







An Improved Adaptive Selected Harmonic Elimination Algorithm for Current Measurement Error Correction of PMSMs

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I. INTRODUCTION

Abstract—Measurement errors are inevitable in the current sensors, which cause speed ripple including one and twice the stator electrical frequency. For the undesired harmonics, the adaptive selected harmonic elimination (ASHE) algorithm outputs the sum of the sinusoidal signals multiplied by the adaptive weights. In order to solve the current measurement error (CME) issue, this article adopts the ASHE algorithm. According to the deterministic functional relationship of the surface-mounted permanent magnet synchronous motor (SPMSM), the adopted algorithm extracts the harmonics of the steady state speed error, and outputs the q -axis current compensation. However, there is no explicit connection between speed and d -axis current, so their relationship is uncertain. The remaining d -axis CMEs result in poor current performance. Therefore, this article proposes an improved ASHE algorithm, which compensates the dq -axis CMEs simultaneously depending on their mutual deterministic connection. The proposed method does not need motor parameters, additional sensors, or complex calculation process. Finally, the effectiveness of the method is verified by the SPMSM platform. Experimental results also show that the proposed method reduces speed ripple and suppresses the negative effects of CMEs.

Index Terms—Adaptive selected harmonic elimination (ASHE), current measurement errors (CMEs), permanent magnet synchronous motor (PMSM), vector control (VC).

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WITH the advanced power electronic technology, ac machines have dominated the traction machine market [1]. Among various ac machines, permanent magnet synchronous motor (PMSM) has many features, such as operation over a wide torque speed range, high power, density, etc. It receives abundant attention and is widely applied in industrial fields and electrified transportation [2]–[4]. Aiming to attain fine servo performance, relying on sensors to sample electrical signals, modern control technologies perform closed-loop control. Among these control technologies, vector control (VC) is very common. In detail, traditional VC requires two current sensors and an encoder [5], [6]. For the motor drives, current and speed feedback are essential.

Current feedback is generally phase current, which is the voltage signal output by the sensor. It is processed by an analog-digital converter (ADC) through matching circuits and noise filter circuits. Due to the circuit nonlinearity, the operating environment, especially temperature variation, even if the system is well constructed, current measurement errors (CMEs) are still inevitable [7]. CMEs mainly include offset error and scaling error, which generate torque pulsation, subsequently yielding speed ripple of single and double fundamental frequencies [8]–[10]. Therefore, these CMEs need to be restricted or compensated. The simplest method is to update the error correction when the motor is down. However, except that the offset error may change due to thermal drift, and this method not only interferes with normal operation but also fail to handle the scale error. Hence, different online compensation methods are proposed.

For online compensation of CMEs, some methods use additional sensors. In [8], the dc-bus current is utilized for mutual calibration of sensors. By means of one voltage sensor, [9] and [10] estimate the stator currents and design controllers to eliminate CMEs. Via the torque transducer, [11] obtains the steady state torque error, and iteratively learns to compensate the current references. There are other methods compensating current references, such as filtering the difference between the predicted and measured currents [12] and exploiting the transfer function of torque disturbance to speed error [13]. In [14],

repetitive control is performed depending on the stored voltage errors. Based on the disturbance observer, [15] designs a composite voltage compensator and [16] directly confirms the offset and gains by the positive sequence component estimator. Moreover, [17] analyzes that the integrator output of the d -axis proportional integral (PI) current regulator is constant, subtracts offset errors, and rescales the gains. By injecting high-frequency voltage, [18] acquires the positive and negative sequence currents to scale the gains. In [19], with isolation and decoupling matrix, the regulator estimates the gains by minimizing the current differential gains. Although above methods compensate CMEs, they may use additional sensors, rely on motor parameters, or have a complicated calculation process.

In addition, there is a classic adaptive notch canceller that eliminates sinusoidal interference in digital signal processing [20]. For power electronic applications, [21] proposes an adaptive select harmonic elimination (ASHE) algorithm, which only requires knowledge of the harmonic frequency. The general framework, theories and methods of harmonic component elimination is described in [22]. In terms of specific applications, [23] applies adaptive filters to shunt active power filters to improve the transient response time of harmonic detection. Besides, the ASHE algorithm is introduced to a three-level T-type inverter to eliminate the 5th-31st harmonics [24]. Regarding motor drives, [25] uses the same structure to diminish the harmonics in the rotor estimation error of sensorless control. Based on the least mean square (LMS) algorithm, [26] compensates the voltage references and suppresses deadtime current distortion in VC. In general, the sole function of ASHE algorithm is to eliminate undesirable higher-order harmonics from the selected variable.

Correspondingly, CMEs cause torque pulsation, thereby resulting in speed ripple with single and double fundamental frequencies. This article adopts the ASHE algorithm to reduce speed ripple of the surface-mounted PMSM. Through the deterministic functional relationship, speed ripple originates from q -axis CMEs. The adopted ASHE algorithm outputs the q -axis current compensation, which reduces speed ripple. However, the d -axis CMEs are not compensated, resulting in poor current performance. Furthermore, the relationship between speed and d -axis current is uncertain. In order to completely suppress the negative impact of CMEs, this article improves the ASHE algorithm. Considering that the dq -axis CMEs are the weighted sums of sinusoidal signals, their mutual connection is deterministic. Then, the d -axis current compensation can be obtained by adaptive weights of the ASHE algorithm. The dq -axis CMEs are compensated simultaneously and respectively. Without motor parameters, additional sensors or complex calculation processes, the proposed method reduces speed ripple and suppresses the negative effects of CMEs.

This article is organized as follows. In Section II, the PMSM model, CMEs and related limits of traditional method are illustrated. In Section III, the principle and implementation of the ASHE algorithm, further improvement, and application are presented. The experimental results are shown in Section IV. Finally, Section V concludes the article.

II. EFFECTS OF MOTOR CMEs

A. Mathematical Model of PMSMs

Aiming at the CMEs of various motors, this article takes the PMSM as an example. In the dq -synchronous reference frame, the mathematical model of PMSM is as follows:

$$\begin{aligned} \frac{di_d}{dt} &= -\frac{R_s}{L_d}i_d + \frac{L_q\omega_e}{L_d}i_q + \frac{1}{L_d}u_d \\ \frac{di_q}{dt} &= -\frac{L_d\omega_e}{L_q}i_d - \frac{R_s}{L_q}i_q + \frac{1}{L_q}u_q - \frac{\psi_{PM}\omega_e}{L_q} \\ J\frac{d\omega_m}{dt} &= T_e - T_L \end{aligned} \quad (1)$$

where u_d and u_q are the stator dq -axis voltage, i_d and i_q are the stator dq -axis current, L_d and L_q are dq -axis inductance, ψ_{PM} is the permanent magnet flux linkage, R_s is the stator winding resistance, ω_e is the electrical angular speed, $\omega_e = p\omega_m$, p represents the number of pole pairs, and ω_m is the mechanical angular speed. Finally, J , T_e , and T_L are the rotational inertia, the electrical torque, and load torque, respectively.

As for the traditional VC with $i_d^* = 0$ (i.e., maximum torque per ampere in torque control), or the surface-mounted permanent magnet synchronous motor (SPMSM), whose stator inductance $L_s = L_d = L_q$, the electromagnetic torque can be described as

$$\begin{aligned} T_e &= 1.5p(\psi_{PM}i_q + (L_d - L_q)i_di_q) \\ &= 1.5p\psi_{PM}i_q = k_T i_q. \end{aligned} \quad (2)$$

Substituting (2) into the motor motion equation in (1), the relationship between speed and q -axis current can be obtained

$$J\frac{d\omega_m}{dt} = k_T i_q - T_L. \quad (3)$$

Thus, the relationship between current and speed is established through the connection of torque, current, and speed.

B. Analysis of CMEs

The stator current is first converted into a voltage signal by the sensor, and then discretized into a digital value by a low-pass filter and ADC. The factors that may cause CMEs include the sensor itself, signal processing circuits, differences between sampling circuits, discrete errors in ADC, and other factors such as thermal drift, magnetic field interference, etc. [20]. Therefore, CMEs inevitably exist under these factors.

Usually, the classic three-phase three-wire circuit topology uses two sensors to measure any two-phase currents. This article takes phases a and b as an example, and phase c current is obtained by Kirchhoff's current law. Then, the measured values of the three-phase currents are expressed as

$$\begin{cases} i_{a_mea} = k_a i_{a_act} + \Delta i_{a_offset} \\ i_{b_mea} = k_b i_{b_act} + \Delta i_{b_offset} \\ i_{c_mea} = -i_{a_mea} - i_{b_mea} \end{cases} \quad (4)$$

where i_{x_mea} and i_{x_act} , $x = a, b, c$, are the measured and actual values of three phase currents, and such as phase a , k_a , and Δi_{a_offset} are the offset error and scaling error, respectively.

Derived from (3), the transfer function of the motor plant is

$$G_p(s) = \frac{k_T}{J s}$$

$$G_p(z) = G_p(s) \Big|_{s=\frac{2}{T} \frac{z-1}{z+1}} = C_p \left(\frac{2z-1}{Tz+1} \right). \quad (11)$$

The input and output of (11) are the q -axis current and speed, respectively, which is applied to the subsequent ASHE algorithm. As shown in Fig. 2, the transfer function of the speed loop is

$$G_t(s) = \frac{k_T k_{p\omega} s + k_T k_{i\omega}}{J s^2 + k_T k_{p\omega} s + k_T k_{i\omega}}. \quad (12)$$

The speed loop can suppress the constant disturbance caused by the friction torque T_f and load torque T_L . In [28], pulsating torque in PMSM is usually generated by various sources, including cogging torque, flux harmonics, and current sensor errors. It is composed of the 1st, 2nd, 6th, and 12th harmonics with the fundamental is the synchronous frequency. The bandwidth of the load inertia and speed loop eliminates higher-order harmonics, but the middle and low frequency ripples within the bandwidth may still cause speed ripple. This article mainly focuses on the first and second harmonics caused by CMEs.

III. IMPROVED ASHE CORRECTION STRATEGY

Since CMEs cause the first and second harmonics of the motor speed. This article improves the ASHE algorithm that eliminates undesirable speed harmonics. The idea of the proposed method derives from the characteristics of CMEs, that is, the dq -axis current errors are sinusoidal signals. The classic ASHE algorithm eliminates the harmonics of the selected frequency from the target, and outputs the sum of sinusoidal signals with adaptive weights. The improved ASHE algorithm aims to suppress the speed ripple by separately compensating the dq -axis current.

A. Classical ASHE

The LMS adaptive algorithm is characterized by parallel computation, online adaptation, and simple implementation. The classical ASHE algorithm uses the LMS algorithm to update the weights online [24], and its structure is shown in Fig. 3. The reference signals $x_c(k)$ and $x_s(k)$ are sinusoidal references, k is the moment index, and T is the sampling period. In $x_c(k)$ and $x_s(k)$, the frequency $\omega_h = 2\pi f_h$ is the selected harmonic to be eliminated from primary input signal $d(k)$, $\varepsilon(k)$ is an error estimate, and $y(k)$ is the output signal. The error estimate $\varepsilon(k)$ is as follows:

$$\begin{aligned} \varepsilon(k) &= d(k) - y(k) \\ &= d(k) - \mathbf{X}^T(k) \mathbf{w}(k) \end{aligned} \quad (13)$$

where $\mathbf{X}(k)$ is the reference vector and $\mathbf{w}(k)$ is weight vector, they are defined as

$$\begin{aligned} \mathbf{X}^T(k) &= [x_c(k) \ x_s(k)] = [\cos \omega_h k T \ \sin \omega_h k T] \\ \mathbf{w}^T(k) &= [w_c(k) \ w_s(k)]. \end{aligned} \quad (14)$$

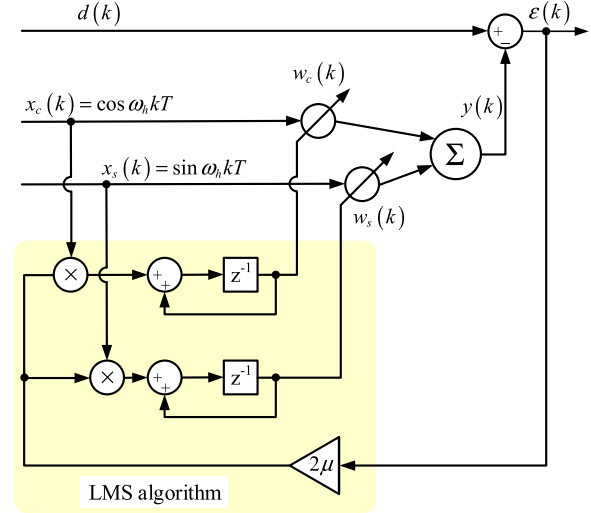


Fig. 3. Structure of the classical ASHE algorithm.

The multiplication of the above two vectors can be used to match the amplitude and phase of the sinusoidal interference in the primary input signal. With the LMS algorithm, the adaptive update of weights can be expressed as

$$\mathbf{w}(k+1) = \mathbf{w}(k) + 2\mu \cdot \mathbf{X}(k) \cdot \varepsilon(k) \quad (15)$$

where μ is the adaptation gain constant, it regulates the convergence speed and algorithm stability. By analyzing the signal propagation in Fig. 3, the mechanism of the classical ASHE algorithm is illustrated [26]. The transfer function $G(z)$ from $\varepsilon(k)$ to $y(k)$ in the z -domain is

$$G(z) = \frac{2\mu(z \cos \omega_h T - 1)}{z^2 - 2z \cos \omega_h T + 1}. \quad (16)$$

B. Adopting Classical ASHE for q -Axis Current Compensation

In this article, the purpose is to suppress speed ripple caused by CMEs, and the ASHE algorithm is adopted. When the ASHE algorithm is applied, the plant should be considered. Thus, the output $y(k)$ is multiplied with the inverse transfer function $G_p^{-1}(z)$ of the plant. In detail, the input $d(k)$ is the speed tracking error, the selected frequency ω_h is the stator electrical frequency corresponding to the speed reference, and the q -axis current compensation i_{q-ASHE} is the output. The structure diagram is shown in Fig. 4, including the motor speed control system model and the ASHE algorithm with $G_p^{-1}(z)$. $\bar{\omega}$ is the speed error without the influence of CMEs, and ε_ω is the speed error after the influence of the q -axis CMEs Δi_q , including $\bar{\omega}$ and speed harmonics $\Delta\omega$, $\tilde{\omega}$ are the compensated speed corresponding to i_{q-ASHE} , and $\hat{\omega}$ is the speed error after compensation. The principle is that after compensation, the speed error ε_ω should be significantly reduced. $G_p^{-1}(z)$ is obtained from (11)

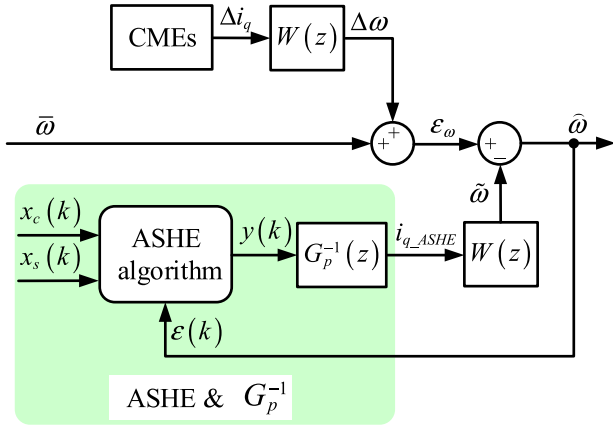
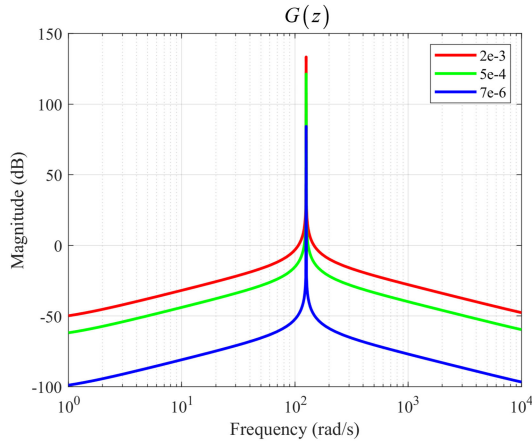


Fig. 4. Current compensation based on the ASHE algorithm.

Fig. 5. Frequency response of $G(z)$ with different μ .

$$G_p^{-1}(s) = \frac{Js}{k_T}$$

$$G_p^{-1}(z) = G_p^{-1}(s) \Big|_{s=\frac{2}{T} \frac{z-1}{z+1}} = G_p^{-1} \left(\frac{2}{T} \frac{z-1}{z+1} \right). \quad (17)$$

In addition, $W(z)$ is the transfer function, which represents the dynamic response of the q -axis current to the speed. $W(z)$ is expressed as

$$W(s) = \frac{\Delta\omega(s)}{\Delta i_q(s)} = \frac{\tilde{\omega}(s)}{i_{q,ASHE}(s)} = \frac{k_T s}{Js^2 + k_T k_{p\omega} s + k_T k_{i\omega}}$$

$$W(z) = W(s) \Big|_{s=\frac{2}{T} \frac{z-1}{z+1}} = W \left(\frac{2}{T} \frac{z-1}{z+1} \right). \quad (18)$$

The transfer function $G(z)$ of the ASHE algorithm can better illustrate the extraction of harmonic components. Fig. 5 shows the frequency response curve of $G(z)$ with different step size μ . The selected frequency ω_h is 40π rad/s. If 40π rad/s is the second harmonic, the corresponding motor fundamental electrical frequency should be 10 Hz, and the mechanical speed should be 150 r/min. Through $G(z)$, the frequency ω_h part of

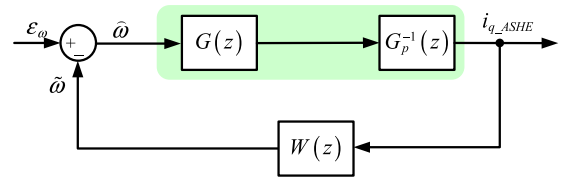
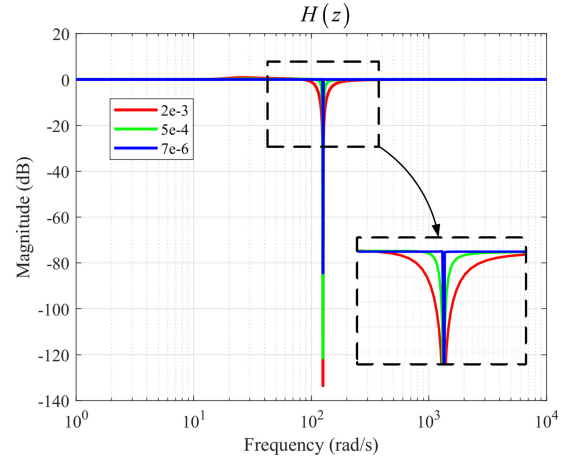


Fig. 6. Block diagram of the ASHE algorithm applied to current compensation.

Fig. 7. Frequency response of $H(z)$ with different μ .

the error $\varepsilon(k)$ is significantly increased, and the gain degree is positively related to the step size.

In order to analyze the ASHE algorithm's influence on the speed error, the block diagram from the speed error ε_ω to the q -axis current compensation is shown in Fig. 6. The transfer function $H(z)$ from ε_ω to $\tilde{\omega}$ in the z -domain is

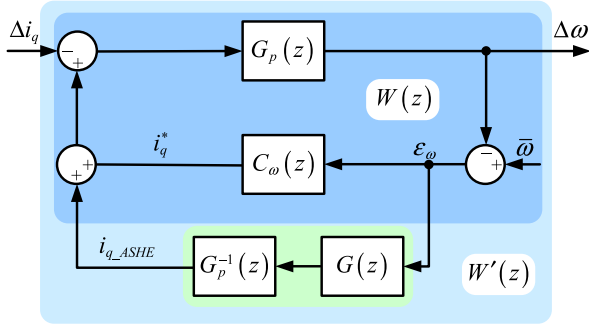
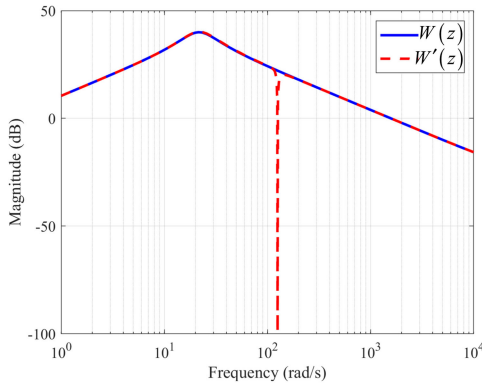
$$H(z) = \frac{1}{1 + W(z)G(z)G_p^{-1}(z)}. \quad (19)$$

The frequency response of $H(z)$ with different step size μ is shown in Fig. 7. It can be seen that the ASHE algorithm actually realizes the function of a notch filter. Fig. 7 shows that the gain of the target frequency is greatly reduced with a narrow notch. On the other hand, at other frequencies, the gain keeps 0 dB. This means that the proposed method can greatly mitigate the second harmonic component of the speed without affecting other frequency components. As step size μ increases, the notch range becomes wider and the attenuation is aggravated accordingly. Conversely, reducing step size μ will result in unsatisfactory notch effects and slow convergence. Therefore, the step size μ can neither be too large nor too small, and an appropriate value should be selected.

Using the ASHE algorithm alters the dynamic response of the q -axis current to the speed. The block diagram is shown in Fig. 8, where $G_\omega(z)$ is the speed PI controller

$$C_\omega(s) = \frac{k_{p\omega}s + k_{i\omega}}{s}$$

$$C_\omega(z) = C_\omega(s) \Big|_{s=\frac{2}{T} \frac{z-1}{z+1}} = C_\omega \left(\frac{2}{T} \frac{z-1}{z+1} \right). \quad (20)$$


 Fig. 8. Equivalent block diagram with q -axis current error after compensation.

 Fig. 9. Frequency response of $W(z)$ and $W'(z)$.

The new transfer function $W'(z)$ is written as

$$W'(z) = \frac{G_p(z)}{1 + G_p(z)(C_\omega(z) + G(z)G_p^{-1}(z))}. \quad (21)$$

Fig. 9 shows the frequency responses of the transfer functions $W(z)$ and $W'(z)$ before and after compensation. The sole difference is that the selected frequency of $W'(z)$ is significantly attenuated. Through the speed error, the applied ASHE algorithm outputs the q -axis current compensation for the motor CMEs.

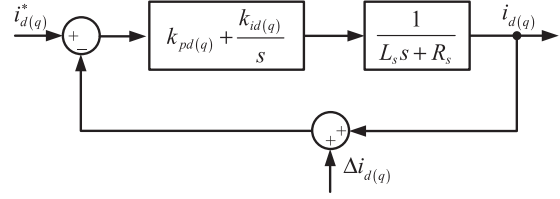
Assuming that the slowly changing weights $w_c(k)$ and $w_s(k)$ are constant, the q -axis current compensation at instant k is

$$\begin{aligned} i_{q_ASHE} &= G_p^{-1}(s)y(k) \\ &= G_p^{-1}(s)(\mathbf{X}^T(k)\mathbf{w}(k)) \\ &= G_p^{-1}(s)(w_c(k)x_c(k) + w_s(k)x_s(k)). \end{aligned} \quad (22)$$

Combining (14) and (17), (22) can be converted to

$$\begin{aligned} i_{q_ASHE} &= \frac{J}{k_T}s(w_c(k)\cos\omega_h kT + w_s(k)\sin\omega_h kT) \\ &= \omega_h \frac{J}{k_T}(-w_c(k)\sin\omega_h kT + w_s(k)\cos\omega_h kT). \end{aligned} \quad (23)$$

For other constant items of reference signals' coefficients, because the LMS algorithm updates the weights adaptively online, they can be ignored. The outputs of the LMS algorithm


 Fig. 10. dq -axis current block diagram.

is weight vector $(\mathbf{w}^*)^T = [w_c^*(k) w_s^*(k)]$ combined with the constant terms, so (23) is rewritten as

$$i_{q_ASHE} = w_s^*(k)\cos\omega_h kT - w_c^*(k)\sin\omega_h kT \quad (24)$$

where

$$\begin{cases} w_c^*(k) = \omega_h \frac{J}{k_T} w_c(k) \\ w_s^*(k) = \omega_h \frac{J}{k_T} w_s(k). \end{cases}$$

Although the weights' signs change, the calculation process of the weight adaptation is still the same as (15)

$$\mathbf{w}^*(k+1) = \mathbf{w}^*(k) + 2\mu \cdot \mathbf{X}(k) \cdot \varepsilon(k). \quad (25)$$

C. Improving ASHE for d -Axis Current Compensation

Through the deterministic function (17), the implemented ASHE algorithm outputs the q -axis current compensation (24). However, even if the q -axis current compensation reduces the speed ripple, it fails to thoroughly suppress the negative effects of CMEs. In the traditional VC method, when the back EMF is ignored, the current loop model is shown in Fig. 10. The transfer function of the current loop is described as

$$C_{d(q)}(s) = \frac{k_{pd(q)}s + k_{id(q)}}{L_s s^2 + (R_s + k_{pd(q)})s + k_{id(q)}}. \quad (26)$$

Since (26) is a second-order transfer function, the dq -axis current harmonics generated by CMEs cannot be eliminated by current closed loop alone. The applied ASHE algorithm compensates the q -axis CMEs and reduces speed ripple, but does not eliminate the d -axis CMEs, which will lead to poor current performance, whereas, it is remarkable that there is uncertainty in the relationship between d -axis current and speed. Therefore, the ASHE algorithm needs to be improved to simultaneously compensate the dq -axis CMEs.

Then, taking the fundamental frequency f_e as an example, that is $\omega_h = \omega_e$, (7) can be expanded as

$$\begin{cases} \Delta i_d = I_1 \sin(\omega_h kT + \varphi_1) \\ = I_1 \sin \varphi_1 \cos \omega_h kT + I_1 \cos \varphi_1 \sin \omega_h kT \\ \Delta i_q = I_1 \cos(\omega_h kT + \varphi_1) \\ = I_1 \cos \varphi_1 \cos \omega_h kT - I_1 \sin \varphi_1 \sin \omega_h kT. \end{cases} \quad (27)$$

Obviously, the q -axis current compensation output and the dq -axis CMEs are all the weighted sums of sinusoidal signals, so the ASHE weights can also be used to obtain d -axis current compensation. Further improve the ASHE algorithm, combining (24) and (27), the corresponding relationship between the

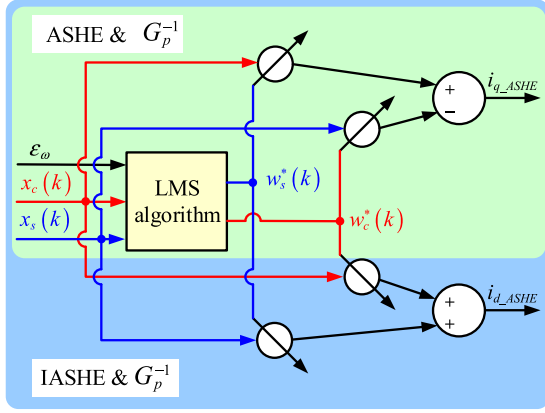


Fig. 11. Block diagram of the IASHE algorithm.

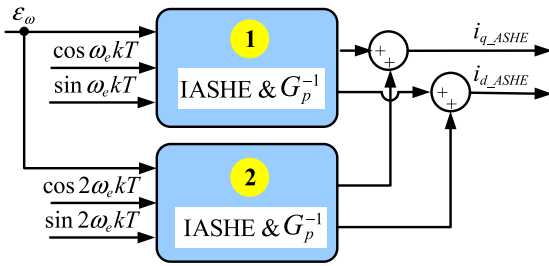


Fig. 12. Block diagram of the IASHE algorithm for the motor CMEs problem.

weights is as follows:

$$\begin{cases} I_1 \sin \varphi_1 = w_c^*(k) \\ I_1 \cos \varphi_1 = w_s^*(k) \end{cases} \quad (28)$$

Thus, the d -axis current compensation is obtained

$$i_{d_ASHE} = w_c^*(k) \cos \omega_h kT + w_s^*(k) \sin \omega_h kT. \quad (29)$$

Using (24), (25), and (29), the proposed method compensates the dq -axis CMEs simultaneously and respectively.

D. Implementation of Improved ASHE on VC

Combined with the improved ASHE (IASHE) algorithm, Fig. 11 shows the block diagram of IASHE algorithm. The inputs are the speed error ε_ω and the reference vector $X(k)$, and the outputs are the dq -axis current compensation i_{d_ASHE} and i_{q_ASHE} . The complexity of the calculation process does not increase. Besides, none of the motor parameters are required.

For other harmonics, such as double fundamental frequency, a second block can be added to the first block of the fundamental frequency to expand and eliminate harmonic components. The IASHE algorithm for the motor CMEs problem is shown in Fig. 12. The added block only changes frequency of the reference signals, and the outputs are summed up accordingly. Furthermore, similar blocks can also be used for other higher-order harmonics.

In terms of traditional VC method, the controller includes two PI regulators, inverse Park transform and SVPWM. Fig. 13 illustrates the implementation of the IASHE algorithm on VC

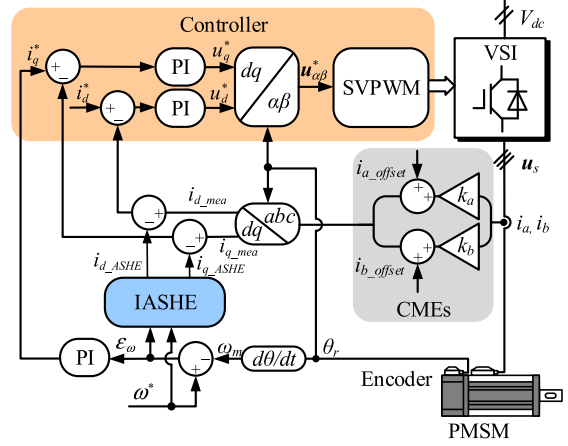


Fig. 13. Implementation of IASHE algorithm on VC method of PMSMs.

TABLE I
SYSTEM PARAMETERS

Symbol	Parameter	Value
P_N	Rated power	0.4 kW
R_s	Resistance	2.35 Ω
L_d / L_q	d -/ q -axis inductance	6.5 mH
Ψ_{PM}	PM flux linkage	0.07876 V·s
p	Number of pole pairs	4
n_N	Rated speed	3000 r/min
J	The moment of inertia	0.0003 kgm ²
T_N	Rated torque	1.27 Nm
i_N	Rated current	2.8 A
k_a	Phase a scaling error	1.01
Δi_{a_offset}	Phase a offset error	0.15 A
k_b	Phase b scaling error	0.98
Δi_{b_offset}	Phase b offset error	-0.1 A

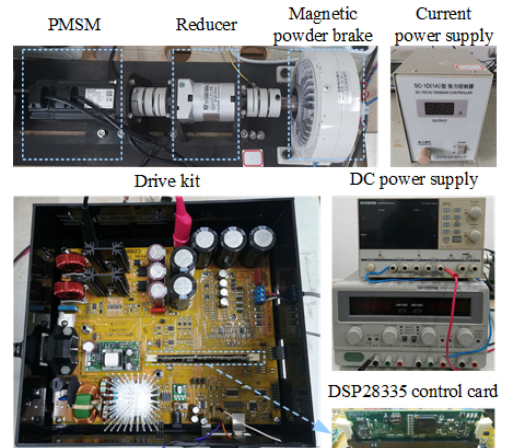


Fig. 14. Experimental platform.

method. The algorithm is designed to compensate the dq -axis synchronous currents. Obviously, the proposed method does not change the traditional control structure. Therefore, the modifications to other modern control technologies are the same as that of VC.

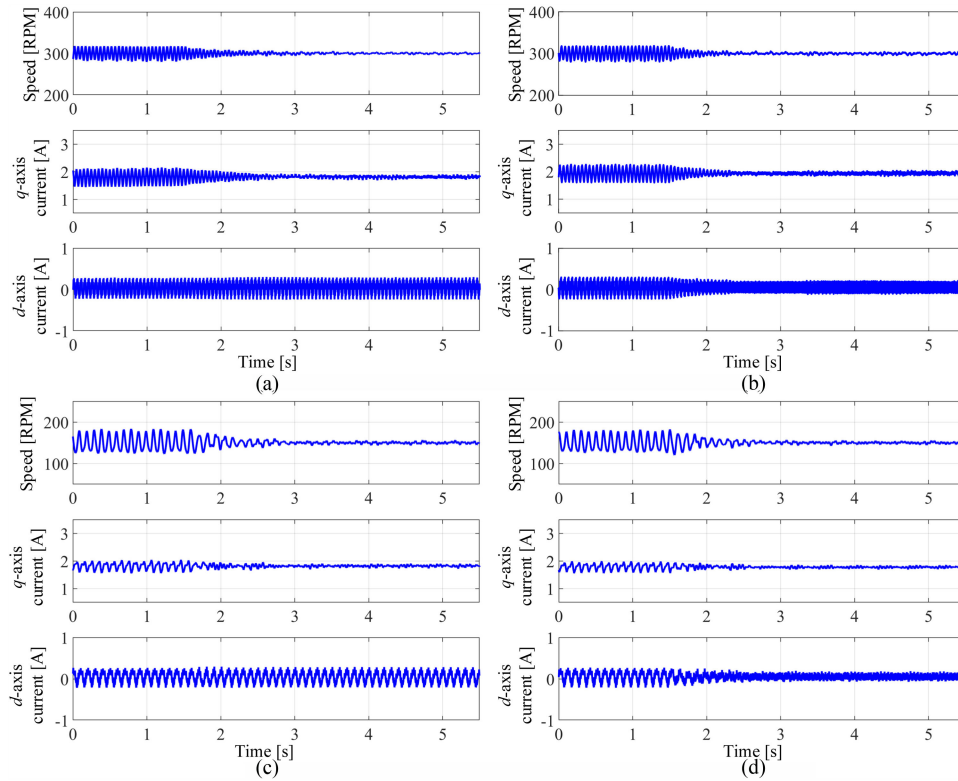


Fig. 15. Waveforms before and after compensation: (from top to bottom) speed, q -axis current, and d -axis current. (a) 300 r/min, ASHE algorithm. (b) 300 r/min, IASHE algorithm. (c) 150 r/min, ASHE algorithm. (d) 150 r/min, IASHE algorithm.

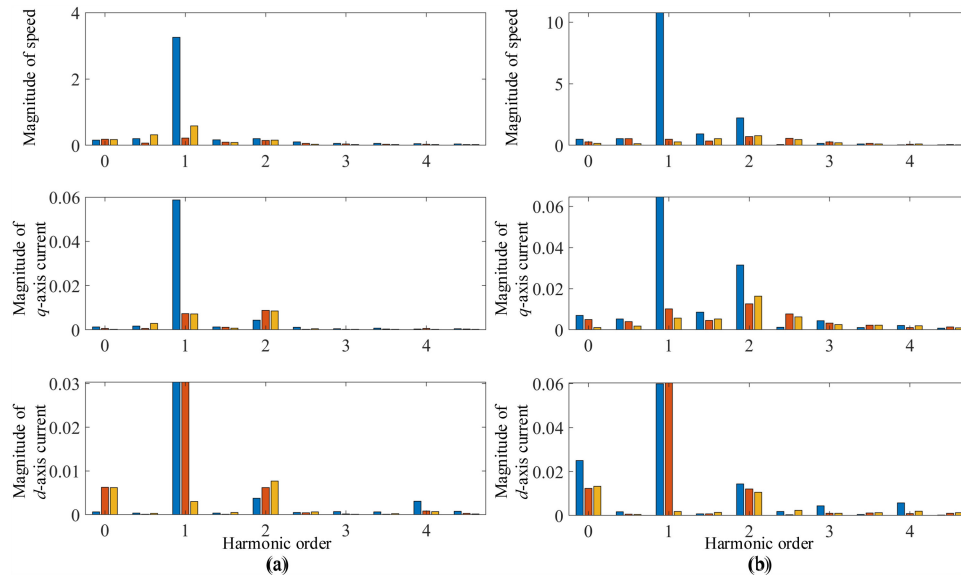


Fig. 16. FFT analysis of speed error, q -axis, and d -axis currents, (blue, red, and orange are without compensation, compensation by ASHE algorithm, and IASHE algorithm). (a) 300 r/min. (b) 150 r/min.

In the proposed method, the key parameter is the step size μ of the LMS algorithm, which is related to the stability of the system and the speed of convergence. Regarding system stability, μ does not allow arbitrary settings. Generally, the larger μ may increase the convergence speed, but also easily triggers instability. On

the other hand, if the step size μ is small, the convergence speed will be slow, resulting in unsatisfactory performance. Therefore, the step size μ should be appropriate, neither too large nor too small. When debugging, a smaller value can be gradually increased to achieve a satisfactory result. This article mainly

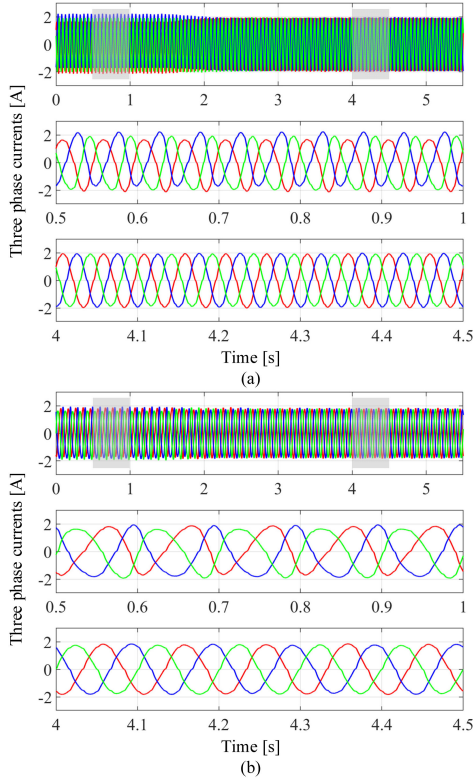


Fig. 17. Three phase currents. (a) 300 r/min. (b) 150 r/min.

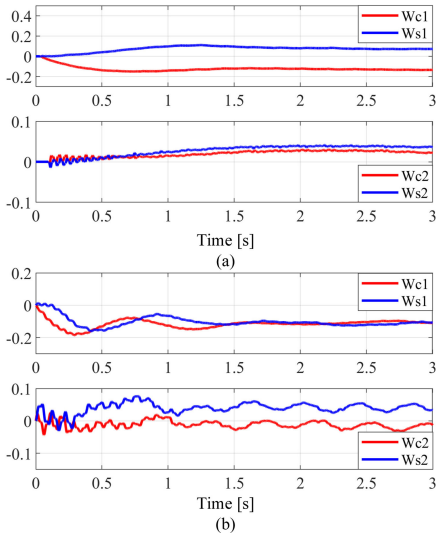


Fig. 18. Weights of IASHE algorithm. (a) 300 r/min. (b) 150 r/min.

tests the effectiveness of the proposed method, so the standard LMS algorithm is adopted with $\mu = 5e - 6$.

IV. EXPERIMENTAL RESULTS

The application of the proposed method in VC has been tested in a SPMSM 2L-VSI drive platform. The system parameters are shown in Table I, and Fig. 14 is the photograph of the equipment. The load side machine is an FZ 25. J magnetic powder brake,

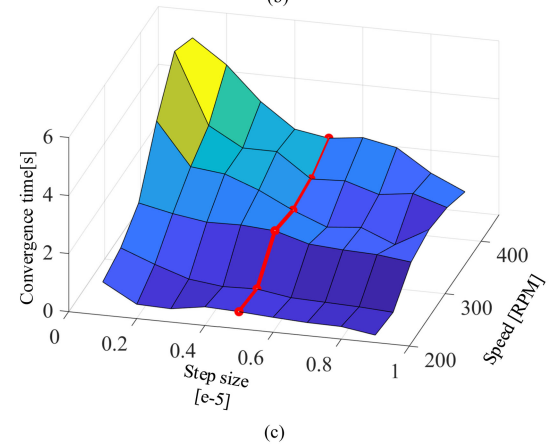
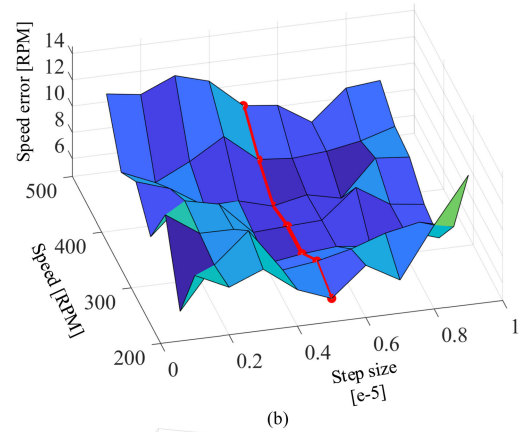
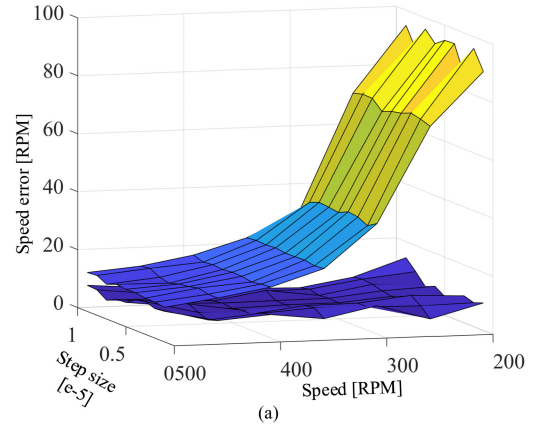


Fig. 19. Experimental results of different step sizes and speeds. (a) Peak-to-peak value measurement comparison of speed ripple error before and after compensation. (b) Peak-to-peak value of speed ripple error after compensation. (c) Convergence time required for stabilization.

which is driven by an SC-1D tension controller. This article uses the DSP-F28335 embedded platform to implement algorithms, and the control period is $62.5 \mu s$, that is, the interrupt frequency is 16 kHz. The currents are sampled through 12-bit ADCs, and the integrated low side resistive shunts are used to measure the currents.

Fig. 15 shows the waveforms before and after compensation using the ASHE and proposed IASHE algorithms with reference speeds of 300 and 150 r/min. Before compensation, CMEs cause

dq -axis current and speed ripples. As the speed increases, the stator electrical frequency and speed harmonic frequency become higher. After the ASHE algorithm performs compensation, the speed and q -axis current ripples are suppressed. However, the d -axis current still has obvious ripple, which indicates that the d -axis CMEs are not eliminated. Using the IASHE algorithm, the d -axis current ripple is also suppressed. The proposed IASHE algorithm compensates dq -axis CMEs and suppresses speed ripple.

Fig. 16 shows the FFT results before and after compensation using the ASHE and proposed IASHE algorithms. When the speed references are 300 and 150 r/min, the stator electrical frequencies are 20 and 10 Hz, respectively. When the speed is 300 r/min, Fig. 16(a) shows that the ripples mainly concentrate on the fundamental frequency. In Fig. 16(b), the speed is 150 r/min and the double fundamental harmonic increases. The reason for this phenomenon is consistent with the analysis in Section II-C: due to the existence of the speed PI regulator and the moment of inertia bandwidth, even if scaling error exists, no higher order harmonics like double fundamental frequency are observed. Compared with the ASHE algorithm, the improved algorithm not only attenuates the harmonics of speed and q -axis current, but also d -axis current.

The three phase current waveforms before and after compensation by IASHE algorithm are shown in Fig. 17. After compensation, the distorted three phase currents are restored to balance. It shows that the simultaneous compensation of the dq -axis current is to correct CMEs. The method proposed in this article suppresses the negative effects of CMEs.

The phenomenon of weights in Fig. 18 also reflects the working mechanism of the proposed method. $Wc1$ and $Ws1$ are the weights of the first block, and $Wc2$ and $Ws2$ represent the weights of the second block. After starting the compensation, the weights change until reaching a stable mutual equilibrium state. These adaptive weights are linearly combined with sinusoidal signals of known electrical frequency to counteract the dq -axis CMEs.

Fig. 19 shows the experimental results of different speeds and step sizes. In Fig. 19(a), as the speed increases, the speed ripple decreases. It is consistent with the above analysis. Due to the bandwidth of the speed PI regulator and the moment of inertia, the higher harmonics of the speed are suppressed. After the compensation of the proposed method, the speed error is significantly reduced. The compensation effect and time of reaching steady state are shown in Fig. 19(b) and (c). As step size increases, the convergence speed increases, and the time for stabilization decreases, but the error reduction effect is not good. Conversely, when step size reduces, the notch effect is not ideal, and the convergence time is greatly increased. Therefore, considering the overall performance, the step size in this article is $5e - 6$, which is the red line part of Fig. 19(b) and (c).

V. CONCLUSION

The problem of CMEs in the motor produces speed and torque ripples with one and twice the stator electrical frequency.

This article proposes a CME correction method for PMSMs. The improved ASHE algorithm is used to directly estimate and compensate the dq -axis CMEs. In terms of performance, speed ripple is suppressed, the three phase currents are restored to balance, and the negative effects of CMEs are suppressed.

The main contributions of this article are that the ASHE algorithm is adopted to solve the CME problem, and compensates q -axis current with the deterministic functional relationship between speed and q -axis current. In addition, for no explicit connection between speed and d -axis current, this article uses the mutual deterministic connection of dq -axis CMEs to obtain the d -axis current compensation.

The proposed method does not require additional sensor, motor parameter, and complex calculation process. Besides, it does not change the structure of modern motor control technologies and has wide applicability. Except for the common VC, the proposed method is suitable for other technologies, such as direct torque control and model predictive control. The higher-order harmonics can also be the targets for the improved ASHE algorithm.

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