the ADP5092, offer relatively large sampling times and periods of  $t_{\text{SAMP}} = 256$  ms and  $T_{\text{MPPT}} = 16$  s ( $r_{\text{S}} = 1.6\%$ ), which are inadequate for applications requiring fast sampling. These large times derive from the suggested values for  $R_1 + R_2$  (20 M $\Omega$ ) and  $C_{\text{SAMP}}$  (10 nF), leading to  $\tau = 50$  ms (with  $R_1 = R_2$ , worst case) and  $r_{\text{C}} = 5.12$ .

### III. PROPOSED CONFIGURATIONS

This section presents three proposed fast-sampling PMU configurations (see Section III-A) followed by their S&H circuit design (see Section III-B) and practical implementation (see Section III-C).

#### A. Reference and Proposed Fast-Sampling Configurations

In this work, a typical configuration of the ADP5092, such as the one found in its evaluation board (EB-ADP5092), was used as the *reference* configuration (config. R hereafter) to be compared with three new proposed and fast-sampling PMU configurations where  $t_{\text{SAMP}}$  and  $T_{\text{MPPT}}$  are greatly reduced to achieve low values of  $r_{\text{S}}$  and  $r_{\text{M}}$ . These units include the ADP5092 IC, to take advantage of its robustness and ultra-low power consumption, and additional low-power sampling circuitry, to drastically increase the sampling rate with respect to config. R.

Fig. 4 shows schematics of the four PMU configurations. Just the S&H circuit changes between configurations (central box). At the input, the WEC model reported in [17] is placed, which consists of a Thévenin equivalent generating a sinusoidal voltage as in (1). An  $R_{\text{G}}$  of 127  $\Omega$ , similar to the value reported in [17], is used in the following sections. For the ESE, a 165-mAh, 3.7-V Li-Ion polymer battery charged to 3.8 V is selected and no load is connected to the SYS pin. So, the output power is only delivered to the ESE. The resistor divider is set to 50% ( $R_1 = R_2$ ). In total, nine test points are used for the analysis of the PMU performance. Four are common:  $V_{\text{GEN}}$ ,  $V_{\text{BAT}}$ ,  $I_{\text{IN}}$  (input current), and  $I_{\text{OUT}}$  (output current); four are specific of the proposed configurations (A, B, and C):  $V_{\text{DIV}}$  (junction of  $R_1$  and  $R_2$ ),  $V_{\text{MPP}}$ ,  $V_{\text{IN}}$ , and  $V_{\text{PULSE}}$  (sampling control signal); one more is only used for config. B:  $V_{\text{OA}}$ . Config. R works as previously described in Section III-C. In the proposed configurations, the MPPT pin was left floating since  $V_{\text{MPP}}$  is provided to  $C_{\text{SAMP}}$  at the CBP pin through the external switch  $S_3$ , which works as described in Section II-C. Next, the particularities of the proposed configurations are described.

- 1) *Config. A*: A single pole double throw switch  $S_{12}$  connects  $V_{\text{GEN}}$  with either  $V_{\text{IN}}$  or the resistor divider. During  $t_{\text{SAMP}}$ ,  $V_{\text{GEN}}$  connects to the resistor divider, leaving  $V_{\text{IN}}$  floating. Then, during  $t_{\text{HARV}}$ ,  $S_{12}$  reconnects  $V_{\text{GEN}}$  with  $V_{\text{IN}}$ , disconnecting the resistor divider to avoid losses. So,  $R_1$  and  $R_2$  can be small to reduce  $t_{\text{SAMP}}$  and achieve a fast MPPT while resistive power losses are kept small. This configuration is similar to that implemented in [10] with a different distribution of the switches.

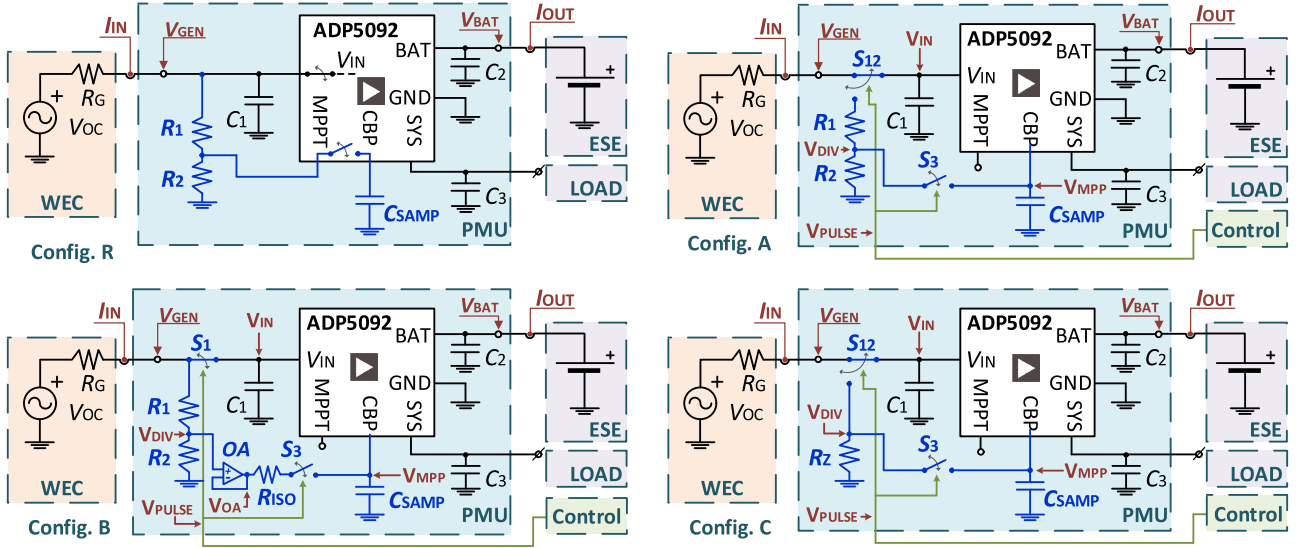


Fig. 4. Proposed PMU configurations: Reference (top left), A (top right), B (bottom left), and C (bottom right). All configurations include the WEC electrical model as the input source and an ESE as the sole output load.

- 2) *Config. B*: An operational amplifier (OA) working as a voltage follower is included with a series resistor ( $R_{ISO}$ ) to faster stabilize its output ( $V_{OA}$ ).  $C_{SAMP}$  is directly charged from the OA output so that its charging time and, thus,  $t_{SAMP}$  mainly depends on the slew rate (SR) and OA bandwidth. Thus,  $R_1$  and  $R_2$  can be increased again to minimize losses without affecting  $t_{SAMP}$ , as long as the effect of the OA input parasitic capacitance ( $C_{OA}$ ) is neglectable.
- 3) *Config. C*: During  $t_{SAMP}$ ,  $S_{12}$  connects  $V_{GEN}$  to an impedance reference  $R_Z (= R_G)$ , so that  $V_{DIV}$  and  $V_{MPP}$  remain as  $V_{OC}/2$ . Thus, the WEC must be previously characterized to know  $R_G$ , and this value should not change significantly over time. During  $t_{HARV}$ ,  $S_{12}$  connects  $V_{GEN}$  to  $V_{IN}$ , disconnecting  $R_Z$ . Given  $R_Z$  is small,  $t_{SAMP}$  can be drastically reduced. This configuration constitutes a novel MPPT method not reported in earlier works and inspired by the working mode of the *e-Peas* chips. It combines the MPPT techniques of resistor emulation [18] and FOCV.

### B. S&H Circuit Values

In order to keep the power losses small, appropriate values of  $R_1$ ,  $R_2$ , and  $C_{SAMP}$  must be used in all configurations. Config. C does not use  $R_1$  and  $R_2$  but  $R_Z = R_G$ . It will be assumed that each loss factor leads to a maximum power loss of  $\varepsilon \cdot P_{MPP}$  with  $\varepsilon \ll 1$ . First, power is wasted in  $R_1$  and  $R_2$ , but they are permanently connected (and in particular during  $t_{HARV}$ ) just in configs. R and B. Thus, we require  $R_1 + R_2 \geq R_G / \varepsilon$  for these two configurations. Second, errors in the determination of  $V_{MPP}$  also lead to a power reduction that applies to all configurations. Assuming the Thévenin equivalent for the energy source, his instantaneous delivered power must satisfy

$$\frac{V_{OC} - V_{GEN}}{R_G} V_{GEN} \geq (1 - \varepsilon) \frac{V_{OC}^2}{4R_G} \quad (5)$$

which is a quadratic inequality that can be easily solved in

$$\frac{V_{OC}}{2} (1 - \sqrt{\varepsilon}) \leq V_{GEN} \leq \frac{V_{OC}}{2} (1 + \sqrt{\varepsilon}). \quad (6)$$

Errors in  $V_{MPP}$  can have the following three causes:

- 1) loading effect of  $R_G$  when using  $R_1$  and  $R_2$  (in all configurations except config. C),
- 2) leakage current ( $I_{leak}$ ) from the ADP5092 CBP pin on  $C_{SAMP}$ , and
- 3) charge injection effect ( $\Delta Q$ ) on  $C_{SAMP}$  due to the internal switch in config. R and  $S_3$  in the proposed configurations.

After some processing, it is found that the following conditions must be met to accomplish (6):  $R_1 + R_2 \geq R_G(1 - \sqrt{\varepsilon})/\sqrt{\varepsilon}$  by cause 1,  $C_{SAMP} \geq I_{leak} \cdot T_{MPPT}/(\cdot V_{MPP})$  by cause 2, and  $C_{SAMP} \geq Q/(\cdot V_{MPP})$  by cause 3.

As an example,  $\varepsilon = 0.1\%$  is assumed. Thus,  $R_1 + R_2 \geq 1000R_G$  for configs. R and B. On the other hand, according to cause 1,  $R_1 + R_2 \geq 30.65 \cdot R_G$  for all configs. except C, which is less restrictive than the previous condition, so it only applies to config. A. Assuming  $R_1 = R_2$ , the minimum value of  $\tau$  ( $\tau_{min}$ ) is  $250 \cdot R_G \cdot C_{SAMP}$  for configs. R and B,  $7.66 \cdot R_G \cdot C_{SAMP}$  for config. A, and just  $0.5 \cdot R_G \cdot C_{SAMP}$  for conf. C. So, config. C has more room for the reduction of  $\tau$  and, thus, for faster sampling rates.

As for  $C_{SAMP}$ , assuming  $V_{MPP} = 1V$  (typical in small-scale WECs according to [4]) and  $I_{leak} = 10$  pA (typical value of the ADP5092),  $C_{SAMP} = 316.5 \cdot T_{MPPT}$  (in pF). For config. R ( $T_{MPPT} = 16$  s), this leads to  $C_{SAMP} \geq 5$  nF (10 nF recommended by the ADP5092). Instead, in the proposed configurations and assuming  $r_M = 0.1$  with  $f_{EH} = 1/T_{EH} = 1.8$  Hz [3], [4],  $C_{SAMP} \geq 17.5$  pF, so much lower. On the other hand, considering  $\Delta Q = 5$  pC (feasible value for commercial switches),  $C_{SAMP} \geq 158$  pF in all configurations. Lower values of  $V_{MPP}$  would lead to higher values of  $C_{SAMP}$  in all cases.

TABLE II  
COMPONENT LIST FOR EACH PMU CONFIGURATION

	Config. R	Config. A	Config. B	Config. C
$S_{12} / S_1$	-	MAX4714	MAX4716	MAX4714
$S_3$	-	MAX4594	MAX4594	MAX4594
$R_1 / R_2$	10 M $\Omega$	100 k $\Omega$	10 M $\Omega$	-
OA	-	-	MAX40007	-
$R_{ISO}$	-	-	3,3 k $\Omega$	-
$R_Z$	-	-	-	127 $\Omega$
$C_{SAMP}$	10 nF	1.2 nF	10 nF	10 nF
$\tau$	50 ms	60 $\mu$ s	7.5*/10.6** $\mu$ s	0.7 $\mu$ s

\*Calculated with the OA input capacitance instead  $C_{SAMP}$ .

\*\*Derived from the OA bandwidth.

### C. Implementation of the PMUs

A generic modular circuit board was produced to hold the three proposed PMU configurations, which includes the ADP5092 IC and the additional sampling circuitry (see Fig. 4). The voltage test points were included in the board and the current test points ( $I_{IN}$  and  $I_{OUT}$ ) were external. The active components included in the new configurations (OA,  $S_3$ , and  $S_{12}$  or  $S_1$ ) were internally fed from the ESE.

Table II tabulates the components of the sampling circuitry used for each of the four PMU configurations. As can be seen, in configs. R and B, the standard values proposed by the ADP5092 manufacturer were used for  $R_1$  and  $R_2$  (10 M $\Omega$ ) and  $C_{SAMP}$  (10 nF), whereas lower values were used for config. A (100 k $\Omega$ , 1.2 nF). Other required components were chosen following the manufacturers' recommendations, as for example,  $C_1 = 10 \parallel 01 \mu$ F,  $C_2 = 220 \mu$ F, and  $C_3 = 4.7 \mu$ F. The active components of the proposed configurations were carefully chosen to be low-power devices. For the OA, a MAX40007 (*Maxim*, 0.7  $\mu$ A of typical supply current, rail-to-rail output) was selected. A low switching time and ON-state resistance ( $R_{ON}$ ) are sought for the switches. In particular,  $R_{ON} \ll R_G$  for  $S_{12}$  and  $S_1$  to reduce losses during  $t_{HARV}$  and for  $S_{12}$  in config. C to set an accurate  $V_{MPP}$  during  $t_{SAMP}$ . For  $S_3$ ,  $R_{ON}$  adds during  $t_{SAMP}$  to  $R_1 \parallel R_2$  in config. A, and to  $R_G \parallel R_Z$  in config. C, thus also contributing to  $\tau$ . A low-charge injection is sought for  $S_3$  to minimize its effects at  $C_{SAMP}$  after the sampling time. For  $S_{12}$ , a MAX4714 (*Maxim*, 0.04  $\mu$ A, 13 ns, 0.6  $\Omega$ ) was selected for  $S_1$  a MAX4716 (*Maxim*, 0.04  $\mu$ A, 12 ns, 0.3  $\Omega$ ) and for  $S_3$  a MAX4594 ( $\sim 0.02 \mu$ A, 25 ns, 6.5  $\Omega$ , 2pC).

Table II also tabulates the resulting values of  $\tau$ . As can be seen, config. R presents a value much higher than the proposed configurations. In config. B, the OA buffers  $C_{SAMP}$ , and  $\tau$  is, thus, calculated as  $R_{TH}C_{OA}$  ( $C_{OA} = 1.5$  pF), which allows high values for  $R_1$  and  $R_2$  while still achieving a low value of  $\tau$ , in particular  $\tau = 7.5 \mu$ s. But the OA bandwidth (15 kHz) leads to a time constant  $\tau_{OA} = 10.6 \mu$ s, so more restrictive. In addition, the SR (12 V/ms) needs also to be considered for large signal variations. Config. C uses  $R_Z = R_G$  (127  $\Omega$ , 0.1%) and, thus,  $\tau = 0.7 \mu$ s (accounting also for the series  $R_{ON}$  of  $S_3$ ).

For the case of  $R_G = 127 \Omega$ , following the design rules of Section III-B for  $R_1$  and  $R_2$  and setting  $C_{SAMP} = 1$  nF

(accounting for a value of  $V_{MPP}$  even lower than 1 V), the resulting values of  $\tau_{min}$  are 32  $\mu$ s, 972 ns, and 70 ns for configs. R, A, and C (with the effect of  $S_3$  included), respectively. A  $\tau$  of 48 ns results for config. B with  $C_{OA} = 1.5$  pF but parasitic capacitances can significantly increase this value. Furthermore, the limiting factor will be the OA bandwidth ( $\tau_{OA} = 10.6 \mu$ s) and SR. With  $r_C = 4.6$ ,  $t_{SAMP}$  results in 147  $\mu$ s, 4.47  $\mu$ s, 48.8  $\mu$ s, and 322 ns for configs. R, A, B, and C, respectively. Thus, all the proposed configurations achieve a lower  $t_{SAMP}$  than config. R, and in particular config. C achieves a near 500-fold decrease, thus allowing very fast sampling. This configuration is also added at the end of Table I to compare it with the literature works presented in Section I. As can be seen, the achieved value of  $t_{SAMP}$  is greatly reduced compared with the previous reported fast-tracking works, and in particular is 100 times smaller than that of [8], which presented the smallest value of  $t_{SAMP}$ . No value is shown for  $T_{MPPT}$  since it depends on the value of  $r_S$ .

### IV. PERFORMANCE OF THE SAMPLING CIRCUITRY

The performance of the additional sampling circuitry of the proposed configurations was tested using the components of Table II. An HP33120A function generator (FG) with an internal output resistance of 50  $\Omega$  was used with an external 77  $\Omega$  series resistor giving a total resistance of  $\sim 127 \Omega$ , in order to emulate the WEC. The FG was set with a voltage step from 0 to 3 V ( $V_{OC}$ ), which was selected considering [4].  $V_{PULSE}$  was provided by a DAQ (USB-6216, National Instruments) and was configured to provide  $T_{MPPT} = 24$  ms and  $t_{SAMP} = 0.5$  ms, which leads to  $r_S = 2.1\%$ , similar to that of the config. R (1.6%). With these values,  $r_C$  results in 8.3, 67, and 700 for configs. A, B, and C, respectively, ensuring an accurate  $V_{MPP}$  ( $r_C > 4.6$ ) in all cases. Then, the dynamic behavior of the voltage test points (except  $V_{BAT}$ ) was observed and the main sampling parameters identified.

A four-channel oscilloscope (Lecroy Wavesurfer 3024) was used to measure the voltage test points; the high-impedance points ( $V_{DIV}$  and  $V_{MPP}$ ) were buffered with an external OA (TL064CN). Fig. 5 shows the temporal profile of the signals. The plots on the left- and right-hand sides show, respectively, zoomed-out and zoomed-in views during the sampling process. Each pair of plots corresponds to a different PMU configuration.

The left-hand side plots show all the signals except  $V_{MPP}$ . A  $V_{PULSE}$  of 0.5 ms ( $t_{SAMP}$ ) is observed ( $T_{MPPT}$  of 24 ms not shown). During  $t_{SAMP}$  and for configs. A and B,  $V_{GEN}$  is disconnected from  $V_{IN}$  and rises from the previous MPP value (0 V in this test) to the current  $V_{OC}$  (3 V) whereas  $V_{IN}$  remains at 0 V. Meanwhile,  $V_{DIV}$  rises from 0 to 1.5 V with a theoretical  $\tau = 60 \mu$ s for config. A. For config. B,  $\tau$  is higher than predicted because of the parasitic capacitance of the external buffer OA.  $V_{OA}$  follows  $V_{DIV}$  with a slope limited by the OA SR. For config. C,  $V_{GEN}$  is directly connected to  $V_{DIV}$  and both rise abruptly to 1.5 V since now  $\tau = 0.7 \mu$ s, much smaller.

For all configurations,  $V_{GEN}$  is reconnected to  $V_{IN}$  after  $t_{SAMP}$  and falls to 0 V (present value at  $C_1$ ) before rising with a nominal time constant of 1.27 ms ( $C_1 = 10 \mu$ F and  $R_G = 127 \Omega$ ) to settle at the new  $V_{MPP}$  (1.5 V). After this, a small ripple

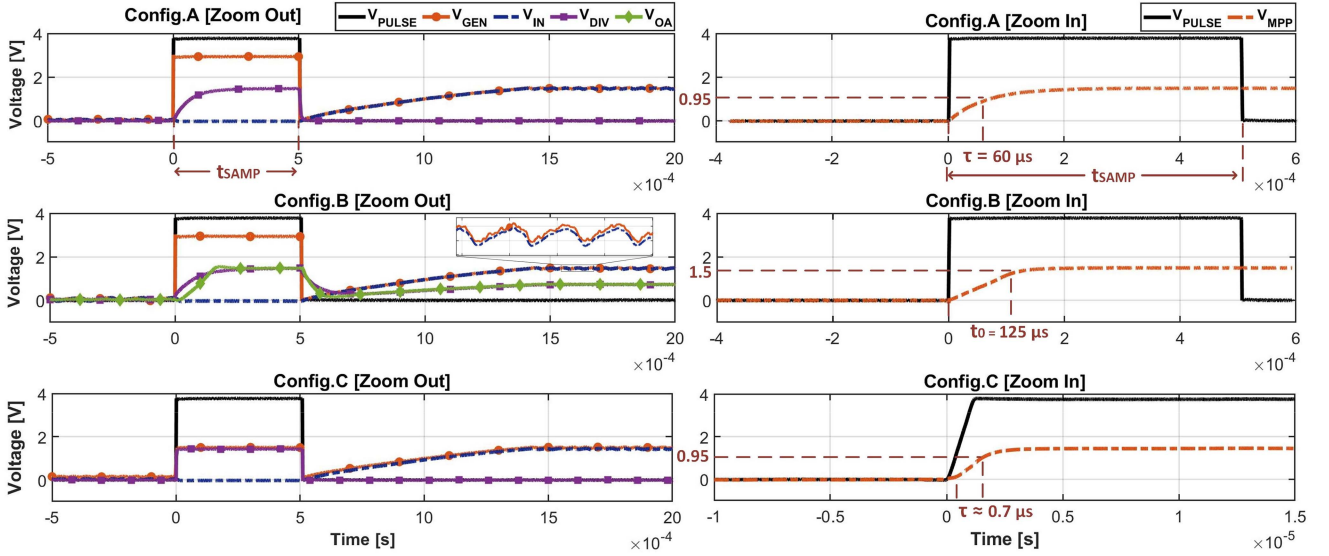


Fig. 5. Dynamic test of the sampling circuitry of the three proposed configurations. Left-hand side: zoomed-out view showing  $V_{PULSE}$  (solid line),  $V_{GEN}$  (circle marker),  $V_{IN}$  (dashed line),  $V_{DIV}$  (square marker), and  $V_{OA}$  (diamond marker). Right-hand side: zoomed-in view of  $V_{MPP}$  (dashed line) and  $V_{PULSE}$  (solid line).

appears (only shown in an inset zoom of config. B plot) between two threshold values around  $V_{MPP}$ , typical of the energy transfer process from the PMU input to its output: when the internal dc/dc converter is OFF,  $C_1$  charges and  $V_{IN}$  ( $= V_{GEN}$ ) increases; contrariwise, when the converter is on and transfers energy to the output,  $C_1$  discharges and  $V_{IN}$  decreases.  $V_{DIV}$  decreases to 0 V in configs. A and C because  $V_{GEN}$  is disconnected. However, in config. B, it follows  $V_{GEN}/2$  after some settling time given by  $\tau$  and  $V_{OA}$  is again initially subjected to the OA SR.

The right-hand side plots show a zoom-in of  $V_{PULSE}$  and  $V_{MPP}$ . In all the configurations and during  $t_{SAMP}$ ,  $V_{MPP}$  reaches 1.5 V from an initial value of 0 V, as previewed. In config. A,  $\tau = 60 \mu\text{s}$  is marked; hence,  $t_{SAMP}$  is  $\geq 8\tau$ , ensuring that  $V_{MPP}$  reaches 1.5 V with a negligible error. In config. B,  $V_{MPP}$  linearly increases to 1.5 V in about  $125 \mu\text{s}$  ( $t_0$ ), hence within  $t_{SAMP}$ , due to the OA SR. The small peak in  $V_{OA}$  (left-hand side plot) is mitigated, thanks to  $R_{ISO}$ . In config. C, a fast  $\tau \approx 0.7 \mu\text{s}$  is identified (note that a different temporal scale is used). Hence, a much lower value of  $t_{SAMP}$  could be used to reduce the losses due to the opening of the EH source. After  $t_{SAMP}$ ,  $V_{MPP}$  stabilizes at 1.5 V.

## V. PERFORMANCE OF THE PMUS

This section shows the PMU experimental performance of the four PMU configurations. First, the three proposed configs. were compared at a fixed  $r_S$  and  $r_M$  (see Section V-A). Second, config. C, the configuration with more room for fast-sampling, was optimized following the design criteria of Section III-B and then tested at different sampling rates (see Section V-B). These results were compared with those obtained in Section II-A using the analytical expressions. Finally, config. C was tested with a WEC placed on a linear shaker emulating sea conditions (see Section V-C). Config. R was also used in Section V-A and C to assess the achieved improvement of the proposed configurations.

In Section V-A and B, the FG with the added external resistor was used ( $R_G \sim 127 \Omega$ ) and set to provide a sinusoid with offset, according to (1), with  $V_{dc} = 2 \text{ V}$  and  $V_{ac} = 1 \text{ V}$  and a frequency between 1.8 and 2 Hz to emulate a small-scale WEC under sea-wave excitation [4]. So, from (2),  $P_{MPP} = 8.86 \text{ mW}$ . Instead, in Section V-C, the WEC presented in [4] was used under an emulated sea environment. In all sections,  $V_{PULSE}$  was provided by the DAQ, and the four-channel oscilloscope was used to measure  $V_{GEN}$ ,  $V_{BAT}$ ,  $I_{IN}$ , and  $I_{OUT}$ . The currents were estimated with a couple of shunt resistors ( $0.5 \Omega$ ,  $3.3 \Omega$ ), placed at the test points defined in Fig. 4 ( $I_{IN}$ ,  $I_{OUT}$ ), and associated current sense amplifiers (CSAs). The respective oscilloscope channels were placed at the outputs of the CSAs. Then, input and output powers were, respectively, calculated as  $P_{IN} = V_{GEN} \cdot I_{IN}$  and  $P_{OUT} = V_{BAT} \cdot I_{OUT}$ . To properly estimate the average powers and currents, 5 s of data were measured for configurations A–C and 200 s for config. R. The setup of the shunt resistors and CSAs is fully described in [[17], Sec. III].

### A. Comparison Between Configurations

Configurations A–C were assessed with a  $T_{MPPT} = 24 \text{ ms}$ ,  $t_{SAMP} = 0.5 \text{ ms}$ , and  $f_{EH} = 1.8 \text{ Hz}$ . So,  $r_S = 1/48$  and  $r_M = 0.0434$  (about 23 samples per period of the signal source). Fig. 6 shows 2 s of measured data from config. A. As can be seen, when the PMU disconnects the FG output every 24 ms,  $V_{GEN}$  rises to  $V_{OC}$  (1–3 V) during  $t_{SAMP}$  and then settles to  $V_{OC}/2$  (0.5–1.5 V) during  $t_{HARV}$ , following the behavior shown in Fig. 1. This behavior is different for config. C, where  $V_{GEN}$  does not rise to  $V_{OC}$  but follows  $V_{OC}/2$  because the presence of  $R_Z$ . During  $t_{SAMP}$ , both  $I_{IN}$  and  $I_{OUT}$  drop to zero. During  $t_{HARV}$ ,  $I_{IN}$  is around  $V_{OC}/(2R_G)$ , thus between 3.9 and 11.8 mA. Experimental values of  $I_{OUT}$  mainly agree with those estimated from  $\eta I_{IN} V_{IN}/V_{BAT}$ , being  $\eta$  the efficiency of the ADP5092 IC ( $\sim 80\%$ – $90\%$  from the datasheet).  $V_{BAT}$  shows a

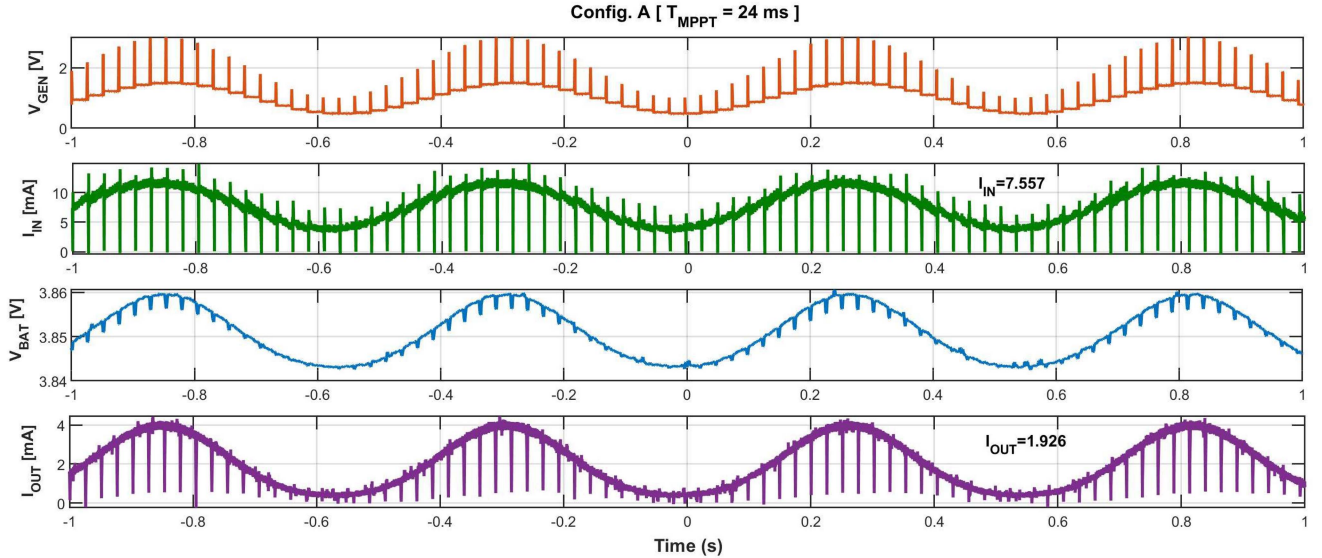


Fig. 6. Acquired waveforms (2 s) for config. A with  $T_{MPPT} = 24$  ms. From top to bottom:  $V_{GEN}$ ,  $I_{IN}$ ,  $V_{BAT}$ , and  $I_{OUT}$ . For this test,  $V_{OC}$  was set between 1 and 3 V and  $T_{EH}$  at 1.8 Hz.

TABLE III  
PERFORMANCE OF THE FOUR PMU CONFIGURATIONS

Config.	$T_{MPPT}$ (ms)	$V_{GEN}$ (V)	$P_{IN}$ (mW)	$P_{OUT}$ (mW)	$\eta$ (%)
A	24.1	1.012	8.42	7.42	88.2
B	24.1	1.012	8.41	7.38	87.7
C	24.1	0.959	8.58	7.34	85.6
R	16k	0.984	7.21	6.13	85.0

$V_{GEN}$ ,  $P_{IN}$ , and  $P_{OUT}$ : Mean values.

small sinusoidal ripple ( $< 20$  mV) due to the variation of  $I_{OUT}$  and the shunt resistor ( $3.3 \Omega$ ) used to measure it.

Table III tabulates a summary of the experimental results, showing the averaged values of  $V_{GEN}$ ,  $P_{IN}$ , and  $P_{OUT}$ . The efficiency ( $\eta$ ) has been obtained as  $P_{OUT}/P_{IN}$  and includes the efficiency of the ADP5092 IC as well as the power wasted by the sampling circuitry (for configs. A–C) and by the input stage resistors but not the capability in harvesting the maximum power from the signal source. Configs. A and B present very similar results. Both have negligible losses due to the resistor divider with the efficiency being slightly smaller in config. B (just 0.5%), in part because some additional power is wasted in the OA. Config. C presents higher  $P_{IN}$  (near the calculated  $P_{MPP}$ ) but lower  $P_{OUT}$  than configs. A and B. The increase in  $P_{IN}$  is justified by the power wasted in  $R_Z$  during  $t_{SAMP}$  (0.186 mW nominally), which does not contribute to  $P_{OUT}$ . The lower value of  $P_{OUT}$  could be caused by the lower average value achieved in  $V_{GEN}$  (0.959 V), maybe due to a mismatch between  $R_G$  and  $R_Z$ , which would lead to a suboptimal working voltage for  $V_{IN}$  (lower than  $V_{OC}/2$ ). Anyway,  $P_{OUT}$  is just 1% lower than that achieved in config. A. Finally, config. R presents the worst results, as expected.  $P_{IN}$  and  $P_{OUT}$  are 17% and 21% higher in config. A than in the config. R. This happens

since  $T_{MPPT}$  is much higher than  $T_{EH}$ , leading to a significant reduction of the harvested energy.

### B. Effect of the Sampling Time and Period

Config. C was chosen to perform further tests since it has similar output power to configs. A and B and presents more room for the reduction of  $t_{SAMP}$ , thus allowing the fastest  $f_{MPPT}$ . For the tests,  $C_{SAMP}$  was reduced to 1 nF to achieve  $\tau = 70$  ns,  $f_{EH}$  was set to 2 Hz ( $T_{EH} = 500$  ms), and  $r_M$  was varied from 1/4 to 1/80, so  $f_{MPPT}$  was varied from 8 to 160 Hz (i.e.,  $T_{MPPT}$  from 125 ms to 6.25 ms).

A first test was performed with  $r_S = 0.1\%$ , so  $t_{SAMP}$  was correspondingly varied from 125 to 6.25  $\mu$ s. Fig. 7 shows a 2 s interval of  $V_{GEN}$  for four cases of  $1/r_M$ . As  $1/r_M$  increases ( $T_{MPPT}$  decreases and  $f_{MPPT}$  increases),  $V_{GEN}$  better follows the sinusoidal shape of  $V_{OC}/2$ . Fig. 8 (left-hand side) shows the measured  $P_{IN}$  (dashed line) normalized to  $P_{MPP}$  (8.86 mW) as well the analytical results from (3) (solid line) normalized to  $P_{MAX}$  [8.92 mW using (4)], as shown in Fig. 2 from Section II-B. This different normalization compensates for the small error in the piecewise quadratic approximation. As can be seen, there is an excellent match between the analytical and experimental results, which validates the model presented in the appendix and (3). Power rises to a maximum as  $r_M$  decreases ( $f_{MPPT}$  increases). Since the drained power through  $R_Z$  during  $t_{SAMP}$  is negligible (just  $r_S = 0.1\%$ ),  $P_{IN}$ , which includes it, was used for the experimental results and  $r_S = 0$  was considered for the analytical results in (3).

A second test was performed using  $r_S r_M = \frac{t_{SAMP}}{T_{EH}} = 10^{-3}$ , so  $t_{SAMP} = 500 \mu$ s. So, decreasing  $r_M$  increases  $r_S$  and, thus, the percentage of time sampling without harvesting energy from the EH source. As before, Fig. 8 (right-hand side) shows the normalized measured (dashed line) and analytical results (solid line). Since in this case, the wasted power across  $R_Z$

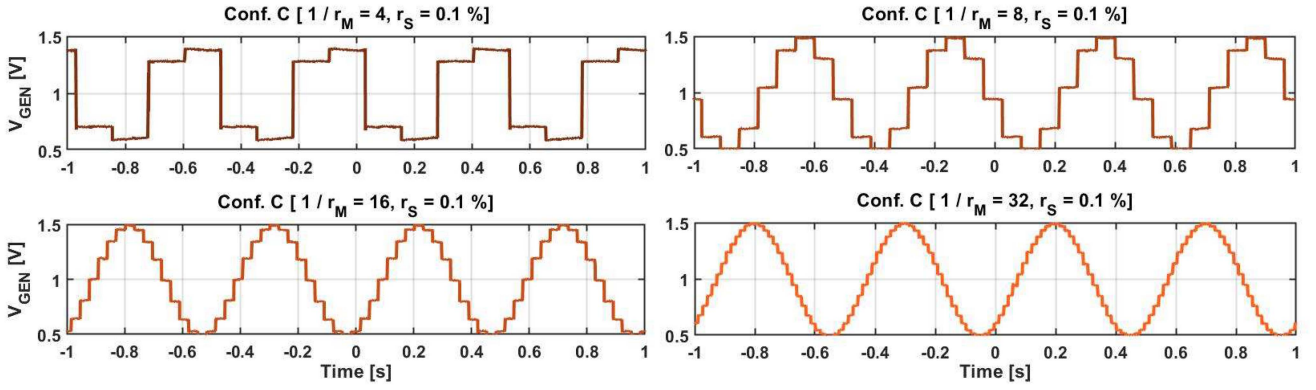


Fig. 7. Acquired  $V_{GEN}$  during 2 s in config. C for  $1/r_M = 4, 8, 16,$  and  $32$ . All four cases belong to scenario one, where  $T_{EH} = 2$  Hz,  $V_{OC} = 1-3$  V, and  $r_S = 0.1\%$ .

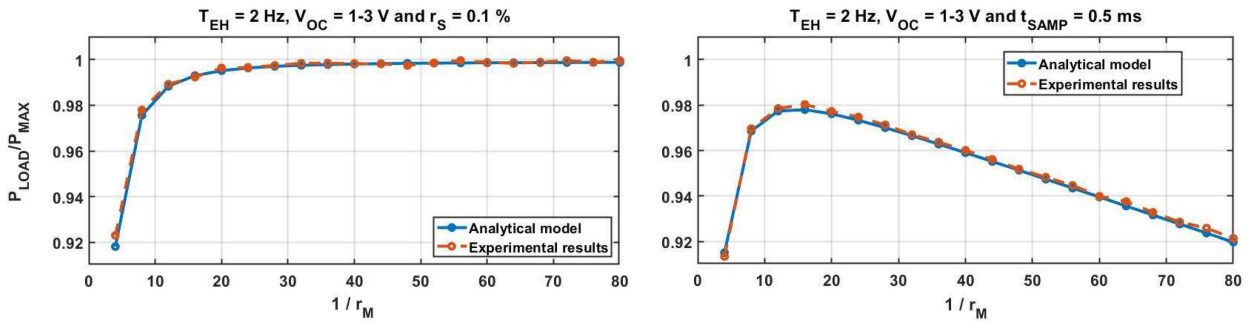


Fig. 8. Normalized harvested power versus  $1/r_M$  with config. C for two sampling scenarios according to analytical approximation in (3) (solid line) and experimental results (dashed line). At the left-hand side,  $r_S = 0.1\%$ , and at the right-hand side,  $r_S r_M = 10^{-3}$ .

during sampling is not negligible ( $r_S$  up to 8% for  $r_M = 1/80$ ),  $P_{OUT}/\eta$  has been used instead  $P_{IN}$  for the experimental results; otherwise, the losses during the sampling time would not be discounted. The mean  $\eta$  obtained in the first test ( $= 87.9\%$ ) was used. The analytical results also discount the losses ( $r_S \neq 0$ ). Again, theoretical and experimental results greatly match. As before, increasing  $1/r_M$  ( $f_{MPPT}$  increasing) increases the normalized power but in this case  $r_S$  also increases, which increases the time percentage sampling and, thus, the losses. Thus, a tradeoff exists and an optimum value of  $r_M$  exists which leads to a maximum value of the normalized power. For  $r_M < 1/20$ , the normalized power loss is  $r_S$ .

### C. WEC Test

Fig. 9 (right-hand side) shows the WEC presented in [17] with the description of the different parts. It consists of a double pendulum containing an arm with a proof mass guaranteeing the alignment of the main body with the wave's direction. The arm is articulated to a ring (main body) which is in turn articulated to the drifter, so it participates in the ring oscillation relative to the drifter. A gear train is coupled to the ring. Through that train, energy is accumulated in a flywheel that drives a dc electrical generator.

The left-hand side of Fig. 9 shows the experimental setup of this section. A linear shaker (APS 129) with controllable motion was used to emulate the drifter's movement under a sea

environment. The WEC was attached to the shaker's moving platform with the device's pendulum aligned to the movement axis. An FG provided a sinusoidal wave used to control the shaker's acceleration amplitude and frequency, set at 2 Hz. The Arduino-based EH monitoring system presented in [17], which includes an inertial measurement unit, was used to measure the acceleration of the platform and tune the FG to achieve an acceleration with peak-to-peak amplitude of 0.4 g, similar to that reported in [4] from a drifter under sea-wave excitation. The WEC's output was connected to the PMU. Two PMU configurations were used for this test: configs. R and C with  $f_{MPPT} = 60$  Hz ( $r_M = 1/30$ ) and  $r_S = 0.1\%$ .

Fig. 10 presents the experimental results of  $V_{GEN}$  and  $P_{OUT}$  using configs. C (left-hand side) and R (right-hand side), with a zoom-in window of 4 and 16 s (one sampling period for config R), respectively. The averaged  $P_{OUT}$  is also plotted. The WEC's  $V_{OC}$  signal under this test excitation was also measured (not shown) and had a sinusoidal-shape with  $V_{DC}$  around 2 V and  $V_{AC}$  around 1 V.

Fig. 10 (left-hand side) shows how config. C closely follows the MPP every  $1/60$  ms.  $V_{GEN}$  has sinusoidal-shape in concordance with the shaker's acceleration, as happened in [5], with a value between 0.5 and 1.5 V ( $V_{OC} = 1-3$  V). In this case,  $V_{GEN}$  does not rise to  $V_{OC}$  for each sample due to the presence of  $R_Z$ .  $P_{OUT}$  presents a square sinusoidal-shape following the pendulum's back-and-forward motion. Thanks to the flywheel that keeps the generator rotating,  $P_{OUT}$  has a positive offset.

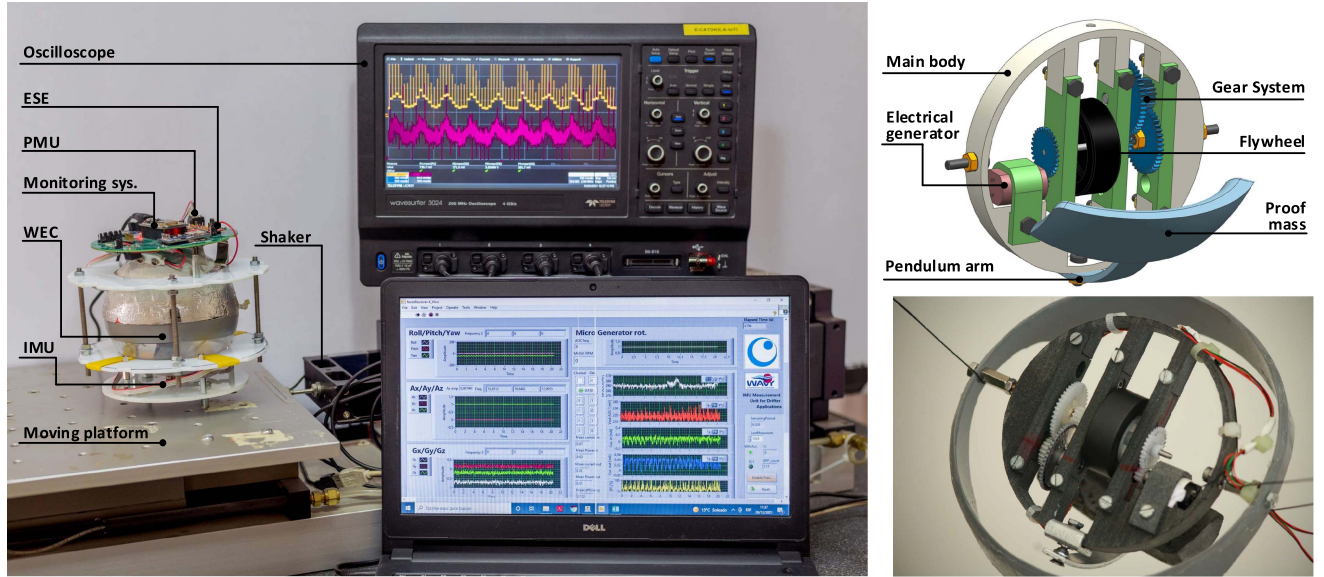


Fig. 9. Experimental setup for the WEC test. Left-hand side: linear shaker (APS 129) with the WEC attached to the moving platform. Also shown are the PMU, the Arduino-based system and monitoring (PC), and the measuring oscilloscope. Top-right: architecture of the WEC proposed in [4] with the description of the different parts. Bottom-right: prototype of the double pendulum WEC device.

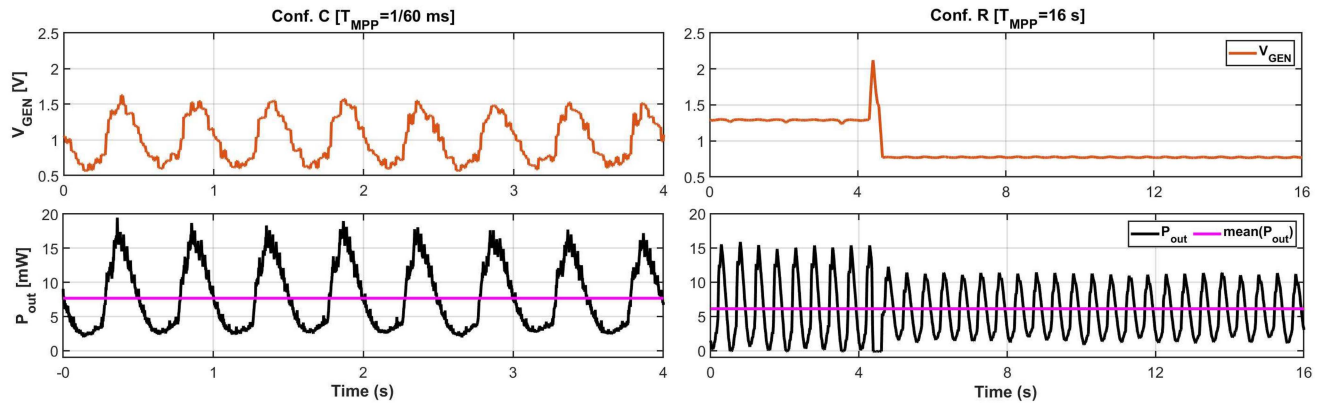


Fig. 10. Experimental results for the WEC test. Left-hand side: config. C with  $T_{MPPT} = 1/60$  ms. Right-hand side: config. R. with  $T_{MPPT} = 16$  s.  $V_{GEN}$  (top),  $P_{OUT}$  (bottom solid lines), and the average of  $P_{OUT}$  (bottom dashed lines) are represented.

TABLE IV  
COMPARISON RESULTS OF THE EMULATED WAVE EXCITATION TEST USING THE LINEAR SHAKER

Config.	$T_{MPPT}$ (ms)	$V_{GEN}$ (V)	$P_{IN}$ (mW)	$P_{OUT}$ (mW)	Eff. (%)
C	1/60	1.00	8.66	7.68	88.7
R	16k	1.08	6.93	6.11	88.2

$V_{GEN}$ ,  $P_{IN}$ , and  $P_{OUT}$ : Mean values.

Fig. 10 (right-hand side) shows how config. R only samples  $V_{OC}$  once every 16 s so just one sampling event can be seen. Before and after the sampling event,  $V_{MPP}$  is fixed to 1.3 and 0.8 V, respectively, but could be anywhere between 0.5 and 1.5 V. Anyhow,  $V_{MPP}$  is not achieved since  $T_{MPPT}$  and, thus  $r_M$ , is too large ( $r_M = 32$ ).

Table IV tabulates the averaged  $V_{GEN}$ ,  $P_{IN}$ , and  $P_{OUT}$  values, as well as the PMU global efficiency.  $P_{OUT}$  is 7.68 and 6.11 mW for configs. C and R, respectively. Config. C improves  $P_{OUT}$  by 25%, harvesting an additional 1.57 mW under the same excitation conditions. This percentage matches with [5], where the WEC was placed at the shaker with similar excitation and the fast tracking was emulated by providing an external sinusoidal  $V_{MPP}$  to the PMU's CBP pin that approached half the measured  $V_{OC}$ . There, the benefit of fast sampling was shown but without the analytical study, proposed circuits, and experimental results that this work provides.

## VI. CONCLUSION

The advantages and limitations of increasing the sampling rate in FOCV-MPPT circuits for low-power fast-varying EH sources

have been assessed. First, the analytical expressions to optimize the sampling parameters have been provided. Second, the limitations of implementing a fast-sampling FOCV-MPPT circuit have been analyzed and some solutions proposed, resulting in three new configurations, one of them being a novel pseudoFOCV method. In addition, this circuit achieves the fastest sampling rate by large among the reported works.

A first test has been performed using a 1.8-Hz, 1 to 3-V sinusoidal signal with an output resistance of 127  $\Omega$ . The three proposed configurations achieved a similar performance and improved by more than 20% the harvested energy with respect to a commercial FOCV-PMU with a low sampling rate. A second test has been performed with the novel pseudoFOCV circuit showing that 1) the harvested power increases with the sampling rate for negligible sampling time (sampling 15 times faster than the source frequency extracts around 99% of the maximum), and 2) for a fixed sampling time, there is an optimum sampling rate where the harvested power is maximum. The first result is also valid for methods other than the FOCV. The experimental and analytical results show very good agreement. Finally, a small-scale WEC prototype has been placed on a linear shaker to emulate the drifter's movement under a sea environment. Results have shown that the proposed configuration improves by 25% the harvested energy from the WEC with respect to the commercial PMU.

#### APPENDIX

This appendix outlines the derivation of (3), which is an analytical approximation for the power extracted from a sinusoidally varying EH source by a PMU employing FOCV MPPT. The source is taken to have a constant series output resistance  $R_G$  and an open-circuit voltage defined as (1). The following assumptions are made to simplify the analysis:

- 1) each quarter period of oscillation contains exactly  $N$  MPPT updates, i.e.,  $T_{EH} = 4NT_{MPPT}$ , where  $N$  is a positive integer;
- 2) the first MPPT update in each quarter cycle occurs at the start of the quarter cycle, i.e., at the zero-crossing or peak.

It is convenient also to replace the sinusoidal part of  $V_{OC}$  by a piecewise quadratic approximation as this allows a closed-form solution to be obtained more easily. The following form will be used to cover the time interval  $0 \leq t < T_{EH}$ :

$$V_{OC}(t) = \begin{cases} V_{dc} + V_{ac} [1 - (1 - \mu)^2] & \mu = \frac{4t}{T_{EH}}; 0 \leq t < \frac{T_{EH}}{4} \\ V_{dc} + V_{ac} [1 - \mu^2] & \mu = \frac{4t}{T_{EH}} - 1; \frac{T_{EH}}{4} \leq t < \frac{T_{EH}}{2} \\ V_{dc} - V_{ac} [1 - (1 - \mu)^2] & \mu = \frac{4t}{T_{EH}} - 2; \frac{T_{EH}}{2} \leq t < \frac{3T_{EH}}{4} \\ V_{dc} - V_{ac} [1 - \mu^2] & \mu = \frac{4t}{T_{EH}} - 3; \frac{3T_{EH}}{4} \leq t < T_{EH}. \end{cases} \quad (7)$$

The approximation in (7) is exact at the zero crossings and peaks and has a continuous first derivative. The maximum deviation from the true sinusoidal form is  $0.056V_{ac}$ .

#### A. Average Extracted Power When $t_{SAMP} \rightarrow 0$

For any given  $V_{OC}$  waveform, the average power delivered to the PMU by an energy harvester with a constant series output resistance  $R_G$  is given by

$$P = \frac{\overline{[V_{OC}(t) - V_{GEN}(t)] V_{GEN}(t)}}{R_G} \quad (8)$$

where overbar denotes a time average over the interval of interest. If  $V_{GEN}$  is derived by the FOCV-MPPT method, with samples being taken at times  $t_n = nT_{MPPT}$ ;  $n \in \mathbb{Z}$ , then we can recast (8) as follows:

$$\langle P_n \rangle = \left\langle \frac{1}{T_{MPPT}} \int_{t_n + t_{SAMP}}^{t_n + T_{MPPT}} \left[ V_{OC}(t) - \frac{V_{OC}(t_n)}{2} \right] \frac{V_{OC}(t_n)}{2R_G} dt \right\rangle \quad (9)$$

where  $P_n$  is the average output power over the  $n$ th sampling interval,  $t_n \leq t < t_{n+1}$ , and  $\langle P_n \rangle$  is the arithmetic mean of the  $P_n$  values over the time interval of interest. Note that in (9), it is assumed that any deviation of  $V_{GEN}$  from the value at the start of the sampling interval is negligible; this is a good assumption as  $t_{SAMP}$  is small compared with the EH oscillation period  $T_{EH}$ .

Then, we continue by considering the average power extracted over the first quadrant or quarter-cycle in the limit where the MPPT sampling time is negligible. According to the simplifying assumptions, MPPT sampling will occur at the discrete times  $t_n = nT_{MPPT}$ , where  $n = \{0, 1, 2, \dots, (N-1)\}$ , and the corresponding values of  $\mu$  from (7) will be  $\mu_n = \frac{4nT_{MPPT}}{T_{EH}} = \frac{n}{N}$ . We can, therefore, express the source voltage in the  $n$ th MPPT interval (i.e., the time interval  $t_n \leq t < t_{n+1}$ ) as follows:

$$V_{OC}(nT_{MPPT} + \sigma T_{MPPT}) = V_{dc} + V_{ac} \left[ 1 - \left( 1 - \frac{n}{N} - \frac{\sigma}{N} \right)^2 \right] \quad 0 \leq \sigma < 1. \quad (10)$$

Now, at the start of the  $n$ th MPPT interval, the EH output voltage (also the PMU input voltage) is set to  $\frac{V_{OC}(nT_{MPPT})}{2}$  and it remains at this level until the next update. The instantaneous extracted power during the  $n$ th MPPT interval is, therefore, as follows:

$$P_{1n} = \frac{V_{dc} + V_{ac} \left[ 1 - \left( 1 - \frac{n}{N} \right)^2 \right]}{2R_G} \left\{ V_{dc} + V_{ac} \left[ 1 - \left( 1 - \frac{n}{N} - \frac{\sigma}{N} \right)^2 \right] - \frac{V_{dc} + V_{ac} \left[ 1 - \left( 1 - \frac{n}{N} \right)^2 \right]}{2} \right\} \\ = \frac{V_{dc} + V_{ac} \left[ 1 - \left( 1 - \frac{n}{N} \right)^2 \right]}{2R_G} \left\{ \frac{V_{dc}}{2} + \frac{V_{ac}}{2} \left[ 1 + \left( 1 - \frac{n}{N} \right)^2 \right] - V_{ac} \left( 1 - \frac{n}{N} - \frac{\sigma}{N} \right)^2 \right\}. \quad (11)$$

The average extracted power over the  $n^{\text{th}}$  MPPT interval is then obtained as follows:

$$\begin{aligned} \overline{P_{1n}} &= \int_0^1 P_{1n} d\sigma \\ &= \frac{V_{dc} + V_{ac} \left[ 1 - \left( 1 - \frac{n}{N} \right)^2 \right]}{2R_G} \left\{ \frac{V_{dc}}{2} + \frac{V_{ac}}{2} \left[ 1 + \left( 1 - \frac{n}{N} \right)^2 \right] \right. \\ &\quad \left. + \frac{NV_{ac}}{3} \left( 1 - \frac{n}{N} - \frac{1}{N} \right)^3 - \frac{NV_{ac}}{3} \left( 1 - \frac{n}{N} \right)^3 \right\} \end{aligned} \quad (12)$$

which, after some manipulation, can be recast as follows:

$$\begin{aligned} \overline{P_{1n}} &= \frac{V_{dc}^2}{4R_G} + \frac{V_{dc}V_{ac}}{R_G} \left\{ \frac{1}{2} - \frac{1}{6N^2} + \frac{\left( 1 - \frac{n}{N} \right)}{2N} - \frac{\left( 1 - \frac{n}{N} \right)^2}{2} \right\} \\ &\quad + \frac{V_{ac}^2}{R_G} \left\{ \frac{1}{4} - \frac{1}{6N^2} + \frac{\left( 1 - \frac{n}{N} \right)}{2N} \right. \\ &\quad \left. - \left( \frac{1}{2} - \frac{1}{6N^2} \right) \left( 1 - \frac{n}{N} \right)^2 - \frac{\left( 1 - \frac{n}{N} \right)^3}{2N} + \frac{\left( 1 - \frac{n}{N} \right)^4}{4} \right\}. \end{aligned} \quad (13)$$

The average extracted power over the first quadrant can now be obtained by averaging the  $N$  values of  $\overline{P_{1n}}$  corresponding to  $n = \{0, 1, 2, \dots, (N-1)\}$ . Here, we can make use of the standard results for sums of powers [19]. In particular, if  $\langle \rangle$  denotes the arithmetic mean then

$$\left\langle \left( 1 - \frac{n}{N} \right) \right\rangle = 1 - \frac{1}{N^2} \sum_0^{N-1} n = 1 - \frac{N-1}{2N} = \frac{N+1}{2N} \quad (14)$$

$$\left\langle \left( 1 - \frac{n}{N} \right)^2 \right\rangle = \frac{(N+1)(2N+1)}{6N^2} \quad (15)$$

$$\left\langle \left( 1 - \frac{n}{N} \right)^3 \right\rangle = \frac{(N+1)^2}{4N^2} \quad (16)$$

$$\left\langle \left( 1 - \frac{n}{N} \right)^4 \right\rangle = \frac{(N+1)(2N+1)(3N^2+3N-1)}{30N^4}. \quad (17)$$

Replacing each term of the form  $\left( 1 - \frac{n}{N} \right)^m$  in (13) by its mean value from (14)–(17), and after some simplification, the average extracted power over the first quadrant is obtained as follows:

$$\overline{P_1} = \frac{V_{dc}^2}{4R_G} + \frac{V_{dc}V_{ac}}{3R_G} + \frac{V_{ac}^2}{R_G} \left\{ \frac{2}{15} - \frac{1}{9N^2} - \frac{1}{24N^3} + \frac{7}{360N^4} \right\}. \quad (18)$$

If the preceding steps are repeated for the other three quadrants, similar results are obtained but with some changes of sign. The results for all four quadrants are encapsulated by the following expression:

$$\begin{aligned} \overline{P}_q &= \frac{V_{dc}^2}{4R_G} - \frac{(-1)^{\text{md}(\frac{q}{2})} V_{dc}V_{ac}}{3R_G} + \frac{V_{ac}^2}{R_G} \\ &\quad \times \left\{ \frac{2}{15} - \frac{1}{9N^2} + \frac{(-1)^q}{24N^3} + \frac{7}{360N^4} \right\} \end{aligned} \quad (19)$$

where  $q$  represents the quadrant number and  $\text{rnd}()$  denotes rounding to the nearest integer.

Finally, the overall average extracted power is obtained as the arithmetic mean of the four quadrant averages. This gives the following:

$$\overline{P} = \frac{V_{dc}^2}{4R_G} + \frac{V_{ac}^2}{R_G} \left\{ \frac{2}{15} - \frac{1}{9N^2} + \frac{7}{360N^4} \right\}. \quad (20)$$

We note that  $\overline{P}$  increases monotonically with  $N$ , which is as expected if the sampling time is negligible. The maximum value of  $\overline{P}$ , approached as  $N \rightarrow \infty$ , corresponds to ideal MPP tracking and is given by

$$\max \{ \overline{P} \} = \frac{V_{dc}^2}{4R_G} + \frac{2}{15} \frac{V_{ac}^2}{R_G}. \quad (21)$$

This result [equivalent to (4) using  $\alpha$  and  $P_{dc}$ ] is slightly different from the standard result for an offset sinusoidal source given by (2) in the main text because of the piecewise quadratic approximation used here.

### B. Effect of Finite Sampling Time

In practice, the sampling time  $t_{\text{SAMP}}$  is finite, and in FOCV MPPT, no power is delivered to the load during sampling. If we assume that  $t_{\text{SAMP}} \ll T_{\text{EH}}$ , then we can take the source voltage to be constant during sampling. Also, since sampling coincides with setting the output voltage to  $V_{\text{MPP}}$ , we can assume that the load presented by the PMU would have been perfectly matched during the sampling interval, and would remained connected. With these assumptions, the energy forfeited during the  $n$ th sampling event in the first quadrant will be

$$\begin{aligned} U_{1n} &= t_{\text{SAMP}} \frac{V_{\text{OC}}^2(nT_M)}{4R_G} = t_{\text{SAMP}} \frac{\left\{ V_{dc} + V_{ac} \left[ 1 - \left( 1 - \frac{n}{N} \right)^2 \right] \right\}^2}{4R_G} \\ &= t_{\text{SAMP}} \left\{ \frac{V_{dc}^2}{4R_G} + \frac{V_{dc}V_{ac}}{2R_G} \left[ 1 - \left( 1 - \frac{n}{N} \right)^2 \right] \right. \\ &\quad \left. + \frac{V_{ac}^2}{4R_G} \left[ 1 - 2 \left( 1 - \frac{n}{N} \right)^2 + \left( 1 - \frac{n}{N} \right)^4 \right] \right\}. \end{aligned} \quad (22)$$

The resulting loss in average power over the first quadrant is

$$\overline{L}_1 = \frac{4}{T_{\text{EH}}} N U_{1n} = r_S \left\langle \frac{U_{1n}}{t_{\text{SAMP}}} \right\rangle. \quad (23)$$

Replacing each term of the form  $\left( 1 - \frac{n}{N} \right)^m$  in (22) by its mean value from (14)–(17), and after some simplification, (23) can be recast as

$$\begin{aligned} \overline{L}_1 &= r_S \left\{ \frac{V_{\text{DC}}^2}{4R_G} + \frac{V_{\text{DC}}V_{\text{AC}}}{R_G} \left[ \frac{1}{3} - \frac{1}{4N} - \frac{1}{12N^2} \right] \right. \\ &\quad \left. + \frac{V_{\text{AC}}^2}{R_G} \left[ \frac{2}{15} - \frac{1}{8N} - \frac{1}{120N^4} \right] \right\}. \end{aligned} \quad (24)$$

Repeating the previous analysis for the other three quadrants gives similar results with some sign changes, and the results for

all four quadrants are encapsulated by the following expression:

$$\bar{L}_q = r_S \left\{ \frac{V_{DC}^2}{4R_G} - \frac{(-1)^{\text{nd}(\frac{q}{2})} V_{DC} V_{AC}}{R_G} \left[ \frac{1}{3} + \frac{1}{4N} - \frac{1}{12N^2} \right] + \frac{V_{AC}^2}{R_G} \left[ \frac{2}{15} + \frac{(-1)^q}{8N} - \frac{1}{120N^4} \right] \right\}. \quad (25)$$

The overall loss of average extracted power due to sampling is obtained by evaluating the arithmetic mean of the four quadrant averages. This gives the following:

$$\bar{L} = r_S \left\{ \frac{V_{DC}^2}{4R_G} + \frac{V_{AC}^2}{R_G} \left[ \frac{2}{15} - \frac{1}{120N^4} \right] \right\}. \quad (26)$$

Combining (20) and (26), the average power extracted by the PMU when the sampling time is finite is

$$P_{LOAD} \approx \bar{P} - \bar{L} = \left[ \frac{V_{DC}^2}{4R_G} + \frac{2V_{AC}^2}{15R_G} \right] (1 - r_S) - \left[ \frac{V_{AC}^2}{9R_G} \right] \frac{1}{N^2} + \left[ \frac{V_{AC}^2}{R_G} \left( \frac{7 + 3r_S}{360} \right) \right] \frac{1}{N^4}. \quad (27)$$

Using the substitutions  $P_{DC} = \frac{V_{DC}^2}{4R_G}$ ,  $r_M = \frac{1}{4N}$ , and  $\alpha = \frac{V_{AC}}{V_{DC}}$ , the expression given in (3) is obtained. The value of  $P_{LOAD}$  given by (27) is exact for the waveform described by (7) in the limit as  $t_{SAMP} \rightarrow 0$ .

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