

# An Input-Oriented Power Sharing Control Scheme With Fast-Dynamic Response for ISOP DAB DC–DC Converter

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**Abstract**—With some advantages, such as electric isolation, high efficiency, and fast dynamic response, the input-series output-parallel (ISOP) dual-active-bridge (DAB) dc–dc converter has been regarded as one of the most promising candidates for connecting the medium voltage terminal and the low voltage terminal. For the ISOP DAB dc–dc converter, the existing control strategies are mainly focusing on the equivalent power sharing control, but the fast-dynamic response is not included and the decoupling between the regulation of input voltage and the adjustment of output voltage is not eliminated significantly. In this article, the average model of this ISOP DAB dc–dc converter is presented first, which can be employed to analyze the power distributions of this modular topology clearly. Then, an input-oriented power sharing control scheme with fast-dynamic response is proposed for ensuring both the power sharing ability and the fast-dynamic performance of the ISOP DAB dc–dc converter in this article. Compared with the existing methods, this proposed scheme can also significantly reduce the coupling between the power sharing control and the output voltage regulation. In addition, an inductance-estimating method is proposed for ensuring the power sharing performance of the ISOP DAB dc–dc converter. Finally, the experimental results are provided to verify the effectiveness of the proposed input-oriented power sharing control with fast-dynamic response for the ISOP DAB dc–dc converter system.

**Index Terms**—Average model, fast-dynamic response, input-series output-parallel (ISOP) dual-active-bridge (DAB) converter, power balancing control.

## I. INTRODUCTION

HIGH-VOLTAGE dc converter systems with large voltage turn ratio are extensively used in some power electronic applications, such as rail transit system, energy storage system,

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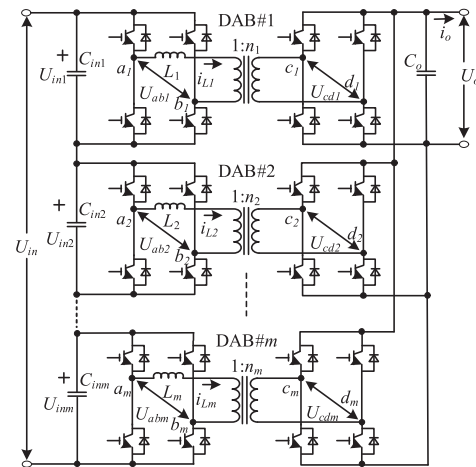


Fig. 1. Topology of the ISOP DAB dc–dc converter system.

and microgrids [1]–[5]. Then, based on input-series output-parallel (ISOP) structure, the power electronic transformers with electric isolation become a promising candidate for connecting the medium/high voltage dc and the low voltage dc in these converter systems [6], [7]. Generally, compared with other isolated dc–dc converters, the dual-active-bridge (DAB) is more suitable for high power applications with high efficiency, bidirectional operation, and fault isolation [8], [9]. So, this article mainly focuses on the ISOP DAB dc–dc converter as shown in Fig. 1 for uninterrupted power supply.

With equivalent power sharing control for ISOP converter system, the equivalent utilization of components can be ensured, and the overvoltage overcurrent issues can be avoided for each converter module [10]. Traditionally, the common duty-ratio operation can be employed to realize power balance performance in parallel/series dc–dc converter system [11], [12], which can significantly reduce the design cost of the controller system. However, the power balance performance is sensitive to the parameter mismatch, especially for the DAB type converter, and the transient process may result in instability under common duty ratio control [13], [14].

To realize positive power sharing control operation, there are two main ways to realize the power balance control for

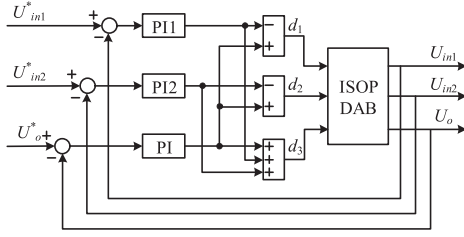


Fig. 2. Traditional decoupling compensation structure for the ISOP DAB dc-dc converter system with three modules [26], [27].

the ISOP dc-dc converter including the positive input-voltage control scheme [15]–[18] and the positive transferred-current control scheme [19]–[23]. For the positive input-voltage control scheme, these existing control strategies can be divided into two groups including the input voltage direct control [15], [16] and the input-voltage droop control [17], [18]. Moreover, for the positive transferred-current control scheme, there are also two categories including the transferred-current direct control [19] and the transferred-current droop control [22], [23]. In [15], a simple sensorless current mode control scheme is proposed for guaranteeing stable sharing performance of the ISOP dc-dc converter system. Similarly, based on the same outer control structure, an input voltage sharing control method is proposed for the ISOP forward dc-dc converter system [16], and the equivalent input voltages can be obtained. For modular converter systems, the droop control concept is also a potential candidate for realizing the power balance performance. Based on the droop structure, a wireless input voltage sharing control method is proposed for the isolated dc-dc converter [17], and a similar decentralized control method is proposed for ISOP DAB dc-dc converter system. Moreover, by directly controlling the transferred current, the power balance operation can be realized, but the converter system prefers to be unstable with the negative resistance model [24]. So, a transferred-current differential control scheme is proposed to address this issue [19]. Furthermore, the transferred-current droop control method can be employed to achieve the power balance control for the ISOP dc-dc converter [22]. A decentralized inverse-droop control method is proposed for balancing power sharing of the ISOP isolated dc-dc converter [23].

Since the transferred current of the DAB dc-dc converter contains the ac current, the transferred-current-based control should be not suitable. Moreover, the droop-based control scheme usually results in poor dynamic and steady-state performances [25]. So, the input-voltage direct control may be the most suitable control for the ISOP DAB dc-dc converter [15], [16], but the decoupling between the regulation of input voltage and the adjustment of output voltage in the traditional ways may result in a bad transient process. So, a novel input voltage sharing control is proposed to decouple the input voltage with the output voltage regulation as shown in Fig. 2 [26], [27]. However, since the PI controller for adjusting the input voltage of the first two modules is employed to determine the phase-shift ratio not the transferred power, the influence on the output voltage is also obvious. In addition, these existing strategies are more focusing on the

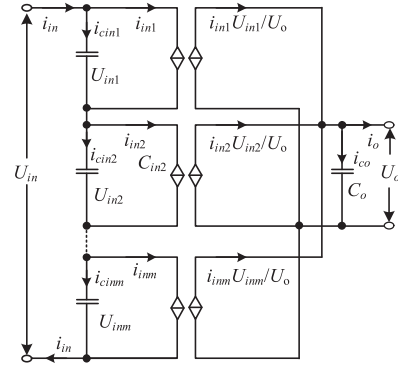


Fig. 3. Simplified circuit of the ISOP DAB dc-dc converter system.

power sharing performance, and the fast-dynamic response for the ISOP DAB dc-dc converter is not studied for dealing with the disturbances of the input voltage and the load current.

Therefore, a novel input-oriented power sharing control method with fast-dynamic response is proposed for the ISOP DAB dc-dc converter system in this article, which can be employed to adjust the input voltages of different modules flexibly for required power sharing performance and maintain the output voltage when the input voltage and load resistor are changed.

The rest of this article is organized as follows. The average model of this ISOP DAB dc-dc converter is demonstrated in Section II. Then, in Section III, combining a minimum-current-stress (MCS) modulation method, the novel power sharing control scheme with fast-dynamic response is proposed. Moreover, an inductance-estimating method is proposed for ensuring the power sharing performance of the ISOP DAB dc-dc converter. In addition, based on experimental results, the effectiveness of the proposed input-oriented power sharing control scheme with fast-dynamic response is verified in Section IV. Finally, Section V concludes this article.

## II. AVERAGE MODEL OF THE ISOP DAB DC-DC CONVERTER SYSTEM

In this section, the average model of the ISOP DAB dc-dc converter system as shown in Fig. 1 will be presented. Then, the current distributions on both the primary side and the secondary side will be demonstrated, which can be employed to analyze the coupling relationship between the adjustment of the input voltages and the output voltage.

### A. Average Model of the ISOP DAB DC-DC Converter

Traditionally, the inductance of the dc-dc converter, such as buck converter and boost converter plays an important role in the modeling analysis. Nevertheless, since the transferred current of the DAB dc-dc converter can be determined by the circuit parameter and the phase-shift ratio, the middle ac inductance can be neglectful [28], [29]. Then, the simplified circuit of the ISOP DAB dc-dc converter system can be shown in Fig. 3, where the input-side current and the output-side current can be modeled as controllable current source.

According to Fig. 3, the average model of the ISOP DAB dc–dc converter can be expressed as

$$\begin{cases} C_{inX} \frac{dU_{inX}}{dt} = i_{in} - i_{inX} \\ C_o \frac{dU_o}{dt} = \sum_{\alpha=1}^m \frac{i_{inX} U_{inX}}{U_o} - i_o \end{cases} \quad (X \in [1, m]). \quad (1)$$

Then, the small-signal model of this ISOP DAB dc–dc converter can be expressed as

$$\begin{cases} C_{inX} \frac{d\hat{U}_{inX}}{dt} = \hat{i}_{in} - \hat{i}_{inX} \\ C_o \frac{d\hat{U}_o}{dt} = \sum_{X=1}^m \frac{\hat{i}_{inX} U_{inX}}{U_o} + \sum_{X=1}^m \frac{i_{inX} \hat{U}_{inX}}{U_o} - \hat{i}_o \end{cases} \quad (X \in [1, m]). \quad (2)$$

According to (1), since the total disturbances of the input voltage for each DAB module should be zero, the input current  $i_{in}$  can be expressed as

$$i_{in} = \frac{\sum_{X=1}^m \frac{i_{inX}}{C_{inX}}}{\sum_{X=1}^m \frac{1}{C_{inX}}} = \frac{\sum_{X=1}^m i_{inX}}{m} \Big|_{\text{same input capacitors}}. \quad (3)$$

In (3), when the ISOP DAB dc–dc converter is at steady-state condition, the transferred current for each DAB module  $i_{inX}$  should be equivalent to the input current  $i_{in}$ .

### B. Inherent Coupling Phenomenon Between Regulations of Input Voltages and Output Voltage

Then, assuming the input capacitors are the same, when a variation  $\Delta i_{inH}$  is added to the  $H$ th DAB module for adjusting its input voltage, the input voltage  $i_{in}$  can be expressed as

$$i_{in} = \frac{\sum_{X=1}^m i_{inX} + \Delta i_{inH}}{m} = i'_{in} + \frac{\Delta i_{inH}}{m}. \quad (4)$$

where  $i'_{in}$  is the required input current for the load side at steady-state condition. Then, the capacitor charging current  $i_{cinX}$  for each DAB module can be expressed as

$$\begin{cases} i_{cinH} = -\frac{m-1}{m} \Delta i_{cinH} \\ i_{cinX} = \frac{1}{m} \Delta i_{cinH} \end{cases} \quad (X \neq H). \quad (5)$$

On this condition, the transferred current to the output side can be calculated as

$$\begin{aligned} \sum_{X=1}^m \frac{i_{inX} U_{inX}}{U_o} &= \sum_{X=1}^m \frac{i'_{in} U_{inX}}{U_o} + \frac{\Delta i_{inH} U_{inH}}{U_o} \\ &= U_o i_o + \frac{\Delta i_{inH} U_{inH}}{U_o}. \end{aligned} \quad (6)$$

According to (6), the charging current of the output capacitor  $i_{co}$  can be calculated as

$$i_{co} = \frac{\Delta i_{inH} U_{inH}}{U_o}. \quad (7)$$

Then, the output voltage will be not stable since the charging current of the output capacitor is not zero. Moreover, when all input voltages  $U_{inX}$  should be adjusted positively for the desired power sharing performance, the variation  $\Delta i_{inX}$  for each DAB module can be expressed as

$$\Delta i_{inX} = C_X \Delta U_{inX} \quad \left( \sum_{X=1}^m \Delta U_{inX} = 0 \right). \quad (8)$$

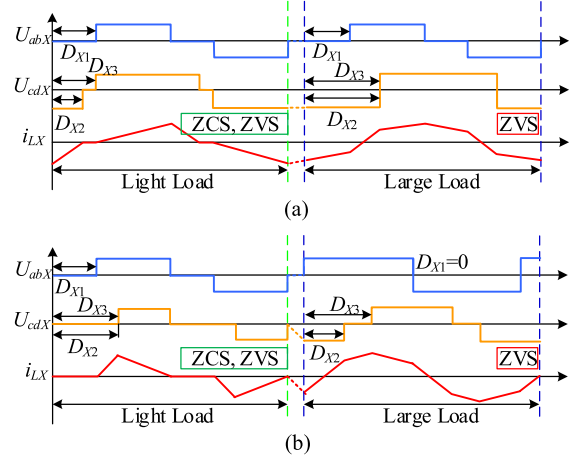


Fig. 4. MCS modulation method under different voltage conditions. (a) Phase-shift modulation methods when  $k > l$ . (b) Phase-shift modulation methods when  $k < l$ .

Assuming the input capacitors are the same, the sum of the transferred current variations can be expressed as

$$\sum_{X=1}^m \Delta i_{inX} = 0. \quad (9)$$

According to (3) and (9), the input current  $i_{in}$  will not be changed. Then, combining Fig. 3 and (6), the charging current  $i_{co}$  of the output capacitor can be expressed as

$$i_{co} = \sum_{X=1}^m \frac{\Delta i_{inX} U_{inX}}{U_o} \neq 0 \quad \left( \sum_{X=1}^m \Delta i_{inX} = 0 \right). \quad (10)$$

During the transient process for adjusting the input voltages, the input voltages  $U_{inX}$  for each DAB module are usually not the same, so the charging current for the output capacitor is not zero. Then, the disturbance of the output voltage is not evitable. In reverse, if  $i_{co}$  is forced to zero in (10), the disturbance of the output voltage can be omitted, but the sum of the transferred current variations cannot be zero. Then, the change of the input voltages  $U_{inX}$  will not be the same as the requirement. Therefore, in terms of adjusting the input voltages for each DAB module, the coupling of the regulation of the input voltages and the adjustment of the output voltage cannot be neglected.

## III. PROPOSED INPUT-ORIENTED POWER SHARING CONTROL SCHEME WITH FAST-DYNAMIC RESPONSE

In this section, the novel input-oriented power sharing control scheme with fast-dynamic response will be proposed for the ISOP DAB dc–dc converter. To reduce the power loss, an existing MCS modulation method is adopted [30]. Then, the proposed power sharing control scheme will be presented and analyzed, which can also provide fast-dynamic response when the input voltage and load resistor are changed.

### A. Minimum-Current-Stress Modulation Method

The waveforms of the MCS modulation method can be shown in Fig. 4, where  $D_{X1}$ – $D_{X3}$  are the phase-shift ratios. Based on

TABLE I  
OPTIMIZED SOLUTIONS OF MCSO STRATEGY UNDER DIFFERENT CONDITIONS

Voltage Conditions	Unified Transferred Current	Range of $i_{TX}$	Middle Variable	Phase-Shift Ratio
$k > 1$	$i_{TX} = \frac{8L_X I_{TX}}{n_X U_{inX} T_s}$	$0 \leq i_{TX} < 2\frac{k_X - 1}{k_X^2}$	$D_{X1} = 1 - \sqrt{\frac{i_{TX}}{2(k_X - 1)}}$	$\begin{cases} D_{X2} = (k_X - 1)(1 - D_{X1}) \\ D_{X3} = D_{X1} \end{cases}$
		$2\frac{k_X - 1}{k_X^2} \leq i_{TX} \leq 1$	$D_{X1} = (k_X - 1) \sqrt{\frac{1 - i_{TX}}{k_X^2 - 2k_X + 2}}$	$\begin{cases} D_{X2} = \frac{k_X - 2}{2(k_X - 1)} D_{X1} + \frac{1}{2} \\ D_{X3} = \frac{k_X - 2}{2(k_X - 1)} D_{X1} + \frac{1}{2} \end{cases}$
$k \leq 1$		$0 \leq i_{TX} < 2(k_X - k_X^2)$	$D_{X1} = 1 - \sqrt{\frac{i_{TX}}{2k_X(1 - k_X)}}$	$\begin{cases} D_{X2} = 0 \\ D_{X3} = k_X D_{X1} - k_X + 1 \end{cases}$
		$2(k_X - k_X^2) \leq i_{TX} \leq 1$	$D_{X2} = \frac{1}{2} \left( 1 - \sqrt{\frac{1 - i_{TX}}{2k_X^2 - 2k_X + 1}} \right)$	$\begin{cases} D_{X1} = 0 \\ D_{X3} = 2k_X D_{X2} - D_{X2} - k_X + 1 \end{cases}$

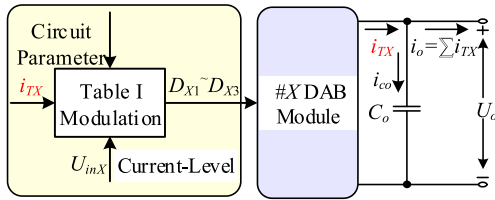


Fig. 5. Schematic of current-level modulation for the DAB dc-dc converter.

this modulation method, the soft switching performance can be obtained during the whole power range, and the minimum conduction power loss can also be achieved. Then, the corresponding phase-shift ratios  $D_{X1} - D_{X3}$  can be given from Table I, where  $I_{TX}$  is the transferred current,  $n_X$  is the transformer turn ratio,  $k_X$  is the voltage ratio as  $n_X U_{inX} / U_o$ , and  $L$  is the middle inductance of the  $X$ th DAB dc-dc module.

Compared with Fig. 3 and Table I, the transferred current  $I_{TX}$  can be expressed as

$$I_{TX} = \frac{i_{inX} U_{inX}}{U_o}. \quad (11)$$

Moreover, based on Table I, the current-level modulation operation can be realized, and the corresponding schematic can be shown in Fig. 5.

As shown in Fig. 5, if the transferred current  $I_{TX}$  is employed as the effective control value for the DAB dc-dc converter, the current-level modulation can be employed. Based on some existing modulation methods [30], the phase-shift ratios can be determined by the transferred current or power even during the transient process. Then, when the DAB converter is modeled, the underlying phase-shift ratios can be avoided, which can significantly simplify the modeling analysis about the DAB converter.

### B. Proposed Input-Oriented Power Sharing Control Method With Fast-Dynamic Response

According to (10), when the input voltages should be controlled positively, the influence on the output voltage is

unavoidable. So, to reduce this influence, the changes  $\Delta U_{inX}$  of each input voltage should be relatively small. Then, the charging current  $i_{cinX}$  for each input-side capacitor can be calculated as

$$i_{cinX} = \frac{\Delta U_{inX} C_{inX}}{T_s}. \quad (12)$$

Moreover, to deal with the disturbance of the load condition, the required output current for the ISOP DAB dc-dc converter can be calculated as

$$i_o^* = \frac{U_o^*}{R_{eq}} = \frac{i_o U_o^*}{U_o} \quad (13)$$

where  $U_o^*$  is the desired output voltage and  $R_{eq}$  is the equivalent load resistor. Since the power losses cannot be neglected in the actual converter system, a compensation value  $k_c$  should be introduced by using the fuzzy adjustment of the PI controller. The compensation value  $k_c$  can be the output value of the PI controller with the output voltage and its desired value as inputs. Then, the static error can be reduced, and (13) can be further expressed as

$$i_o^* = k_c \frac{i_o U_o^*}{U_o}. \quad (14)$$

In (14), all DAB modules should share this required output current  $i_o^*$ . Traditionally, the existing strategies prefer to divide this required output current evenly for each dc-dc converter module [15], [16], [19], [26], and [27]. However, this operation will usually influence the regulation of the input voltages since the DAB modules have different transferred current abilities with different input voltages, and the input-side capacitors have to compensate for the transferred currents. Then, the adjustment of the output voltage will influence the input voltages when the input voltages are not the same. To meet the current transferred abilities of each DAB module, the transferred current  $i_{TX}$  for meeting the requirement of the output side should be expressed as

$$i_{TX} = \frac{i_o^* U_{inX}}{U_{in}}. \quad (15)$$

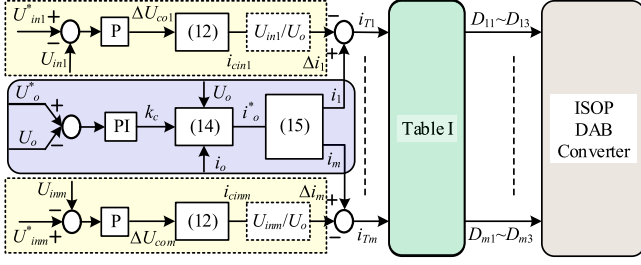


Fig. 6. Diagram of the proposed input-oriented power sharing control scheme with fast dynamic response for ISOP DAB dc-dc converter.

According to (15), when the input voltage and the load condition are changed, the influence on the voltage sharing performance on the input side can be significantly eliminated. Then, combining Table I, (12), (14), and (15), the proposed input-oriented power sharing control scheme with fast-dynamic response can be demonstrated in Fig. 6. At the beginning of the switching period, the input voltages, the output voltage, and the load current are measured. Based on the error of the output voltage and its desired value, the compensated value  $k_c$  can be obtained from the PI controller. Then, according to (14), the required output current can be calculated based on (15), the required transferred current  $i_X$  of each DAB module for meeting the requirement of load side can be obtained. Moreover, based on the error of the input voltages and their desired values, the required change values for each input voltage can be obtained based on a proportionality controller. Then, according to (12) and  $U_{inX}/U_o$ , the required transferred current  $\Delta i_X$  for adjusting the input voltages can be obtained. However, since the input voltages of each module may be very different, the item  $U_{inX}/U_o$  will usually result in large difference of transferred currents for charging and discharging the input-side capacitors. So, it is better to delete this item in the control system. Furthermore, the total required transferred current  $I_{TX}$  can be calculated as the difference of  $i_X$  and  $\Delta i_X$ . Finally, based on Table I, the corresponding phase-shift ratios can be obtained, and the proposed strategy can be implemented for positively adjusting the input voltages and dealing with the disturbance of the total input voltage and the load condition.

### C. Designs of the P Parameter and the PI Parameters in the Proposed Scheme

Combining (8), (10), and Fig. 6, when the input voltages of the DAB modules are adjusted, the disturbance of the output voltage  $\Delta U_o$  in a switching period can be expressed as

$$\begin{aligned} \Delta U_o &= \sum_{X=1}^m \frac{\Delta i_{inX} U_{inX} T_s}{C_o U_o} \\ &= \frac{\sum_{X=1}^m k_{pin} (U_{inX}^* - U_{inX}) C_X U_{inX} T_s}{C_o U_o} \end{aligned} \quad (16)$$

where  $k_{pin}$  is the proportional parameter of the P controller. Then, assuming the allowable output-voltage disturbance

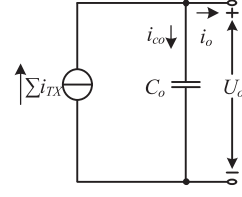


Fig. 7. Simplified circuit of the ISOP DAB dc-dc converter.

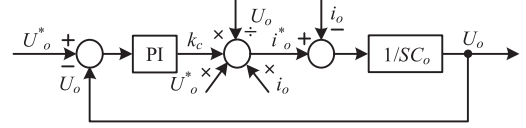


Fig. 8. Control schematic for regulating the output voltage.

TABLE II  
CIRCUIT PARAMETERS OF THE ISOP DAB DC-DC CONVERTER SYSTEM

$L_1, L_2$	40 $\mu$ H
$n_1, n_2$	1
$f_s$	40 kHz
$R$	15 $\Omega$ ~ 50 $\Omega$
$U_{in}$	100V ~ 120V
$U_o^*$	50V
$k_p, k_i, k_{pin}$	0.05, 0.005, 0.2
$C_{in1}, C_{in2}, C_o$	1mF

$\Delta U_{o\max}$ ,  $k_{pin}$  can be calculated as

$$k_{pin} \leq \frac{C_o U_o \Delta U_o}{\sum_{X=1}^m (U_{inX}^* - U_{inX}) C_X U_{inX} T_s}. \quad (17)$$

Moreover, since storage energy in middle inductance at the beginning and the end of a switching period can be regarded as the same at the steady-state condition and during the transient process, the simplified circuit of the ISOP DAB dc-dc converter can be shown in Fig. 7.

To reduce the influence on the output voltage during the adjustment of the input voltages, the variations of the input-capacitor currents should be very small. Thus, these branches for adjusting the input voltages can be eliminated when analyzing the PI parameters of the middle PI controller in Fig. 6. Then, the control schematic for regulating the output voltage can be demonstrated in Fig. 8.

According to Fig. 8, the transfer function with control-loop delay can be expressed as

$$H(s) = \frac{U_o^* i_o}{U_o} \frac{k_p s + k_i}{s} \frac{1}{s C_o} e^{-T_s}. \quad (18)$$

In addition, the main circuit parameters of the ISOP DAB dc-dc converter can be shown in Table II. Combining (18), the bode diagram can be demonstrated as Fig. 9.

As shown in Fig. 9, the measured simulation frequency response results are similar to the bode diagram, and the phase margin at cross-over frequency is bigger than 45° as 90°. Therefore, the stability of the proposed power sharing control scheme

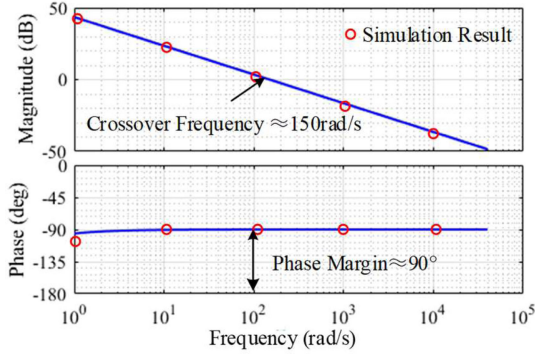


Fig. 9. Bode diagram of control loop for regulating the output voltage.

with fast-dynamic response can be ensured for the ISOP DAB dc–dc converter.

Moreover, by using the parameters at rating condition, the close-loop transfer function of the proposed scheme for the ISOP DAB dc–dc converter can be expressed as

$$G(s) = \frac{500se^{-T_s} + 50e^{-T_s}}{3s^2 + 500se^{-T_s} + 50e^{-T_s}}. \quad (19)$$

According to (19), the poles of the close-loop transfer function can be calculated as

$$P(s) = \frac{-500e^{-T_s} \pm \sqrt{(500e^{-T_s})^2 - 600e^{-T_s}}}{6} < 0. \quad (20)$$

Therefore, (20) can further verify the stability of the proposed scheme for the ISOP DAB dc–dc converter.

#### D. Inductance-Estimating Method for Ensuring the Desired Power Sharing Performance

According to Table I, the circuit parameters are employed to realize the power sharing performance of the ISOP DAB dc–dc converter system. So, if the employed inductance is not accurate, the power sharing performance should be affected without the integral function for adjusting the input voltages. When the steady-state condition is achieved, the relationship between the input power and the output power for each DAB module can be expressed as

$$\begin{aligned} & i_{in}U_{in1} : \dots : i_{in}U_{inX} : \dots : i_{in}U_{inm} \\ & = i'_{T1}U_o : \dots : i'_{TX}U_o : \dots : i'_{Tm}U_o \end{aligned} \quad (21)$$

where  $i'_{TX}$  is the actual transferred power for each DAB module. Assuming the actual inductance for each DAB module is  $L'_X$ , (21) can be further expressed as

$$U_{in1} : \dots : U_{inX} : \dots : U_{inm} = \frac{i_{T1}L_1}{L'_1} : \dots : \frac{i_{TX}L_X}{L'_X} : \frac{i_{Tm}L_m}{L'_m}. \quad (22)$$

Then, by using the first inductance  $L'_1$  as a reference, the other inductance can be calculated as

$$L'_X = \frac{i_{TX}L_X L'_1 U_{in1}}{i_{T1}L_1 U_{inX}}. \quad (23)$$

According to (23), the total transferred current  $i_T$  can be calculated as

$$i_T = \frac{i_{T1}L_1}{L'_1} + \sum_{X=2}^m \frac{i_{T1}L_1 U_{inX}}{L'_1 U_{in1}}. \quad (24)$$

Based on the Law of Conservation of Energy, the total transferred current  $i_T$  should be equivalent to the desired output current  $i^*_o$  as

$$i_T = i^*_o = \frac{i_{T1}L_1}{L'_1} + \sum_{\alpha=2}^m \frac{i_{T1}L_1 U_{inX}}{L'_1 U_{in1}}. \quad (25)$$

According to (25), the actual inductance  $L'_1$  of the first DAB module can be expressed as

$$L'_1 = \frac{i_{T1}L_1}{i^*_o} + \sum_{X=2}^m \frac{i_{T1}L_1 U_{inX}}{i^*_o U_{in1}}. \quad (26)$$

Then, combining (23), the inductances of other DAB modules can be estimated. Sometimes, the inductance values of the ISOP DAB dc–dc converter system may be unknown, a general inductance-estimating method will be presented as follow. For each DAB converter, the transferred current can be expressed by the calculated phase-shift ratios as [8]

$$i_{TX} = \frac{U_{inX} f(D_{X1}, D_{X2}, D_{X3}) T_s}{4n_X L_X}. \quad (27)$$

Combining (15) and (27), the estimated inductance for each DAB module can be expressed as

$$L'_X = \frac{f(D_{X1}, D_{X2}, D_{X3}) U_{in} T_s}{4i^*_o n_X}. \quad (28)$$

According to (28), the preset inductance can be eliminated. So, even without knowledge of inductance values, the presented general inductance-estimating method can be employed in other control schemes with the measurement of load current for the ISOP DAB dc–dc converter system. Moreover, since the inductance-estimating method should be employed in the steady-state condition for a more accurate estimated value, the decoupling between the estimating process and the transient process should be realized, especially for dealing with the load-resistor disturbance. To deal with this issue, the change of the load current can be employed to stop the estimating process, and the change of the input voltage should be observed for ensuring the steady-state condition of input voltages. Then, when the change of the input voltage in two continuous switching periods is smaller than the peak value of the measurement noise, the estimating operation can be activated again. The time duration of these two switching periods should be big enough such as more than half of the change time of the input voltages.

## IV. VERIFICATION

In this section, based on the circuit parameters in Table II, a simulation model and a small-scale experimental platform with two DAB modules are built to verify effectiveness of the proposed input-oriented power sharing control method with fast-dynamic response for the ISOP DAB dc–dc converter system.

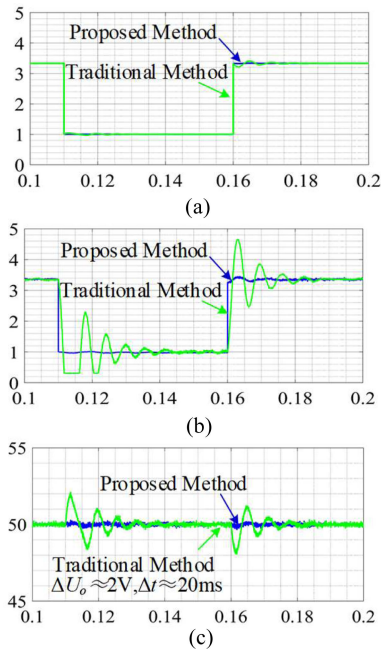


Fig. 10. Simulation results when the load resistor is changed ( $t$ : 20 ms/div). (a) Load current (A). (b) Total transferred current (A). (c) Output voltage (V).

### A. Simulation Results

In the simulation part, the comparison of the traditional method [26], [27] and the proposed input-oriented power sharing control scheme with fast-dynamic response will be provided. Moreover, by using the proposed general inductance-estimating method for the ISOP DAB dc–dc converter, the inductance values under the traditional method are estimated with the measurement of the load current.

When the input voltage is 100 V and the power balance performance is achieved, Fig. 10 shows the simulation results of the traditional method and the proposed scheme when the load resistor is changed between 15 and 50 Ω. As shown in Fig. 10(b), when the load resistor is changed, the total transferred current  $\Sigma i_{TX}$  under the proposed scheme can follow with the change of the load current timely as shown in Fig. 10(a). Thus, as shown in Fig. 10(c), the output voltage can remain at its desired value 50 V by using the proposed scheme. However, compared with Fig. 10(a) and (b) under the traditional method, the total transferred current can not be stable at the required current timely, so the output voltage disturbances are obvious.

Moreover, when the input voltage is 100 V and the load resistor is 15 Ω, Fig. 11 shows the simulation results when the power sharing performance of these two DAB modules is changed between 1:1 and 2:1 [see from Fig. 11(a) and (b)]. As shown in Fig. 11(c), during the regulation of input voltages, the transferred current under the proposed scheme can keep constant, but the transferred current under the traditional method has some disturbances. Then, according to Fig. 11(d), the stable output voltage can be obtained by using the proposed scheme, but the output-voltage disturbances under the traditional method are obvious.

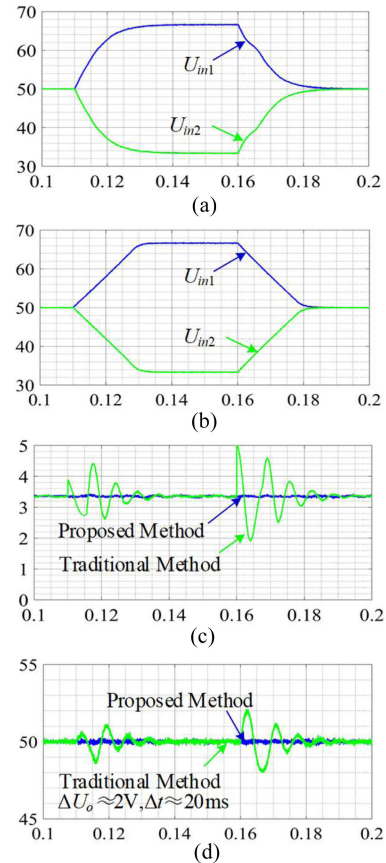


Fig. 11. Simulation results when the power sharing performance is changed ( $t$ : 20 ms/div). (a) Input voltage (V) under the traditional method. (b) Input voltage (V) under the proposed method. (c) Total transferred current (A). (d) Output voltage (V).

In addition, when  $L_1$  is changed to 30 μH in the simulation model, Fig. 12 shows the simulation results of the proposed inductance-estimating method embedded in the traditional method [26], [27] at the cost of an additional load-current sensor. As shown in Fig. 12(a), the estimated inductances are close to the setup values. The relationship of these two estimated inductances can be accurate as shown in Fig. 12(b). Therefore, the proposed general inductance-estimating method can also be employed in other control schemes for the ISOP DAB dc–dc converter if the accuracy of the inductances should be ensured.

### B. Experimental Results

When the inductance of the first DAB module  $L_1$  is inaccurate as 24 μH, Fig. 13 shows the experimental results when the input voltage and the load resistor are changed. As shown in Fig. 13(a) and (b), when the total input voltage is changed between 100 and 120 V, the output voltage  $U_o$  can be kept at its desired value as 50 V. However, the power balance performance cannot be achieved since the inductance value  $L_1$  is not accurate. Moreover, as shown in Fig. 13(c) and (d), when the load resistor is changed between 15 and 50 Ω, the output voltage  $U_o$  can be stable at its desired value. Therefore, when the inductance value is not accurate, the desired power sharing performance cannot be

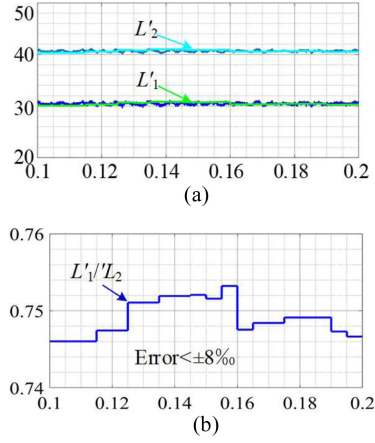


Fig. 12. Simulation results of the estimated inductance by using the proposed general inductance-estimating method embedded in the traditional control method ( $t$ : 20 ms/div). (a) Estimated inductances ( $\mu\text{H}$ ). (b) Relationship of  $L'_1$  and  $L'_2$ .

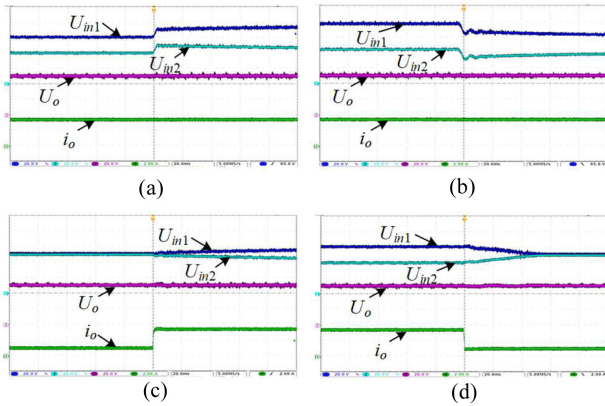


Fig. 13. Experimental results when  $L_1 = 24 \mu\text{H}$  and  $L_2 = 40 \mu\text{H}$  ( $U_{in1}$ ,  $U_{in2}$  and  $U_o$ : 20 V/div;  $i_o$ : 2 A/div; and  $t$ : 20 ms/div). (a)  $U_{in} : 100 \text{ V} \rightarrow 120 \text{ V}$ . (b)  $U_{in} : 120 \text{ V} \rightarrow 100 \text{ V}$ . (c)  $R : 50 \Omega \rightarrow 15 \Omega$ . (d)  $R : 15 \Omega \rightarrow 50 \Omega$ .

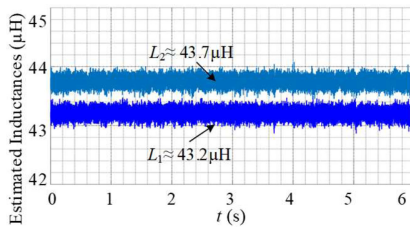


Fig. 14. Estimated inductances.

realized, but the excellent dynamic response can be provided for the ISOP DAB dc–dc converter.

Then, when the total input voltage is 100 V, the desired output voltage is 50 V and the load resistor is 15  $\Omega$ , the experiment result of these estimated inductances of these two DAB modules can be shown in Fig. 14. As shown in Fig. 14, the estimated inductance of the first DAB module  $L_1$  is 43.2  $\mu\text{H}$ , and the estimated inductance of the second DAB module  $L_2$  is 43.7  $\mu\text{H}$ . Thus, these estimated inductances are close to the actual inductances

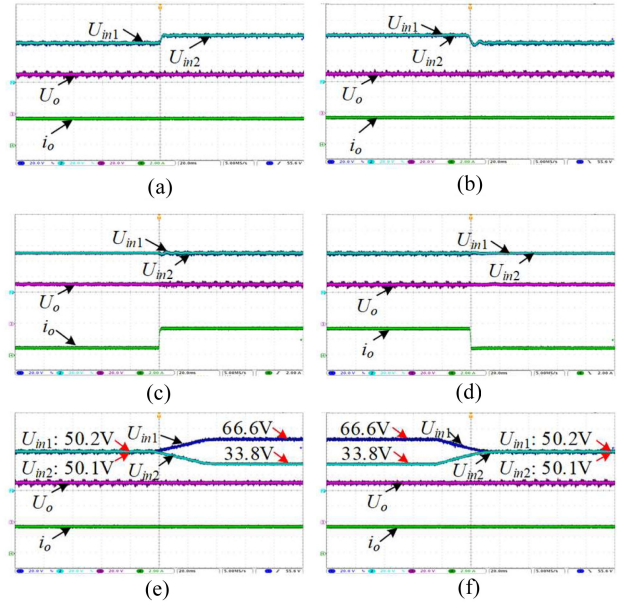


Fig. 15. Experimental results with estimated inductances  $L_1 = 43.2 \mu\text{H}$  and  $L_2 = 43.7 \mu\text{H}$  ( $U_{in1}$ ,  $U_{in2}$  and  $U_o$ : 20 V/div;  $i_o$ : 2 A/div; and  $t$ : 20 ms/div). (a)  $U_{in} : 100 \text{ V} \rightarrow 120 \text{ V}$ . (b)  $U_{in} : 120 \text{ V} \rightarrow 100 \text{ V}$ . (c)  $R : 50 \Omega \rightarrow 15 \Omega$ . (d)  $R : 15 \Omega \rightarrow 50 \Omega$ . (e)  $P_1 : P_2 = (1 : 1) \rightarrow (2 : 1)$ . (f)  $P_1 : P_2 = (2 : 1) \rightarrow (1 : 1)$ .

as given in Table II but a little bigger, which should be caused by the power losses.

Based on the estimated inductances, the experiment results can be shown in Fig. 15 when the input voltage, the load resistor, and the power sharing performance are changed. As shown in Fig. 15(a) and (b), the power balance performance of the ISOP DAB dc–dc converter can be ensured, and when the input voltage is changed, the output voltage can be stable at its desired value. Moreover, as shown in Fig. 15(c) and (d), when the load resistor is changed between 15 and 50  $\Omega$ , the output-voltage disturbance can be regarded as zero. In addition, As shown in Fig. 15(e) and (f), when the desired power sharing performance of these two DAB modules is changed between 1:1 and 2:1, the corresponding actual power sharing performances are 1:1 and 1.97:1. So, based on the proposed scheme, the power sharing performance of the ISOP DAB dc–dc converter can be adjusted flexibly. Furthermore, when the power sharing performance is changed, the output voltage can be kept at its desired value. Therefore, with the estimated inductances, the required power sharing performance can be ensured, and an excellent dynamic response can be achieved when the input voltage, the load resistor, and the power sharing performance are changed.

With the actual inductances of these two DAB modules, the experiment results, when the input voltage, the load resistor, and the power sharing performance are changed, can be shown in Fig. 16. Similarly, when the input voltage, the load resistor, and the power sharing performance of the ISOP DAB dc–dc converter are changed, the output voltage can be kept at its desired value, and the excellent dynamic performance can be provided for this converter system. Moreover, as shown in Fig. 16(e) and

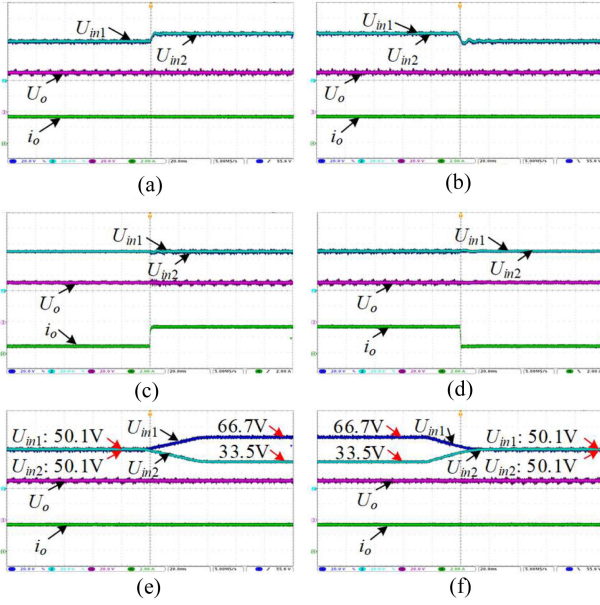


Fig. 16. Experimental results when  $L_1 = 40 \mu\text{H}$  and  $L_2 = 40 \mu\text{H}$  ( $U_{in1}$ ,  $U_{in2}$  and  $U_o$ : 20 V/div;  $i_o$ : 2 A/div; and  $t$ : 20 ms/div). (a)  $U_{in1}$ : 100 V  $\rightarrow$  120 V. (b)  $U_{in1}$ : 120 V  $\rightarrow$  100 V. (c)  $R$ : 50  $\Omega$   $\rightarrow$  15  $\Omega$ . (d)  $R$ : 15  $\Omega$   $\rightarrow$  50  $\Omega$ . (e)  $P_1 : P_2 = (1 : 1) \rightarrow (2 : 1)$ . (f)  $P_1 : P_2 = (2 : 1) \rightarrow (1 : 1)$ .

(f), when the desired output power of the first DAB module is double as that of the second DAB module, the actual power sharing performance of these two modules is 1.99 : 1, and when the desired output power of the first DAB modules should be the same as that of the second DAB module, this power balance requirement can be achieved. Therefore, with actual inductance values, the desired power sharing performance can be ensured for the ISOP DAB dc–dc converter by using the proposed input-oriented power sharing control scheme with fast-dynamic response. Thus, experiment results in Fig. 16 can be a reference for experiment results in Fig. 15, which can be employed to verify the effectiveness of the proposed inductance-estimating method.

## V. CONCLUSION

In this article, an input-oriented power sharing control scheme with fast-dynamic response is proposed for the ISOP DAB dc–dc converter system. With the average model of this converter system, the coupling between adjusting power sharing performance and maintaining the output voltage is analyzed. Based on the proposed scheme, this coupling can be reduced significantly. Moreover, the proposed scheme can provide the excellent dynamic response for the DAB dc–dc converter, and the robustness of the converter system can be enhanced markedly. The conducted studies are summarized as follows.

- 1) The coupling between adjusting power sharing performance and maintaining the output voltage of the ISOP DAB dc–dc converter is unavoidable. Then, during the adjusting of the power sharing performance, the total transferred current caused by the regulation of the input voltages should be controlled close to zero, or the

regulation of the input voltages should be slow enough. Then, the influence on the output voltage can be reduced significantly.

- 2) When the adopted inductance value of the ISOP DAB dc–dc converter is inaccurate, the power sharing performance of this converter system will be damaged. Under this condition, the excellent dynamic response of output voltage can also be obtained by using the proposed scheme.
- 3) Based on the proposed inductance-estimating method, the inductance values for each DAB module can be estimated, which can be employed to ensure the power sharing performance of the ISOP DAB dc–dc converter system. Moreover, the proposed inductance-estimating method can be embedded in other control schemes for these DAB-based converter systems if the accuracy of inductances is required.
- 4) Based on the proposed input-oriented power sharing control strategy with fast-dynamic response, the excellent dynamic response can be provided for the ISOP DAB dc–dc converter when the total input voltage, the load resistor, and the power sharing performance are changed.

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