

# Inductive Power Transfer System With Maximum Efficiency Tracking Control and Real-Time Mutual Inductance Estimation

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**Abstract**—To design simple and efficient inductive power transfer (IPT) systems, a minimum number of conversion stages and an effective maximum efficiency tracking (MET) are the primary design criteria. The MET control uses a fast mutual inductance estimation (MIE) algorithm to achieve fast tracking of the maximum efficiency point, especially when the variation of the gap distance and misalignment of the magnetic coupler are significant. The feedback control of the MET-MIE IPT system should be designed without a wireless communication channel to improve stability and robustness. In this article, a novel MET-MIE control strategy is proposed for achieving simplicity and high efficiency in IPT systems. Verifications are provided by simulations and experiments. It is shown that maximum efficiency can be tracked with less than 4% error in MIE under significant variation of the gap distance and misalignment of the magnetic coupler.

**Index Terms**—Inductive-power-transfer (IPT), maximum efficiency tracking (MET), misalignment, mutual inductive estimation.

## I. INTRODUCTION

THE development of wireless power transfer (WPT) technology has progressed rapidly in the past three decades and has now reached the stage of commercialization [1]. The inductive power transfer (IPT), in particular, is a near field WPT technology transferring power in a short distance by inductive coupling via magnetic fields with relatively high efficiency [2]. The IPT technology is now widely used in consumer electronics [3], biomedical implants [4], metro rail transit [5], and electric vehicles (EV) [6], [7].

The simplest IPT topology is shown in Fig. 1(a). It consists of a power source  $V_{in}$ , an inverter, a magnetic coupler, a rectifier, and load  $R_L$ . Among the basic compensation schemes, namely, series–parallel (S–P), parallel–parallel (P–P), parallel–series (P–S), and series–series (S–S) compensation schemes, the S–S

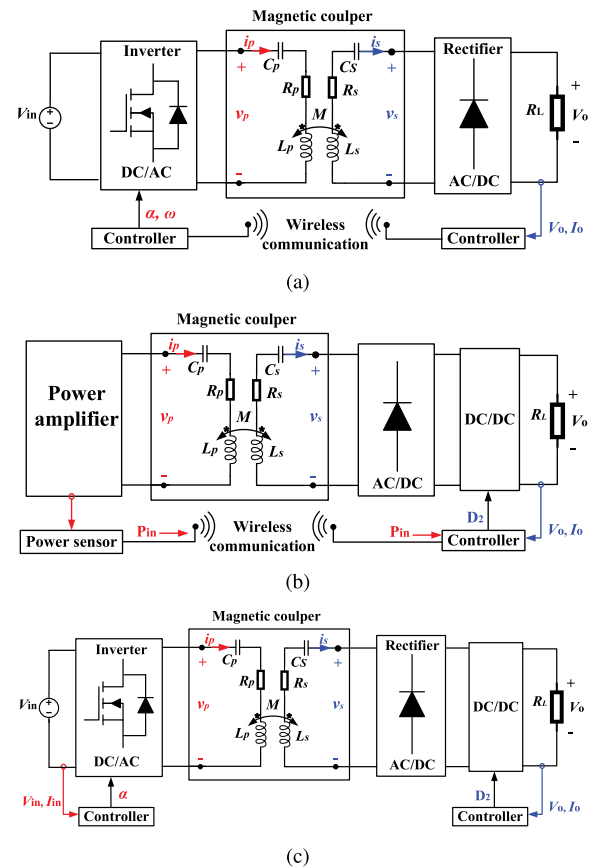


Fig. 1. (a) Simplest S–S compensated IPT system; (b) with extra DC/DC converter at load side [9], [10]; (c) with extra DC/DC converter at load side but without fast wireless communication channel [11].

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scheme is most widely used for its low sensitivity to variations of load and mutual inductance [8]. Unfortunately, being a resonant converter system, the maximum efficiency of this simple IPT system can only be achieved if the following conditions are satisfied [6], [8]: 1) load  $R_L$  equals a matched load  $R_m$ , which varies with mutual inductance  $M$ , and 2) the phase difference between the inverter voltage and current must be slightly positive in order to permit zero-voltage switching (ZVS) of all the MOSFET power switches. To cater for a wider load range, an extra dc/dc converter responsible for transforming  $R_L$  dynamically into  $R_m$  as seen by the rectifier has been proposed using a

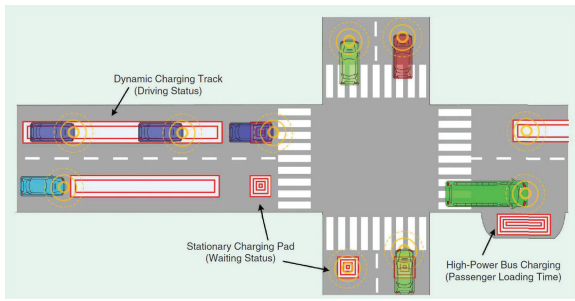


Fig. 2. Dynamic and static charging scenario of a EV driving on a road [7].

power amplifier as power source, as shown in Fig. 1(b) [9], [10]. However, the efficiency gained from impedance matching may not compensate for the extra losses due to the presence of more power conversion stages in the low-efficiency power amplifier and the cascaded buck–boost dc/dc converter. Moreover, the system efficiency can be maximized using the information of input power and output power, but it necessitates the use of wireless communication. In order to achieve high efficiency over a wider load range with output regulation, and to eliminate the need for wireless communication, an extra dc/dc converter responsible for output regulation and an independent maximum efficiency tracking (MET) control implemented in the inverter are proposed for the simple IPT system shown in Fig. 1(c) [11]. It should be noted that the MET control requires information of  $R_L$  and  $M$ . The inverter is controlled by modulating a phase angle  $\alpha$ , corresponding to the duty cycle of the inverter (described in Section II), and the process is digitally controlled by an inherently slow perturbation and observation (P&O) algorithm, which aims to minimize the input current and the input power of the inverter. The drawbacks of this system are that 1) the extra dc/dc converter stage incurs extra loss, 2) ZVS cannot be achieved for all power switches, and 3) the P&O control is inherently slow due to the random perturbation speed and amplitude to search the optimal control variable when the load or mutual inductance have variations.

To alleviate the above problems, the duty cycle regulated extra dc/dc converter can be replaced by an active rectifier with appropriate control to achieve the required impedance matching and output regulation with ZVS in all power switches [12]–[14]. Unfortunately, the mutual inductance  $M$  is not measured dynamically and its value is a design parameter for achieving a specific converter voltage ratio [12]. Moreover,  $M$  is also a reference parameter for efficiency optimization [13] and is used for the determination of control parameters [14]. Thus,  $M$  is an important design parameter for the accurate control of an IPT system in dynamic scenarios [12]–[14], where the misalignment and gap distance between the transmitting coil and receiving coil may change with time. For example, when a EV is driving on the road, the gap distances are varying with time [7], especially under different load conditions as shown in Fig. 2. The accuracy of the control can be greatly compromised without real-time measurement of  $M$  [12]–[14]. In a recent work [15], the mutual

inductance  $M$  is dynamically measured for facilitating real-time control against misalignment and variation of the gap distance of the magnetic coupler. However, the system configuration is still inadequate in the following aspects: 1) it requires a primary side dc/dc converter for the regulation of the output voltage, thus incurring extra loss; 2) the impedance matching is performed by a secondary T-type filter built with a matrix of relay switches that is too slow to keep up with the speed of impedance matching. Moreover, the control relies on a high-speed wireless data link for the exchange of important control information from one switching cycle to another between the primary and the secondary controllers.

Many attempts have been made to perform real-time measurement (or estimation) of  $M$ . By measuring the zero crossing time instants of the square inverter voltage, the voltage of the parallel compensation capacitor and the current of the transmitter of the magnetic coupler of an *LCC–LCC* compensated IPT converter system,  $M$  can be estimated from the time lapse between successive zero-crossing time instants [16]. While, the calculation is subject to high round-up (or round-down) errors when the resolution of the data point acquired is not sufficiently fine. In [17],  $M$  is estimated by operating at a test frequency different from the normal resonant frequency. The input impedance derived has a singularity at the resonant frequency that makes this method unsuitable for real-time measurement at resonance. In a recent work [18], extra bidirectional switch and capacitor are added in parallel to the primary side compensation capacitor of an *S–S* compensated IPT system. The *S–S* IPT system operates as usual when the switch is OFF. The switch is turned ON when the information of  $M$  is needed. The information of  $M$  can be estimated from the real-time measurements of the dc input voltage and the two-set values of the rms current of the transmitter and operating frequency during tuned and detuned operations. However, the additional bidirectional switch needs two extra MOSFETs, which may incur loss and increase the cost and complexity of the system. In another recent work [19], a method of shorting the secondary active rectifier to ground for a brief duration is proposed to estimate  $M$  for the *S–S* compensation IPT system by precisely detecting the phase differences between the switching signal of the inverter and the transmitter current of the magnetic coupler. In addition, a topology with two sets of square wave generators having different voltage and frequency have been used [20]. The generator sets are connected with the secondary windings in series, so as to create a beat frequency out of the sum of two power signals with two frequencies and magnitudes, to drive the magnetic coupler of an *S–S* compensated IPT system. When the information of  $M$  is needed, the power switch is turned OFF to create a modulation of current at the receiver of the magnetic coupler. The modulated amplitude of the current at steady-state is measured to estimate  $M$ .

Some methods have been proposed to activate a measurement circuit in demand and wait until a new steady-state is reached for the actual measurement [17]–[20]. After the measurement, the measurement circuit is disabled and the converter system resumes its normal operation. The switching between two modes

TABLE I  
FEATURES OF IPT SYSTEM WITH MET CONTROL AND REAL-TIME MIE

Feature	[10], [11]	[12]	[13]–[15]	[16]	[17]–[20]	[21]	proposed
Simplest topology with active rectifier	×	×	✓	×	×	✓	✓
ZVS for all MOSFETs	–	×	✓	×	×	×	✓
Fast MET with real-time estimation of $M$	×	×	×	✓	×	×	✓
Specific and simple $M$ estimation	×	×	×	✓	×	×	✓
General but complicated $M$ estimation	×	×	×	×	✓	✓	×
Wireless communication for feedback control not necessary	×	✓	×	×	✓	✓	✓

Keys: (check, Yes), (–, Unknown), (×, No).

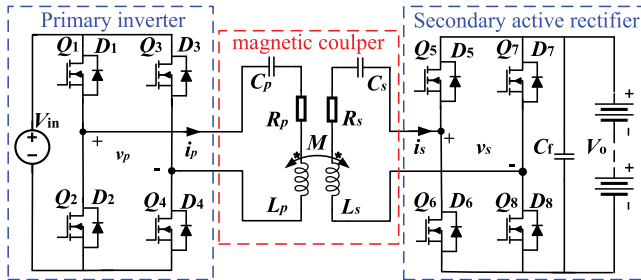


Fig. 3. Simplest S–S compensation IPT topology with active rectifier.

of operation can complicate the control, disrupt the normal operation of the system, and decrease the controller speed and the overall system performance.

The desirable features of the MET control implemented in an S–S compensation IPT system are shown in Table I. Compared with the existing methods, the merits of our proposed method include 1) using simplest topology with an active rectifier, 2) achieving ZVS for all MOSFETs, 3) implementing MET control with real-time estimation of mutual inductance for dynamic scenarios, and 4) requiring no wireless communication between the primary and secondary sides.

## II. SYSTEM STRUCTURE AND STEADY-STATE MODEL

Fig. 3 shows a simplest S–S compensation IPT system with a secondary active rectifier and battery load. For ease of reference, subscripts  $p$  and  $s$  denote parameters in the primary and secondary sides, respectively. The magnetic coupler has self-inductances  $L_p$  with resistance  $R_p$  and  $L_s$  with resistance  $R_s$ , and mutual inductance  $M$ . The series–series compensation capacitors  $C_p$  and  $C_s$  are driven by the primary inverter with a high frequency voltage  $v_p$  and the secondary active rectifier with a high frequency voltage  $v_s$ .

Power switches  $Q_1$  to  $Q_8$  are driven by control signals  $G_1$  to  $G_8$ . Typical steady-state operating waveforms  $v_p$ ,  $v_s$ ,  $i_p$ , and  $i_s$  are shown in Fig. 4, corresponding to a power flowing from primary side to secondary side. For the primary side, transistor pairs  $(Q_1, Q_4)$  and  $(Q_2, Q_3)$  turn ON and OFF simultaneously with 50% duty cycle, which defines two levels of  $v_p$  with 50% duration of positive and negative voltages in one period. Moreover, the conduction angle  $\beta \in [0, \pi]$  defines the duration of positive and negative voltages of  $v_s$  within one period. The relative phase angle  $\theta \in [0, \pi/2]$  of  $v_p$  and  $v_s$  can be controlled by the relative phase of transistor pairs  $(Q_1, Q_2)$  and  $(Q_5, Q_6)$ .

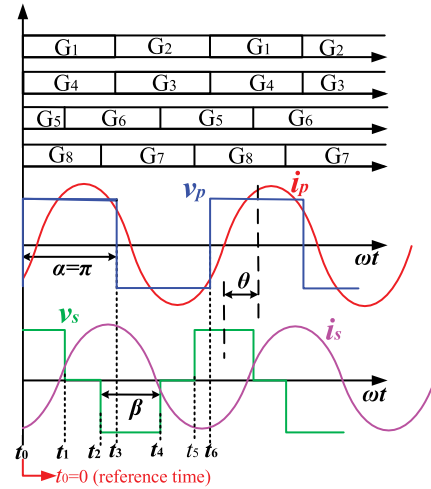


Fig. 4. Steady-state operating waveforms.

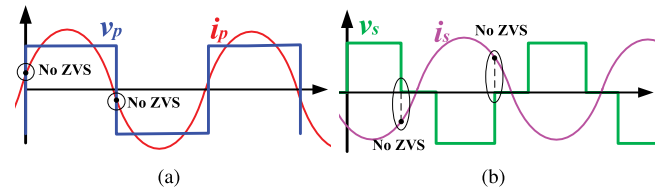


Fig. 5. Steady-state waveforms corresponding to absence of ZVS. (a) Primary side. (b) Secondary side.

The time sequence  $\{t_0, \dots, t_6\}$  is the turn-ON times of one of the eight power switches within a switching period. It should be noted that the phases of  $i_p$ ,  $i_s$ ,  $v_p$ , and  $v_s$  shown in Fig. 4 are designed for ensuring ZVS of all transistors for the desired power flow. By changing the time sequences of control signals  $G_1$  to  $G_8$ , a situation may arise where the phases between currents and voltages in both sides do not permit ZVS to be achieved for all switches, as shown in Fig. 5. The detailed analysis of the ZVS conditions is given in Section III-A. The initial time point  $t_0 = 0$  is set as the time reference point of the time-domain model.

In general,  $C_p$  and  $C_s$  are designed to compensate  $L_p$  and  $L_s$  for matching the required resonant frequency  $\omega$  in order to minimize the apparent power rating and maximize the transfer capability. The operating switching frequency is usually designed at the resonant frequency, i.e.,

$$\omega = \frac{1}{\sqrt{L_p C_p}} = \frac{1}{\sqrt{L_s C_s}}. \quad (1)$$

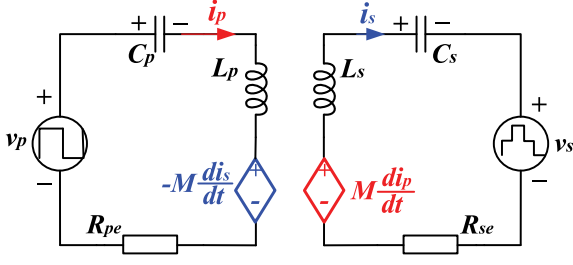


Fig. 6. Equivalent circuit of the magnetic coupler of Fig. 3.

With  $t_0 = 0$ , the fundamental component of  $v_p(t)$  and  $v_s(t)$  can be written as

$$v_p(t) = \frac{4V_{in}}{\pi} \cos\left(\omega t - \frac{\pi}{2}\right), \text{ and} \quad (2)$$

$$v_s(t) = \frac{4V_o}{\pi} \cos\left(\omega t - \frac{\pi}{2} + \theta\right) \sin\left(\frac{\beta}{2}\right). \quad (3)$$

Referring to Fig. 6 and applying KVL, we obtain

$$i_p(t)R_{pe} + L_p \frac{di_p(t)}{dt} + v_{C_p}(t) - M \frac{di_s(t)}{dt} = v_p(t) \quad (4)$$

$$i_s(t)R_{se} + L_s \frac{di_s(t)}{dt} + v_{C_s}(t) - M \frac{di_p(t)}{dt} = -v_s(t). \quad (5)$$

where  $R_{pe} = R_p + 2R_{ds} + R_{C_p}$  and  $R_{se} = R_s + 2R_{ds} + R_{C_s}$  are equivalent resistances of the magnetic coupler, with  $R_{ds}$  being the ON-state resistance of the MOSFET and  $R_{C_s}$  the series resistance of the capacitor. At resonance, the sum of the voltages across  $C_p$  and  $L_p$  is zero, and likewise for  $C_s$  and  $L_s$ . Thus, (4) and (5) can be approximated as

$$i_p(t) = \frac{v_p(t) - M \frac{di_s(t)}{dt}}{R_{pe}} \quad (6)$$

$$i_s(t) = \frac{M \frac{di_p(t)}{dt} - v_s(t)}{R_{se}}. \quad (7)$$

Substituting  $v_p(t)$  in (2) and  $v_s(t)$  in (3) into (6) and (7), and using  $\omega M \gg R_{se}$  and  $\omega^2 M^2 \gg R_{pe}R_{se}$  for this high-Q circuit, we obtain

$$i_p(\vartheta) = \frac{4V_o}{\pi} \frac{\sin(\frac{\beta}{2}) \sin(\vartheta - \frac{\pi}{2} + \theta)}{\omega M}, \text{ and} \quad (8)$$

$$i_s(\vartheta) = \frac{4V_{in}}{\pi} \frac{\sin(\vartheta - \frac{\pi}{2})}{\omega M} \quad (9)$$

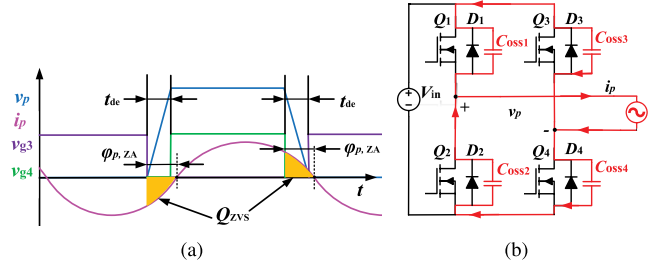
where  $\vartheta = \omega t$ . The transmission power for this approximated lossless system can be expressed as

$$P = \frac{1}{2\pi} \int_0^{2\pi} v_p(\vartheta) i_p(\vartheta) d\vartheta \quad (10)$$

Substituting (8) and (2) into (10), we get

$$P = \frac{8V_{in}V_o}{\pi^2\omega M} \sin\left(\frac{\beta}{2}\right) \sin(\theta). \quad (11)$$

The output power is proportional to  $P$  and can be controlled monotonically by the control angles  $\beta \in [0, \pi]$ , and  $\theta \in [0, \pi/2]$ .

Fig. 7. Principles of ZVS soft switching about  $Q_4$ . (a) Operating waveforms. (b) Equivalent circuit during dead time.

### III. MAXIMUM EFFICIENCY AND MUTUAL INDUCTANCE TRACKING

In this section, we will formulate the condition for ZVS of all power switches to minimize switching loss. With ZVS guaranteed, the conduction loss formulated in Section III-B will be minimized by finding the optimal control angles ( $\beta$ ,  $\theta$ ) and the real-time estimated mutual inductance  $M$  described in Section III-D.

#### A. ZVS Conditions

In order to achieve ZVS, taking the primary side switch  $Q_4$  as an example, the phase angle of current  $i_p$  should lag  $v_p$  to discharge the parasitic output capacitance  $C_{oss4}$  of  $Q_4$  during the dead time  $t_{de}$ , as shown in Fig. 7(a), where the integral of  $i_p$  during  $t_{de}$  is denoted as  $Q_{ZVS}$ . Then, ZVS of  $Q_4$  can be achieved when  $Q_{ZVS}$  is sufficient to charge  $C_{oss3}$  from 0 V to  $V_{in}$  and discharge  $C_{oss4}$  from  $V_{in}$  to 0 V, i.e.,

$$Q_{ZVS} = \int_0^{t_{de}} i_p dt \geq \int_0^{V_{in}} (C_{oss3} + C_{oss4}) dv. \quad (12)$$

Taking the primary inverter as an example, to determine the minimum phase difference  $\delta_{p,\min}$  and the minimum dead time  $t_{p,de-\min}$  required by ZVS, the waveform of  $i_p$  during the dead time is expressed as a piecewise sine wave. Therefore, according to (12) and the equivalent circuit shown in Fig. 7(b),  $\delta_{p,\min}$  and  $t_{p,de-\min}$  can be calculated from [21], given by

$$\delta_{p,\min} = \arccos\left(1 - \frac{\sqrt{2}\pi V_{in}(C_{oss3} + C_{oss4})}{T_s I_p}\right) \approx \sqrt{\frac{2\sqrt{2}\pi V_{in}(C_{oss3} + C_{oss4})}{T_s I_p}} \quad (13)$$

and

$$t_{p,de-\min} = \frac{\delta_{p,\min} T_s}{2\pi} \quad (14)$$

where  $T_s = 2\pi/\omega$  is the switching period of the primary inverter and  $I_p$  is the root-mean-square value of  $i_p$ . Similarly, the minimum phase difference and the minimum dead time required by ZVS in secondary active rectifier can also be obtained. For simplicity, the equations are not given here. According to the design parameters listed in Table III and the data sheet value of  $C_{oss}$  of MOSFETs adopted in our experimental prototype,

TABLE II  
PARAMETERS OF MAGNETIC COUPLED COILS

Parameters	Symbols	Values
Materials	Litz Wire	AWG38
Turns	$n_p, n_s$	30, 46
Outer Diameter	$d_{o\_p}, d_{o\_s}$	300mm, 500mm
Inner Diameter	$d_{in\_p}, d_{in\_s}$	35mm, 35 mm
Radius	$r_p, r_s$	0.5 mm, 0.75 mm

TABLE III  
PARAMETERS OF EXPERIMENTAL PROTOTYPE

Parameters	Symbols	Values
Operating frequency	$f$	85 kHz
Input voltage	$V_{in}$	45 V
Output voltage	$V_o$	80 V
Rated power	$P_N$	120 W
Dead Time	$t_{de}$	300 ns
Self inductance	$L_p, L_s$	117.9 $\mu$ H, 174.4 $\mu$ H
Current Transformer	CT	TAK12-02
Digital to analog module	DA	DAC8501
Equivalent resistances	$R_{pe}, R_{se}$	0.27 $\Omega$ , 0.32 $\Omega$
Compensation capacitances	$C_p, C_s$	29.98 nF, 20.12 nF

we arrive at a design with a margin of the minimum phase difference  $\delta_{\min} = 0.14$  rad and the dead time  $t_{de-\min} = 300$  ns in the primary inverter and the secondary active rectifier.

We denote by  $\varphi_{p,ZA}$  and  $\varphi_{s,ZA}$  the phase angle of the current lagging the voltage in primary and secondary sides, respectively. According to the steady-state operating waveforms shown in Fig. 4,  $\varphi_{p,ZA} = \frac{\pi}{2} - \theta$  and  $\varphi_{s,ZA} = \frac{\beta}{2} - \theta$ . Then, the conditions of ZVS in both sides are

$$\frac{\pi}{2} - \theta \geq \delta_{\min}, \text{ and} \quad (15)$$

$$\frac{\beta}{2} - \theta \geq \delta_{\min}. \quad (16)$$

Since  $\beta \leq \pi$ , (16) implies (15). Thus, we only need to focus on (16) to guarantee ZVS of all power switches.

### B. System Conduction Loss

Once ZVS is guaranteed, the system conduction losses should be dynamically optimized to achieve MET. Referring to the equivalent circuit shown in Fig. 6, the resistive power loss in the magnetic coupler can be expressed as

$$P_{\text{con-loss}} = I_p^2 R_{pe} + I_s^2 R_{se} \quad (17)$$

where  $I_p$  and  $I_s$  are the RMS values of  $i_p$  and  $i_s$ . According to (8) and (9), we have

$$I_p = \sqrt{\frac{1}{\pi} \int_0^\pi i_p^2(\vartheta) d(\vartheta)} = \frac{2\sqrt{2}V_o}{\pi\omega M} \sin \frac{\beta}{2}, \text{ and} \quad (18)$$

$$I_s = \sqrt{\frac{1}{\pi} \int_0^\pi i_s^2(\vartheta) d(\vartheta)} = \frac{2\sqrt{2}V_{in}}{\pi\omega M}. \quad (19)$$

Substituting (18) and (19) into (17), the system conduction loss  $P_{\text{con-loss}}$  is given by

$$P_{\text{con-loss}}(\beta) = \frac{8V_o^2}{\pi^2\omega^2 M^2} \sin^2 \frac{\beta}{2} R_{pe} + \frac{8V_{in}^2}{\pi^2\omega^2 M^2} R_{se}. \quad (20)$$

### C. Optimal Solutions

In Sections III-A and III-B, the ZVS conditions and the formulation of system conduction loss are discussed. Our aim in this section is to find optimal solutions  $(\beta, \theta)$  to modulate the inverter and active rectifier to achieve MET with ZVS given by the condition (16) and minimum conduction loss by minimizing  $P_{\text{con-loss}}(\beta)$  as given in (20) at transmission power  $P_N$  given by (11). The optimization can be described as

$$\text{Minimize } \{P_{\text{con-loss}}(\beta)\} \text{ such that} \quad (21)$$

$$\begin{cases} P_N - \frac{8V_{in}V_o}{\pi^2\omega M} \sin \frac{\beta}{2} \sin \theta = 0 \\ \frac{\beta}{2} - \theta \geq \delta_{\min}. \end{cases} \quad (22)$$

This is an optimization problem with limited conditions that can be solved by using the Lagrange multiplier method. According to (21) and (22), the constrained Lagrange function can be described as

$$\begin{aligned} L(\beta, \theta, \lambda_1, \lambda_2) = & P_{\text{con-loss}}(\beta) \\ & + \lambda_1 \left( P_N - \frac{8V_{in}V_o}{\pi^2\omega M} \sin \frac{\beta}{2} \sin \theta \right) \\ & + \lambda_2 \left( \frac{\beta}{2} - \theta - \delta_{\min} \right) \end{aligned} \quad (23)$$

where,  $\lambda_1 \neq 0$  and  $\lambda_2 \geq 0$ . The optimal solutions should satisfy the Karush–Kuhn–Tucker condition given by

$$\begin{cases} \frac{\partial L}{\partial \beta} = 0 \\ \frac{\partial L}{\partial \theta} = 0 \\ \lambda_1 \left( P_N - \frac{8V_{in}V_o}{\pi^2\omega M} \sin \frac{\beta}{2} \sin \theta \right) = 0 \\ \lambda_2 \left( \frac{\beta}{2} - \theta - \delta_{\min} \right) = 0. \end{cases} \quad (24)$$

Solving (24), an optimal solution of  $\theta_{\text{op}}$  and  $\beta_{\text{op}}$  is

$$\beta_{\text{op}} = \arccos \left( 1 - \frac{\pi^2\omega M P_N}{4V_{in}V_o} \right) + \delta_{\min}, \text{ and} \quad (25)$$

$$\theta_{\text{op}} = \frac{1}{2} \arccos \left( 1 - \frac{\pi^2\omega M P_N}{4V_{in}V_o} \right) - \frac{1}{2} \delta_{\min}. \quad (26)$$

### D. Dynamic Measurement of Mutual Inductance

In Section III-C, given a power  $P_N$ , the optimal solution  $(\beta_{\text{op}}, \theta_{\text{op}})$  with maximum efficiency in an IPT system has been obtained. From (25) and (26), it is clear that the optimal solution needs the value of  $M$ . In order to realize a dynamic MET control, the mutual inductance should be estimated dynamically by a simple measurement.

According to (9), the peak value of  $i_s$  denoted as  $|i_{s\_peak}|$  is given by

$$|i_{s\_peak}| = \frac{4V_{in}}{\pi\omega M}. \quad (27)$$

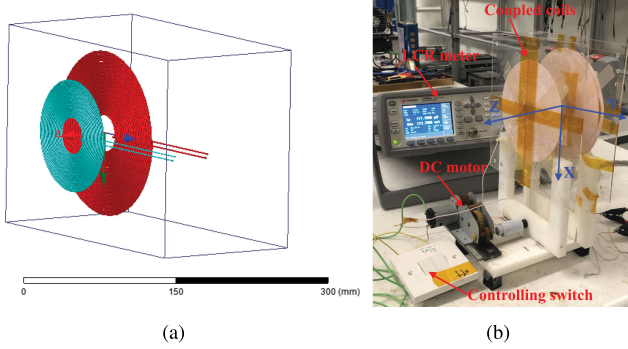


Fig. 8. Magnetic coupler coils. (a) Maxwell's simulation model of magnetic coupler coils. (b) Experimental setup of the magnetic coupler coils and misalignment control.

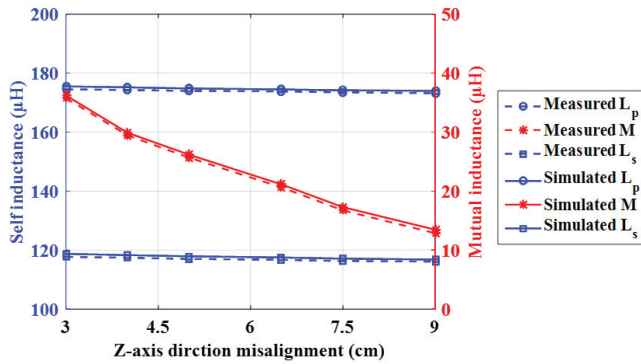


Fig. 9. Comparisons of the simulated and measured results.

It can be observed that  $|i_{s\_peak}|$  is a function of the input voltage  $V_{in}$ , operating angular frequency  $\omega$  and mutual inductance  $M$ . Since  $V_{in}$  and  $\omega$  are known,  $|i_{s\_peak}|$  can be regarded as inversely proportional to  $M$ . Therefore, we can simply measure  $|i_{s\_peak}|$  to estimate  $M$ , i.e.,

$$M = \frac{4V_{in}}{\pi\omega|i_{s\_peak}|}. \quad (28)$$

#### IV. DESIGN CONSIDERATIONS

##### A. Magnetic Coupler and Misalignment Measurement

A popular circular pad structure of the magnetic coupler is used in our design here, as shown in Fig. 8 with detailed parameters listed in Table II. A simulated model of the magnetic coupler is built using ANSYS Maxwell 2015 as shown in Fig. 8(a) with parameters given in Table II. A KEYSIGHT E4980AL LCR meter is used to measure the self and mutual inductances, as shown in Fig. 8(b). Fig. 9 compares the simulated and measured results of self inductances  $L_p$ ,  $L_s$  and mutual inductance  $M$ . It can be observed that the measured results is nearly identical to the simulated results.

We use the origin, i.e., the distances between the primary coil and secondary coil in the  $X$ -axis,  $Y$ -axis, and  $Z$ -axis being zero, as a reference point. We define the position change between the primary and secondary coils in the  $X$ -axis/ $Y$ -axis direction

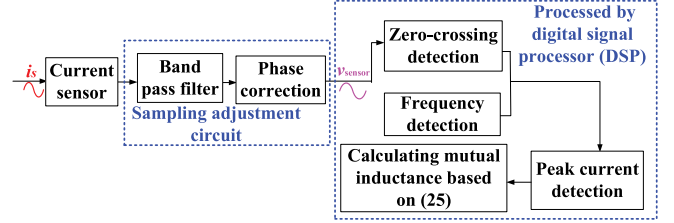


Fig. 10. Diagram of the peak current estimation.

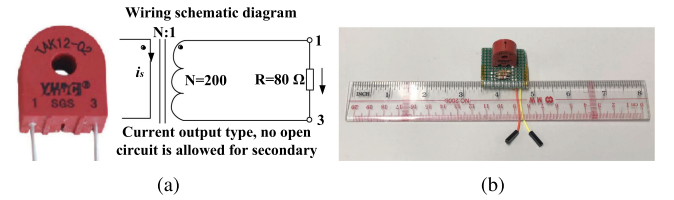


Fig. 11. High-frequency pulse current sensor of TAK12-02. (a) Circuit diagram of the current sensor. (b) Photograph of the current sensor.

relative to the origin as horizontal misalignment, and the change in  $Z$ -axis as vertical misalignment. In this article, we adopt a dc motor to modulate the position of the secondary coil in the  $Z$ -direction for a corresponding change of the mutual inductance, as shown in Fig. 8(b).

##### B. Peak Current Sampling and High Frequency Current Sensor

Using an analog-to-digital (AD) module of a digital signal processor (DSP), the sampling of current can be triggered by a flag signal in a register counter. The process of peak current detection is shown in Fig. 10. First, the secondary current  $i_s$  is sampled by a high-frequency pulse current sensor, as shown in Fig. 11. Then, the sampled signal is sent to a band-pass filter to eliminate the high frequency component and perform a phase correction. Next, the signal is sent to an ultra-fast amplifier to perform the zero-crossing detection. Finally, the zero-crossing point is taken as flag signal sending to the DSP, and after a time delay of one quarter ( $1/4$ ) period, the DSP triggers the AD module to sample the current  $|i_{s\_peak}|$ .

The phase between the actual  $i_s$  and the measured signal  $v_{sensor} = \frac{i_s R}{N}$  is important to guarantee the accuracy of the estimated mutual inductance. The circuit of the pulse current sensor with  $N = 200$  and  $R = 80 \Omega$  is shown in Fig. 11(a). A comparison of waveforms of  $i_s$  and  $v_{sensor}$  at  $|i_{s\_peak}| = 5 \text{ A}$  is shown in Fig. 12. It is clear that  $i_s$  and  $v_{sensor}$  are in phase to give the accurate calculation of  $M$ .

##### C. Overall Control

An overall control is shown in Fig. 13. The output voltage  $V_o$  and current  $I_o$  are sampled and then sent to the DSP. The output power  $P_o$  can be calculated through a multiplier in the DSP. A PI controller is used to regulate the output power with reference to the power  $P_N$ . Meanwhile, the secondary side peak current is sampled and the mutual inductance  $M$  can be calculated



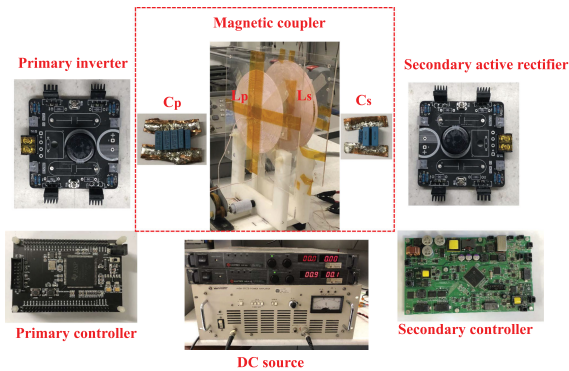


Fig. 16. Photograph of the experimental prototype.

theoretical optimal solution is  $(\beta_{op1}, \theta_{op1}) = (0.58\pi, 0.23\pi)$  at  $M = 21.66 \mu\text{H}$ , and  $(\beta_{op2}, \theta_{op2}) = (0.82\pi, 0.33\pi)$  at  $M = 36.15 \mu\text{H}$ . It can be found that the simulated  $\theta$  is comparable with the theoretical value, while the simulated  $\beta$  is slightly larger than that of the theoretical lossless value after the feedback control is included because a slightly larger  $\Delta\beta$  is needed to compensate for the system loss.

In Fig. 15,  $v_{DA}$  is the sampled peak of  $v_{\text{sensor}}$ , which tracks  $i_s$  well. In the experiments, in order to observe the estimation results directly, the estimated value of  $M$  in the DSP is converted to an analog signal by a digital-to-analog (DA) module. Here, we adopt DAC8501E as the DA module, as shown in Fig. 14.

### B. Experimental Verification

An experimental prototype is built, as shown in Fig. 16, to verify the effectiveness of our proposed dynamic MET control. The parameters of the prototype are listed in Table III. Both primary and secondary sides adopt the DSP TMS320F28335 as the microcontrollers. All voltages and currents are captured by a Tektronix DPO 4104 Oscilloscope.

The experimental results are shown in Fig. 17, which have good agreements with the simulation results shown in Fig. 15, where positions A and B represent distances of 3 and 6.4 cm, respectively, in the Z-direction between the primary and secondary coils, which correspond to the measured mutual inductances of 36.15 and 21.66  $\mu\text{H}$ , respectively.

Fig. 17(a) shows the dynamic experimental waveforms with the mutual inductance changing from 36.15  $\mu\text{H}$  in position A to 21.66  $\mu\text{H}$  in position B, and Fig. 17(d) shows the movements from position B to position A. Fig. 17(b) gives the steady-state waveforms in position B and Fig. 17(e) gives the steady-state waveforms in position A. It is clearly the  $v_{\text{sensor}}$  can well track the secondary peak current  $i_s$  both in dynamic and steady state and the output of DA module  $v_{DA}$  can well track the peak envelope of  $v_{\text{sensor}}$ . This verifies that our designed control strategy can well estimate the mutual inductance. Fig. 17(c) and (f) shows the steady-state waveforms of  $v_p$ ,  $i_p$ ,  $v_s$  and  $i_s$  at positions B and A, respectively. It can be observed that ZVS is achieved and the optimal solutions are identical to the simulated and theoretical values.

TABLE IV  
COMPARISON OF OPTIMAL SOLUTIONS

Unit (rad)	Theoretical	Simulated	Experimental
$\beta_1$	$0.82\pi$	$\approx 0.83\pi$	$\approx 0.88\pi$
$\theta_1$	$0.33\pi$	$\approx 0.33\pi$	$\approx 0.33\pi$
$\beta_2$	$0.58\pi$	$\approx 0.60\pi$	$\approx 0.63\pi$
$\theta_2$	$0.22\pi$	$\approx 0.22\pi$	$\approx 0.22\pi$

### C. Measured Results Analysis

Fig. 18 shows the estimated results of mutual inductance under six different positions. In order to improve the accuracy of the identification results, the highest and lowest point envelopes of  $i_s$  are continuously sampled, and the average value is used to solve the mutual inductance. It can be observed that the values of estimation error  $\xi = \frac{|\text{Measured } M - \text{Estimated } M|}{\text{Measured } M} \times 100\%$  are all less than 4%, which show that our proposed method of estimating mutual inductance is feasible and accurate. In addition, we can observe that  $\xi$  increases slightly with increasing misalignment. This indicates that the proposed method is more accurate when the coupling of the coils is stronger. It can be observed that with an increase in  $M$ ,  $\beta$  would also increase. Since  $\beta \in [0, \pi]$ , using (28) and the system parameters listed in Table III, the estimated range of  $M$  is 0–45.53  $\mu\text{H}$ . However, from Fig. 18, it can be observed that with the decrease of  $M$ , the estimated error  $\xi$  would increase. Thus, to improve the estimation accuracy, e.g.,  $\xi < 4\%$ ,  $M$  should be larger than 13.46  $\mu\text{H}$ .

The powers and efficiencies are measured by a precision power scope YOKOGAWA PX8000. The captured screen of the measured results of position A and position B are shown in Fig. 19. The measured maximum efficiency curve under the six positions is shown in Fig. 20. It can be observed that the maximum efficiency is 93.6% under a strong magnetic coupling at  $M = 36.15 \mu\text{H}$ , while the minimum efficiency is 88.3% under a weak coupling at  $M = 21.66 \mu\text{H}$ . With increasing distance between the primary and secondary coils, i.e., decreasing  $M$ , the efficiency decreases as a larger current is needed to get the same power.

A summary of the control angles used for theoretical calculation, simulation and experiment are listed in Table IV. The column under ‘‘Theoretical’’ are two sets of control angles calculated directly from (25) and (26) at  $M = 36.15 \mu\text{H}$  and 21.66  $\mu\text{H}$ , respectively. The columns under ‘‘Simulated’’ and ‘‘Experimental’’ are the corresponding control angles compensated by the control as shown in Fig. 13 at steady state. Both the theoretical calculation and simulation include the same conduction loss. The experiment includes conduction loss, switching loss, and all other losses. The control angle  $\beta$  becomes larger with more loss after feedback compensation is applied, as shown in Fig. 13.

A comparison of the theoretical, simulated and experimental system efficiencies for  $M = 36.15 \mu\text{H}$  and 21.66  $\mu\text{H}$  are listed in Table V, where the theoretical efficiency is calculated by  $\eta = \frac{P_N}{P_N + P_{\text{con-loss}}}$  at the optimal control angles without feedback control. The small deviation of control angles compensated by the control loop accounts for the lower efficiency of

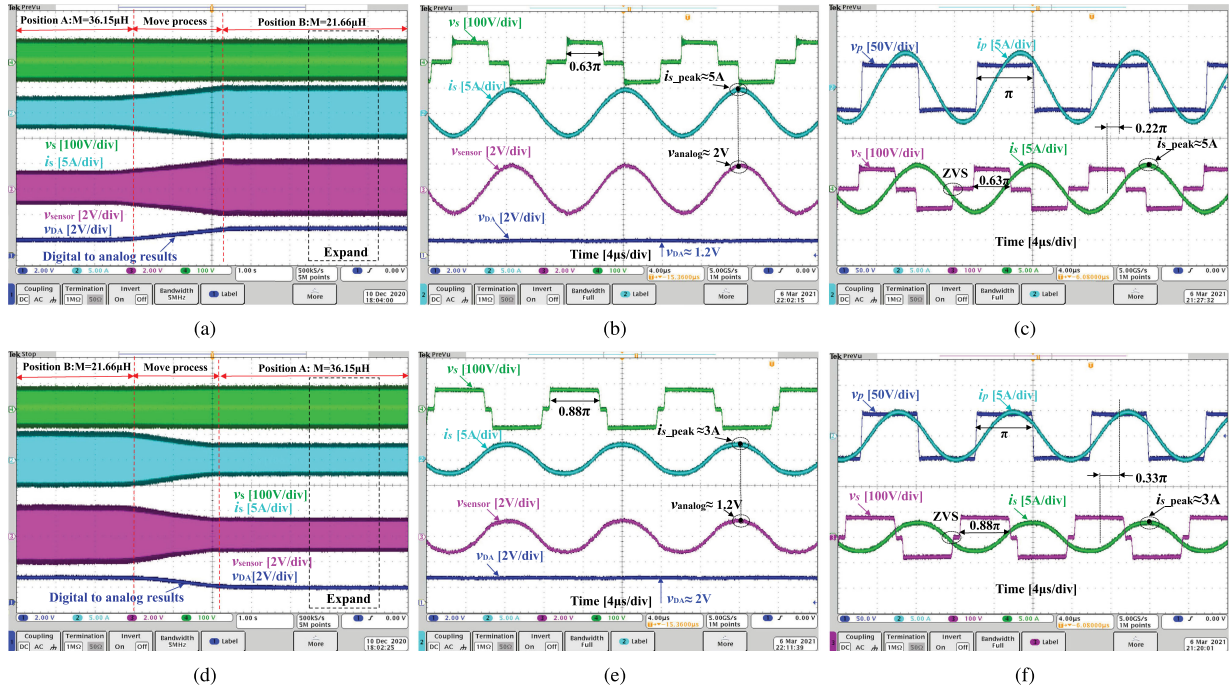


Fig. 17. Experimental waveforms under our proposed dynamic MET control. (a) Transient waveforms moving from position A to position B. (b) Steady-state waveforms at position B. (c) Corresponding steady-state waveforms of  $v_p$ ,  $i_p$ ,  $v_s$  and  $i_s$  at position B. (d) Transient waveforms from position B to position A. (e) Steady-state waveforms at position A. (f) Corresponding steady state waveforms of  $v_p$ ,  $i_p$ ,  $v_s$  and  $i_s$  at position A.

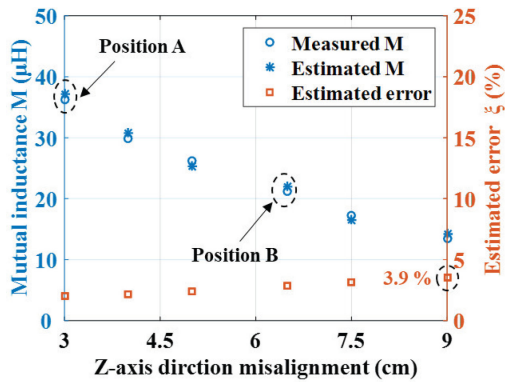


Fig. 18. Comparisons of estimating results with measured values.

TABLE V  
COMPARISON OF EFFICIENCY RESULTS

Efficiency (%)	Theoretical	Simulated	Experimental
$M = 36.15 \mu\text{H}$	96.3%	95.2%	93.6%
$M = 21.66 \mu\text{H}$	92.1%	91.0%	88.3%

the simulated and experimental results. The reason for the differences between the theoretical and experimental efficiency data shown in Table V is that only conduction loss has been used to calculate the theoretical efficiency and the turn-OFF loss is not included. Since  $\alpha = \pi$  and according to Fig. 4, we see that, on the primary side,  $Q_1$  and  $Q_4$  are turned OFF with current  $i_p(t_0)$ , and

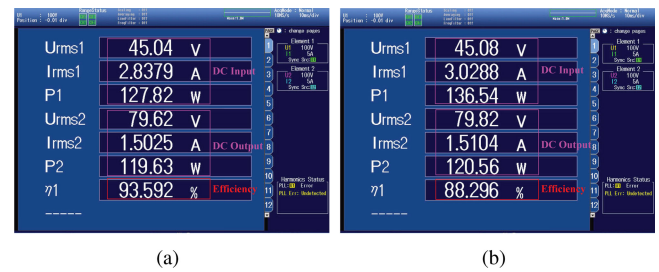


Fig. 19. Screen capture of power analyzer at (a)  $M = 36.15 \mu\text{H}$  and (b)  $M = 21.66 \mu\text{H}$ .

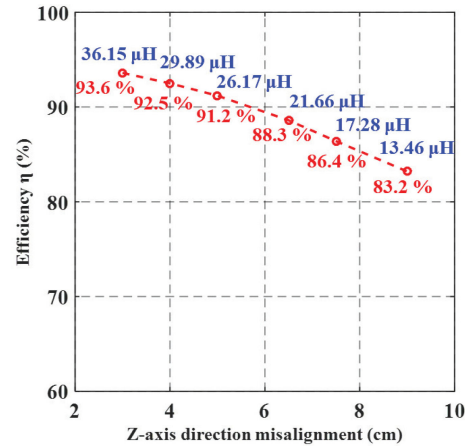


Fig. 20. Measured maximum efficiencies curve under different mutual inductances.

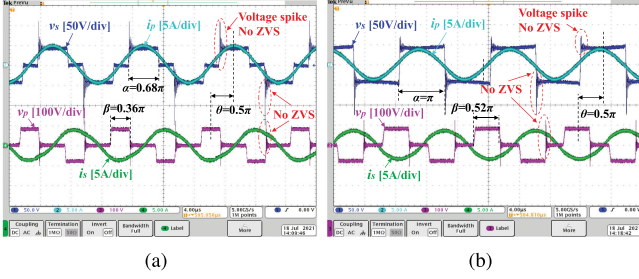


Fig. 21. Experimental steady-state waveforms of  $v_p$ ,  $i_p$ ,  $v_s$ , and  $i_s$  under impedance matching condition under (a)  $M = 21.66 \mu\text{H}$  and (b)  $M = 29.89 \mu\text{H}$ .

$Q_2$  and  $Q_3$  are turned OFF with current  $i_p(t_3)$ . Similarly, on the secondary side,  $Q_5$  and  $Q_8$  are turned OFF with  $i_s(t_1)$  and  $i_s(t_2)$ , respectively, and  $Q_6$  and  $Q_7$  are turned OFF with  $i_s(t_4)$  and  $i_s(t_5)$ , respectively. By symmetry, we have  $|i_p(t_0)| = |i_p(t_3)|$ ,  $|i_s(t_1)| = |i_s(t_4)|$  and  $|i_s(t_2)| = |i_s(t_5)|$ . The turn-OFF loss in the primary and secondary sides can be readily found [24], i.e.,

$$P_{\text{sw},p} = 2 \times \frac{1}{3T} V_{\text{in}} |i_p(t_0)| t_{\text{off}} \quad (29)$$

$$P_{\text{sw},s} = \frac{1}{3T} V_o |i_s(t_1)| t_{\text{off}} + \frac{1}{3T} V_o |i_s(t_2)| t_{\text{off}} \quad (30)$$

where  $t_{\text{off}}$  is the turn-OFF time of the MOSFET, which is approximately equal to the dead time  $t_{\text{de}}$ . According to the optimal theoretical angle variables  $\beta$  and  $\theta$  listed in Table IV, the total turn-OFF losses for  $M = 36.15 \mu\text{H}$  and  $21.66 \mu\text{H}$  can be found as 2.9 and 5.1 W, respectively. Considering the turn-OFF losses, the theoretical efficiencies are 94.2% and 88.7%, respectively, which are close to the measured values of 93.6% and 88.3%.

### D. Efficiency Comparison

The impedance matching control strategy is a popular efficiency optimization method, which can achieve a global minimum conduction loss of an IPT system [22], [23]. A comparison of our proposed optimal control strategy and the impedance matching should be considered.

Fig. 21 shows the steady-state waveforms of impedance matching for  $M = 29.89 \mu\text{H}$  and  $21.66 \mu\text{H}$ . It can be observed that ZVS cannot be achieved, and the high voltage spikes and oscillations would incur a large switching loss. The measured system efficiencies are 89.1% and 85.9% corresponding to  $M = 29.89$  and  $21.66 \mu\text{H}$ , respectively, which are both lower than the measured values of 92.5% and 89.6% using our proposed optimal control scheme shown in Fig. 20.

### E. Transients With Stepping Output Voltage

With the output voltage stepped between 50 and 80 V, the waveforms of  $v_s$ ,  $i_s$ ,  $I_o$ ,  $V_o$  and power  $P_o = V_o I_o$  are measured and shown in Fig. 22(a). Also, Fig. 22(b) and (c) is the corresponding steady-state waveforms for  $V_o = 50$  and 80 V, respectively. It can be observed that  $P_o$  is kept constant at 120 W under step changes of  $V_o$ , verifying the stable constant operation of the converter under stepping output voltage. In

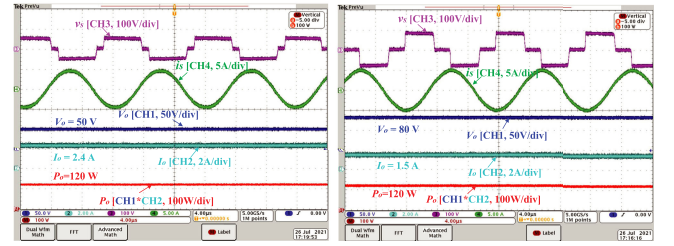
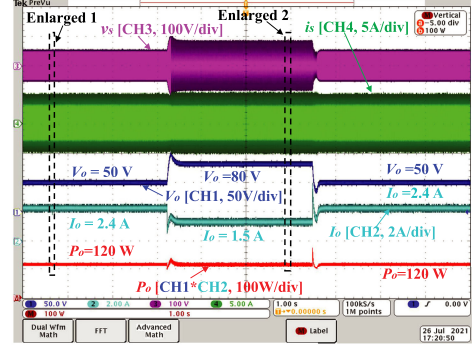


Fig. 22. Experimental waveforms of the IPT system under the proposed control strategy. (a) Transient waveforms of  $V_o$  steps from 50 to 80 V and back to 50 V. (b) Steady state waveforms at  $V_o = 50$  V. (c) Steady state waveforms at  $V_o = 80$  V.

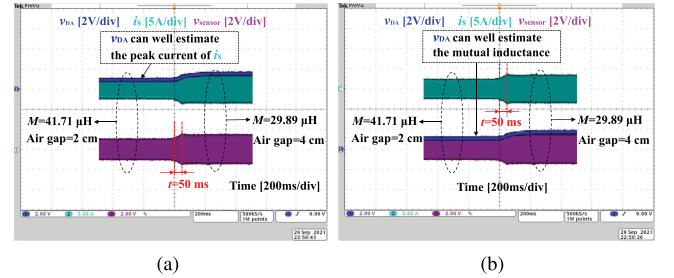


Fig. 23. Experimental transient waveforms of moving from  $M = 41.67 \mu\text{H}$  to  $M = 29.89 \mu\text{H}$ . (a)  $V_{\text{DA}}$  can well track peak envelope of  $i_s$ . (b)  $V_{\text{DA}}$  can well track the peak envelope of  $v_{\text{sensor}}$ .

addition, it can be observed that the peak value of  $i_s$  has no variations in Fig. 22(a), which means that the mutual inductance can be estimated accurately even when the load changes.

### F. Discussions on Practicability

It should be noted that the experimental platform in this article is a scale-down prototype, which is used to imitate the variations of mutual inductance  $M$  in practice. In our experiment, the receiving coil is driven by a 5 V dc motor with a small torque. Thus, the variation speed of  $M$  is slower compared with an actual EV driving on the road.

To speed up the movement of the receiving coil, a mechanical device is used, and the waveforms corresponding to a high-speed receiving coil are shown in Fig. 23. It can be observed that it takes 50 ms to drive the receiving coil to move a gap distance of 2 cm, and the average speed is  $v = 2 \text{ cm in } 50 \text{ ms}$ , i.e., 1.44 km/h.

The radius of transmitting and receiving coils are 48 and 80 mm, respectively, which are much smaller than the coils used in a real EV. Assuming the setup is a 1/15 scale-down model, the change of  $M$  is almost the same as it is at 21.6 km/h in a real-scale IPT system used in an EV. In Fig. 23, it is clear the  $v_{\text{sensor}}$  can well track the secondary peak current  $|i_{s\_peak}|$  in dynamic state and the output of DA module  $v_{\text{DA}}$  can well track the peak envelope of  $v_{\text{sensor}}$ , verifying the ability of our control strategy in estimating the mutual inductance with the receiving side being driven at about 20 km/h over a transmitter.

In addition, the delivering power of 120 W in this article is lower than the usual charging power applied to an EV. For high-power applications, the coil size would be larger, and the actual input voltage  $V_{\text{in}}$  and output voltage  $V_{\text{o}}$  would be higher than those used in this article. According to (25) and (26), the optimal solution  $(\beta_{\text{op}}, \theta_{\text{op}})$  contains parameters of  $V_{\text{in}}$ ,  $V_{\text{o}}$ ,  $M$ ,  $P_{\text{N}}$ ,  $\omega$ , and  $\delta_{\text{min}}$ . Since the input voltage  $V_{\text{in}}$ , operating angular frequency  $\omega$  and the minimum designed ZVS angle  $\delta_{\text{min}}$  are all constants, the optimal solution  $(\beta_{\text{op}}, \theta_{\text{op}})$  only contains three variables, namely,  $M$ ,  $V_{\text{o}}$ , and  $P_{\text{N}}$ , which may change in practice. Also,  $V_{\text{o}}$  can be sampled and  $M$  can be calculated directly using our proposed control strategy. Therefore, for high-power applications with large  $P_{\text{N}}$ ,  $(\beta_{\text{op}}, \theta_{\text{op}})$  can still be calculated in the secondary microcontroller to modulate the IPT system with maximum efficiency. Also, another problem is that the sampling noise is significant at a higher power level, which may affect the accuracy of the estimated  $M$ . Thus, an advanced sampling filter algorithm is needed to reduce the sampling noise, e.g., using a recursive least square filter [25].

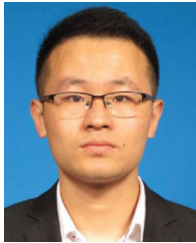
## VI. CONCLUSION

This article presents an effective and fast MET control with a fast mutual inductance estimation (MIE) algorithm for fast tracking of the maximum efficiency point under variation of the gap distance and misalignment of the magnetic coupler of a series-series compensated IPT (SS-IPT) system. The system contains minimum number of power conversion stages, and achieves the best system efficiency. A feedback control of the MET-MIE SS-IPT system is designed without using a wireless communication channel for improved stability and robustness. The effectiveness of the proposed MET-MIE control is validated by simulation and experimental results. It is shown that the maximum efficiency is well tracked with less than 4% error in MIE under significant variation of the gap distance and misalignment of the magnetic coupler.

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