

# A Clamped and Harmonic Injected Class-E Converter With ZVS and Reduced Voltage Stress Over Wide Range of Distance in WPT System

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**Abstract**—The inherent frequency of magnetic coupling resonance based wireless power transfer system (MCR-WPT) is up to the level of kHz or even MHz. The class-E converter with zero-voltage switching (ZVS) could eliminate the considerable switching loss, however, the high voltage stress and sensitive ZVS condition to coils distance limit its application seriously in MCR-WPT. To solve the issues, a voltage-clamped class-E converter, consisting of an auxiliary clamped circuit to decrease the voltage stress and a harmonic circuit to realize ZVS against a wide range of coils position, is proposed for the WPT system. According to the harmonic analysis, the relationship among duty cycle, input voltage, amplitudes and phases of the harmonics is obtained. Then, the design strategy for system parameters, especially for the harmonic circuit is presented, so that, ZVS could be maintained over a wide range of coils distance. Meanwhile, the efficiency analysis is also carried out, suggesting a steady high efficiency further. Three design examples with disparate harmonic parameters and ZVS ranges are presented and one of the three examples is selected to make comparison with a typical Class-E WPT system. The experimental results agree with the theoretical analysis well.

**Index Terms**—Class-E converter, harmonic injection, soft switching, voltage stress, wireless power transfer (WPT).

## NOMENCLATURE

$V_{DD}$	Input dc voltage.
$L_C$	Choke inductor.
$C_C$	Clamping capacitor.
$C_S$	Shunt capacitor.
$S, S_a$	Main and auxiliary switches.
$L_n, C_n$	Inductor and capacitor of the $n$ th harmonic circuit.
$L_1, C_1$	Coil's inductance and capacitor of the primary side.
$k$	Coupling coefficient of the coils.
$L_1, C_{11}$	Coil's inductance and capacitor of the secondary side.

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$R$	Real load.
$C_O$	Rectifier capacitor.
$R_L$	Equivalent load considering the voltage drop on the rectifier.
$i_C$	Current of $L_C$ .
$I_C$	Average value of $i_C$ .
$v_{Cc}$	Voltage on $C_C$ .
$V_{Cc}$	amplitude of $v_{Cc}$ .
$i_{CS}$	Current flows through $C_S$ .
$v_{Cs}$	Voltage on $C_S$ .
$V_{Cs}$	Amplitude of $v_{Cs}$ .
$i_S$	Current flows through $S$ .
$i_{Cc}$	Current flows through $C_C$ .
$i_1$	Current in the primary coil.
$I_1$	Amplitude of $i_1$ .
$i_n$	Harmonic current.
$I_n$	Amplitude of $i_n$ .
$i_{11}$	Current in the secondary coil.
$V_{out}, I_o$	Output voltage and current.
$R_e$	Equivalent resistance on the primary side.
$R_{opt}$	Optimal load when class-E realize ZVS/ZDS.
$M$	Mutual inductance.
$v_{hn}$	$n$ th harmonic voltage in $v_{Cs}$ .
$V_{hn}$	Amplitude of $v_{hn}$ .
$v_{fa}$	Fundamental voltage in $v_{Cs}$ .
$V_{fa}$	Amplitude of $v_{fa}$ .
$D$	Conducting duty cycle of $S$ .
$T, \omega$	Period and angular frequency.
$\varphi_1, \varphi_n$	Initial phase of $v_{fa}$ and $v_{hn}$ .
$\theta_1, \theta_n$	Phase of $v_{fa}$ and $v_{hn}$ when $S$ is turned ON.
$\alpha_n$	Phase of $i_{hn}$ when $S$ is turned ON.
$Z_1, Z_n$	Reactance of the harmonic and resonant network.
$Q_{Cs}$	Charge stored in $C_S$ .
$Q_{IC}$	Charge injected by $I_C$ .
$Q_{i1}$	Charge injected by $i_1$ .
$Q_t$	$Q_{IC} + Q_{i1} + Q_{Cs}$ .
$R_S$	Conduction resistance of switches.
$R_n$	Parasitic resistance in harmonic circuit.
$R_{s1}, R_{s11}$	Parasitic resistances in resonant network.
$V_F$	Forward voltage drop of the diode.
$P_{Rn}$	Power loss on $R_n$ .
$P_S$	Power loss on $R_S$ .
$P_{R_{s1}}$	Power loss on $R_{s1}$ .

$P_t$	Total power loss $P_{R_n} + P_S + P_{R_{s1}}$ .
$\eta_p$	Efficiency of the primary side.
$\eta_p$	System efficiency.

## I. INTRODUCTION

**S**TRONG coupled coils can achieve wireless power transfer (WPT) in a few millimeters [1]. However, the frequency and power transfer distance are seriously limited due to the leakage inductance, making it inapplicable in many occasions. Magnetic coupling resonance WPT (MCR-WPT) technology uses capacitor to compensate the leakage inductance, and can keep a high efficiency over a middle distance, up to now, it has been applied in electric vehicles, biomedical implanted devices, and household appliances [2]–[9]. In the MCR-WPT systems, the dc source needs to be transformed to high-frequency ac source, correspondingly, considerable switching loss will be introduced. Zero-voltage-switching (ZVS) is an effective technology to solve this issue [10]. Due to the inherent ZVS and zero-derivative-switching (ZDS) feature, the class-E converter becomes one of the most potential candidates for WPT systems [11]–[14]. Based on the traditional design strategy of the class-E converter, WPT systems could attain a high efficiency under the fixed distance and load. However, for the class-E converter-based WPT system, ZVS and ZDS are sensitive to the coils position and can hardly be maintained during the whole operation process, leading potential safety hazard and low efficiency [15]. To solve this issue, parameters tunable technologies, using dc-feed inductor or switched-capacitor matrixes, have been introduced [16], [17]. In these research works, the value of choke inductor or the parameters of matching network could be adaptively tuned, however, the structures are difficult to be implemented.

ZDS is to avoid the current being reversed before the switch is turned ON. In recent research works, unidirectional switches such as MOSFET have been widely used and ZDS becomes no longer necessary for high efficiency [13]. Correspondingly, many design strategies focus on ZVS operation in a wide range of distance and load have been proposed [18]–[20]. However, another drawback lies in that the voltage stress will be influenced by the coils distance and the load. An uncertain voltage stress may breakdown the switches.

In former research works, adding harmonic circuits is a common method to decrease voltage stress [21]–[27]. In [21] and [22], several of harmonic filters are connected in series with the resonant network and the voltage curve on the switch becomes flat, however, as each harmonic requires a filter, the system is complex. In [23]–[26], a second harmonic circuit with much simpler construction is connected in parallel with the switch and the voltage stress can also decrease to 2.6 times of the input voltage under the optimum condition. Furthermore, in [27], harmonic circuit consisting of two inductors and two capacitors were analyzed, similar to the class F and class E/F converter in [21],[22], the voltage stress can decrease to 2.2 times of the input voltage, but, less passive components are needed in the work.

Unfortunately, even though above research works are effective, following drawbacks are pendent for class-E WPT systems.

- 1) In above researchers, ZVS realization is still on the basis of the reactive current in the resonant network. Namely, there is always a phase difference between the voltage source and the resonant current during the power injection process [20]. This will weaken the power transfer efficiency of the WPT system. How to eliminate the phase difference remains to be solved.
- 2)  $R_e$  of the WPT system is sensitive to the coils distance (the meanings of the symbols are in the nomenclature). In former researchers, after the parameters are determined, ZVS could only be realized when  $R_e$  equals to  $R_{opt}$ , or slightly smaller than  $R_{opt}$ . Because a larger load leads to a smaller resonant current, namely, less charge can be extracted from the capacitor. On the contrary, when  $R_e$  is much smaller than  $R_{opt}$ , the resonant current will become extremely large, and the shunt capacitor may be recharged.
- 3) When the resonant current and the choke current are changed due to the fluctuation of  $R_e$ , the charge injected in the shunt capacitor of the switch will also varies. As the shunt capacitor is small in typical and improved class-E converters, the drain-switch voltage of the switch will fluctuate seriously [28]. Namely, the voltage stress is still unfixed in former research works, leading system security issue [29].

Therefore, decreasing the voltage stress, decoupling the relationship between voltage stress and external factors, widening the ZVS range, and eliminating the phase difference during the power injection process are still pending issues for class-E converter based WPT systems.

In the article, a clamped and harmonic injected class-E converter with much looser ZVS condition, lower and steadier voltage stress, is employed for the WPT system. Compared with the method of reducing voltage stress using harmonic circuit, the clamped circuit in the proposed converter, consisting of an auxiliary switch and a relatively large capacitor, makes the switch voltage waveform become a quasi-square with a lower voltage amplitude. Meanwhile, because of the clamped capacitor, the amplitude of the clamped voltage could hardly be influenced by external factors, therefore, the system security could be enhanced. In the article, the harmonic circuit connected in parallel with the main switch is employed to provide a steady harmonic current to extract the charge of the shunt capacitor, correspondingly, ZVS could always be realized even when  $R_e \geq R_{opt}$ . In addition, since ZVS is achieved through the harmonic current, the phase difference between the switch voltage (defined as  $v_{Cs}$ ) and the main resonant current (defined as  $i_1$ ) is unnecessary for the proposed topology to realize ZVS. Thus, reactive power in the proposed system can be eliminated and the power transfer efficiency can be enhanced.

The rest of the article is organized as follows. In Section II, the circuit is described, and then the principle and harmonic analysis is developed. The parameter design strategy and efficiency analysis are given in Section III. In Section IV, three design examples with different harmonics circuits and ZVS regions are built up to verify the harmonic analysis and the parameter design strategy, furthermore, one case is selected to make comparison with

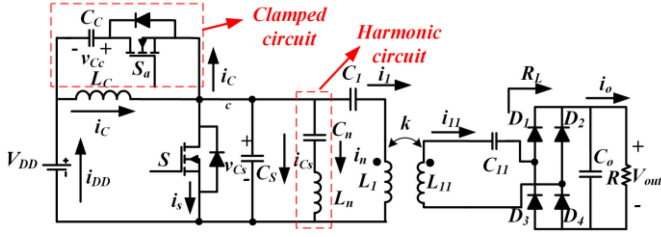


Fig. 1. Configuration of the proposed topology.

typical class-E converter under coils distance change. Finally, a summary is given in the final section.

## II. OPERATION PRINCIPLE DESCRIPTION AND HARMONIC ANALYSIS

### A. Circuit Description

The proposed topology is presented in Fig. 1 and the series compensation network is employed in the receiver.

$V_{DD}$  is the dc supply voltage source.  $L_c$  denotes the choke inductor.  $S$  denotes the main switch, providing circuit path for  $L_c$  and the resonant network.  $C_s$  represents the shunt capacitor across  $S$ , which can ensure ZVS by reducing the climb rate of the voltage.  $L_1$  and  $L_{11}$  represent the inductance of primary and secondary coils. Relying on the mutual inductance between the two coils, the energy can be transformed from the primary side to the secondary side without contact. The capacitors  $C_1$  and  $C_{11}$ , which are placed in series with  $L_1$  and  $L_{11}$ , respectively, are the compensation capacitors for the primary and secondary side of the WPT system.

If only the above components are utilized, a traditional class-E WPT system can be made up. Then, to decrease its voltage stress and realize ZVS, a voltage clamped circuit and a harmonic circuit are introduced.  $S_a$  is the auxiliary switch in voltage clamped circuit, and a relatively large capacitor  $C_c$  is connected in series with it to clamp the voltage on  $S$ .  $C_n$  and  $L_n$  are the capacitor and inductor of harmonic circuit. The  $n$ th harmonic current can flow through the path to extract the charge from  $C_s$ . In addition, a rectifier bridge in parallel with a relatively large capacitor  $C_o$  is applied in the receiver to filter a dc output, and the relationship between equivalent load  $R_L$  and real  $R$  is as follows:

$$R_L = \frac{8R}{\pi^2} + \frac{2V_F}{I_o} \quad (1)$$

where  $V_F$  is the forward voltage drop on single diode and  $I_o$  is the average output current. When  $I_o$  is small, the voltage drop on the diode cannot be negligible.

### B. Operation Principle

As the principle to achieve ZVS by different harmonics is similar, only the third harmonic is selected as an example to analyze. The typical waveform of the WPT system is shown in Fig. 2, and the current-flow path of each mode is shown in Fig. 3. There are six operating modes in one switching period, and they are described as follows.

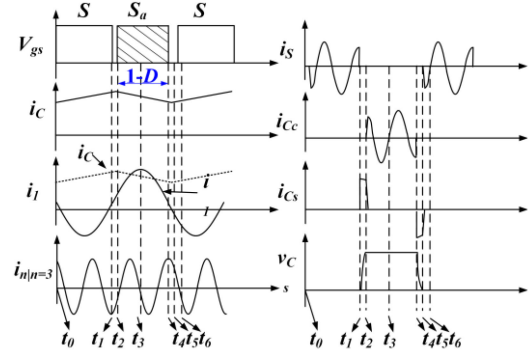
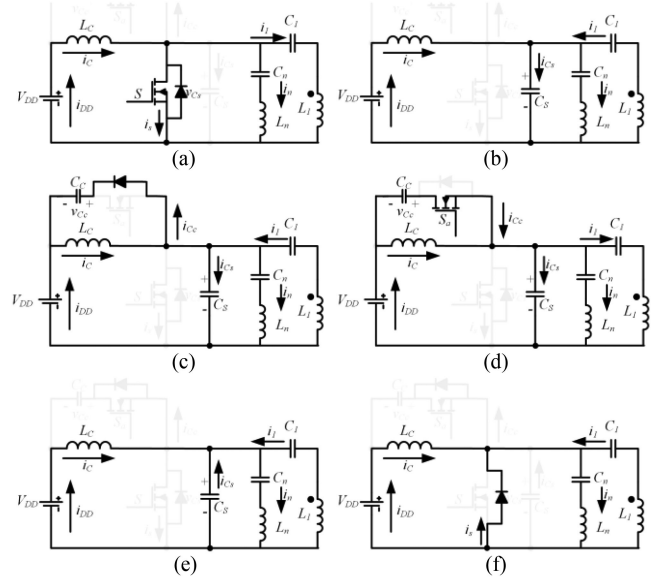


Fig. 2. Key waveform of the WPT system.

Fig. 3. Current loops of each operation mode for the proposed topology. (a) Mode 1 [ $t_0-t_1$ ]. (b) Mode 2 [ $t_1-t_2$ ]. (c) Mode 3 [ $t_2-t_3$ ]. (d) Mode 4 [ $t_3-t_4$ ]. (e) Mode 5 [ $t_4-t_5$ ]. (f) Mode 6 [ $t_5-t_6$ ].

**Mode 1** [ $t_0, t_1$ ]: Before  $t_1$ , the  $S$  is turned ON and  $S_a$  is turned OFF. Choke inductor  $L_c$  is charged by the dc source  $V_{DD}$ , therefore,  $i_c$  increases linearly. Meanwhile, the main resonant current  $i_1$  and the harmonic current  $i_n$  flow through  $S$ . During the mode, the capacitor  $C_c$  is never charged nor discharged.

**Mode 2** [ $t_1, t_2$ ]: During this mode, both  $S$  and  $S_a$  are OFF and  $i_s$  becomes zero.  $C_s$  is charged by  $i_{Cs}$ , which is the sum of  $i_c$ ,  $i_n$ , and  $i_1$ . Due to the voltage clamping feature of  $C_s$ ,  $v_{Cs}$  rises from zero slowly. Then, as both  $i_s$  and  $v_{Cs}$  are about zero at  $t_1$ , zero-voltage turn-OFF is realized on  $S$ . Meanwhile, the main resonant circuit consists of  $C_1$  and  $L_1$  begins to be charged.

**Mode 3** [ $t_2, t_3$ ]: At  $t_2$ , voltage  $v_{Cs}$  equals to the sum of  $v_{Cc}$  and  $V_{DD}$ . Thus, the body diode of the clamped switch  $S_a$  begins to conduct, then,  $C_c$  and  $C_s$  are charged together. Due to the large capacitance of  $C_c$ , most of the current goes through  $C_c$  and its voltage  $v_{Cc}$  barely changes, thus,  $v_{Cs}$  is clamped. As the body diode of  $S_a$  conducts,  $S_a$  can achieve ZVS during the mode.

**Mode 4** [ $t_3, t_4$ ]: Switch  $S$  is still OFF and  $S_a$  is ON.  $C_c$  and  $C_s$  are charged or discharged together. Similar to the mode 3, the main resonant circuit is still charged.

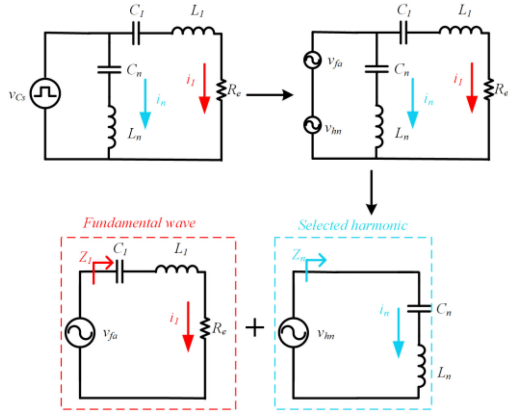


Fig. 4. Equivalent circuit of the proposed topology for harmonic analysis.

*Mode 5* [ $t_4$ ,  $t_5$ ]: At  $t_4$ , the clamping switch  $S_a$  is turned OFF,  $C_C$  stops discharging and the harmonic current  $i_n$  continues to discharge  $C_S$ . However, due to the voltage clamping feature of  $C_S$  and  $C_C$ , the drain-source voltage  $v_{S_a}$  of  $S_a$  rises from zero slowly and ZVS can be achieved on  $S_a$ .

*Mode 6* [ $t_5$ ,  $t_6$ ]: At  $t_5$ ,  $C_S$  finishes discharging.  $i_1$ ,  $i_n$  and  $i_C$  flow through the body diode of  $S$ . As  $v_{C_S}$  is clamped to zero, ZVS can be achieved if  $S$  is turned ON during the mode.

### C. Harmonic Analysis

Before analyzing, the proposed topology is simplified.

- 1) The series type receiver of the WPT system is considered as an equivalent resistance  $R_e$  on the primary side. It can be calculated by the following equation:

$$\begin{cases} R_e = \frac{\omega^2 M^2}{R_{s11} + R_L} \\ M = k\sqrt{L_1 L_{11}} \end{cases} \quad (2)$$

where  $\omega$  is the operation angle frequency of the system,  $k$  is the coupling coefficient,  $M$  is the mutual inductance, and  $R_{s11}$  is the parasitic resistance of  $L_{11}$  and  $C_{11}$ .

- 1) In the primary side, only the resonant circuit is kept and the other part is replaced by the voltage source  $v_{C_S}$ .
- 2) As [ $t_1$ ,  $t_2$ ] and [ $t_4$ ,  $t_5$ ] shown in Fig. 2 are negligible,  $v_{C_S}$  is assumed as square voltage.

Fig. 4 shows the corresponding equivalent circuit of Fig. 1. According to FFT, the quasi-square waveform  $v_{C_S}$  contains different frequency sine components and the series resonant circuit provides the almost zero impedance for specific frequency. Hence, only  $v_{fa}$  (the fundamental element of  $v_{C_S}$ ) and  $v_{hn}$  (the  $n$ th harmonic of  $v_{C_S}$ ) are considerable in the proposed topology.  $Z_1$  denotes the impedance of the main resonant circuit under the fundamental voltage  $v_{fa}$  and  $Z_n$  denotes the reactance of the harmonic circuit under the  $n$ th harmonic voltage  $v_{hn}$ .

$$\begin{cases} v_{hn} = V_{hn} \sin(\omega n t + \phi_n) \quad n = 1, 2, 3, \dots \\ v_{fa} = v_{hn} \quad n = 1 \end{cases} \quad (3)$$

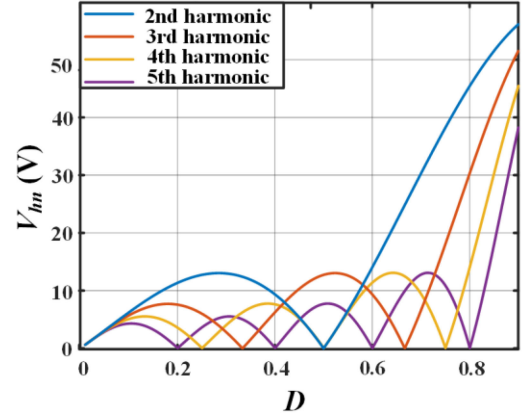


Fig. 5. Variation in  $V_{hn}$  with respect to  $D$ .

$$\begin{cases} V_{hn} = \sqrt{A_n^2 + B_n^2} \\ A_n = -\frac{V_{C_S} \cdot \sin(2\pi n D)}{n\pi} \\ B_n = -\frac{V_{C_S} \cdot \cos(2\pi n D)}{n\pi} \end{cases} \quad (4)$$

$$\phi_n = \arctan\left(\frac{A_n}{B_n}\right) \quad (5)$$

where  $D$  is the conduction duty cycle of  $S$ ,  $V_{hn}$  is the amplitude of the  $n$ th harmonic voltage  $v_{hn}$  and  $\phi_n$  is the initial phase.  $V_{C_S}$  is the amplitude of the square voltage  $v_{C_S}$ . It can be calculated based on the relationship between  $V_{C_S}$  and  $V_{DD}$ , and voltage-second balance theory on  $L_C$ , which are shown in (6) and (7). The result is shown in the following:

$$V_{C_S} = V_{C_C} + V_{DD} \quad (6)$$

$$\int_0^{DT} V_{DD} dt = \int_0^{(1-D)T} V_{C_C} dt \quad (7)$$

$$V_{C_S} = \frac{V_{DD}}{1-D} \quad (8)$$

Fig. 5 shows the relationship between  $D$  and  $V_{hn}$ . Obviously, the  $n$ th harmonic has  $(n-1)$  zero points when  $D$  ranges from 0 to 1. At the zero points, no harmonic current could be provided to release the charge in  $C_S$ . Therefore, to realize the ZVS condition, appropriate harmonic should be selected according to the duty cycle.

Theoretically, any harmonic could be employed for ZVS. However, there is less time for high-order harmonic to release the charge in  $C_S$ , namely, a larger harmonic current is required to achieve ZVS, leading to a higher loss on the parasitic resistance. Thus, the low-order harmonic is preferred.

In Fig. 5, the envelop line of the second and third harmonic can cover almost all the range of  $D$ , therefore, these two harmonics are the best candidate components for ZVS realization due to their low-order.

### III. PARAMETERS DESIGN AND EFFICIENCY ANALYSIS

The following assumptions are given before analysis.

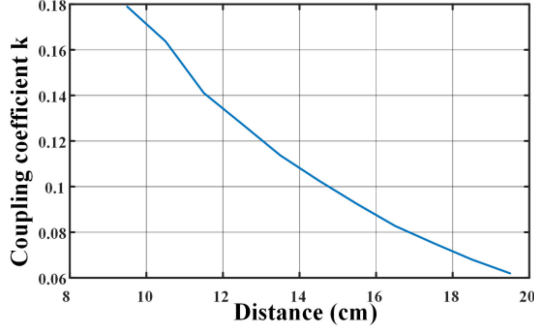


Fig. 6. Relationship between  $k$  and the coils distance in the proposed prototype.

- 1) The choke inductance  $L_C$  is large enough so that its current  $i_C$  is assumed to be the constant current  $I_C$ .
- 2) The clamped capacitor  $C_C$  is large enough and the clamped voltage  $v_{C_c}$  is considered to be constant value of  $V_{C_c}$ .
- 3) The resonant current  $i_1$  and  $i_n$  are sinusoidal.
- 4) The parameters of  $S$  and  $S_a$  are assumed to be the same.
- 5)  $C_S$  is so small that  $[t_1, t_2]$  and  $[t_4, t_5]$  are neglected. In the other words, it is assumed that  $[t_1, t_5]$  approximately equals to  $[t_2, t_4]$ . Then, assume the operation period  $T$ , the conduction duty cycle  $D$  of the main switch  $S$  could be defined as follows:

$$D \approx \frac{T - (t_4 - t_2)}{T} \quad (9)$$

- 6) As shown in Figs. 4 and 5, there are numerous of harmonics  $v_{hi}$  in  $v_{C_s}$ , and only the fundamental wave  $v_{fa}$  and the selected harmonic  $v_{hn}$  are considered in the article, because the resonant circuits exhibit large reactance under other harmonics.

Furthermore, following notes should also be noticed.

- 1)  $k$  demonstrates the coil distance. Fig. 6 shows the  $k$ -distance curve of the coils used in the proposed prototype. Where  $k$  between two coils is measured by the WK-6500B impedance analyzer. Seen from the curve,  $k$  is negatively correlated to the coils distance.
- 2) In the following content,  $R_e$  is contained in the equations, instead of  $k$  and  $R_L$ . Obviously in (2), the influence of coupling coefficient  $k$  and the load  $R_L$  to the system performance equals to the change of equivalent resistance  $R_e$  on the primary side. Therefore, the essence of realizing ZVS over a wide range of coils distance and load is to maintain ZVS under a variable  $R_e$ .

#### A. Parameters Design of Harmonic Circuit

$I_1$  and  $I_C$  can influence the released charge. In the section, they are assumed as known quantities and will be calculated in later section.

The harmonic current  $i_n$  is required to discharge the shunt capacitor  $C_s$ . As a large  $i_n$  will results in a high loss, while a small  $i_n$  may lose the ZVS condition, an appropriate  $i_n$  is needed to keep ZVS operation while introducing a relatively small loss. In

this section, an optimal design strategy for the harmonic circuit to realize critical ZVS under the fixed  $k$  and  $R_L$  is proposed.

To determine the value of  $i_n$ , it is necessary to calculate how much charge should be discharged from shunt capacitor  $C_s$ . The charge is defined as  $Q_t$ . From Figs. 1 and 2, obviously,  $Q_t$  is consisted of three parts as follows:

$$Q_t = Q_{C_s} + Q_{I_C} + Q_{i_1} \quad (10)$$

where  $Q_{C_s}$  is the charge stored in  $C_s$ , and it can be calculated out as follows:

$$Q_{C_s} = V_{C_s} C_s = \frac{V_{DD}}{1-D} C_s \quad (11)$$

$Q_{I_C}$  is the charge injected by the choke current  $I_C$ , and it can be calculated out as follows:

$$Q_{I_C} = I_C \cdot t_r \quad (12)$$

where  $t_r$  is the required time to completely release  $Q_t$ , and it should be set based on the switching speed of the applied switch  $S$ .  $I_C$  will be solved when analyzing the efficiency.

$Q_{i_1}$  is the charge injected by the main resonant current  $i_1$ , and it can be calculated as follows:

$$Q_{i_1} = \int_0^{t_r} I_1 \sin(\omega t + \theta_1) dt = \frac{I_1 (\cos(\theta_1) - \cos(\omega t_r + \theta_1))}{\omega} \quad (13)$$

where  $\theta_1$  is the phase of the fundamental voltage  $v_{fa}$ . As the main resonant circuit works in resonant state and there is no phase difference between  $v_{fa}$  and  $i_1$ ,  $\theta_1$  also represents the phase of  $i_1$ . As to the phase of  $v_{hn}$ , it is defined as  $\theta_n$ .  $\theta_1$  and  $\theta_n$  can be calculated by following equations:

$$\begin{cases} \theta_1 = \varphi_1 + 2\pi(1-D) \\ \theta_n = \varphi_n + 2\pi n(1-D) \end{cases} \quad (14)$$

After  $Q_t$  is obtained, the value of  $i_n$  to meet ZVS condition can be calculated by following equations:

$$\int_0^{t_r} I_n \sin(\omega n t + \alpha_n) dt \geq Q_t \quad (15)$$

$$I_n \geq \frac{Q_t \cdot \omega n}{\cos(\alpha_n) - \cos(\omega n t_r + \alpha_n)} \quad (16)$$

where  $\alpha_n$  is the phase of  $i_n$ . Different from the main resonant circuit, there is a phase difference between  $v_{hn}$  and  $i_n$ . As the parasitic resistance of the harmonic circuit has much small weight in the harmonic impedance  $Z_n$ , it is negligible when considering the phase of  $i_n$ . Therefore, the relationship between  $\alpha_n$  and  $\theta_n$  is as follows:

$$\begin{cases} \alpha_n = \theta_n + \frac{\pi}{2} Z_n < 0 \\ \alpha_n = \theta_n - \frac{\pi}{2} Z_n > 0 \end{cases} \quad (17)$$

In (17), if  $Z_n$  is capacitive, the phase difference between  $i_n$  and  $v_{hn}$  is  $90^\circ$ . Reversely, if  $Z_n$  is inductive, it should be  $-90^\circ$ . To illustrate the relationship among different phases more clearly, an example of second harmonic is illustrated in Fig. 7. Obviously, when  $S_a$  is turned OFF,  $\alpha_n$  can influence the direction of  $i_{hn}$ , and only when the harmonic current  $i_{hn}$  is in positive direction, it can discharge  $C_s$ . Namely, when  $S_a$  is turned OFF,

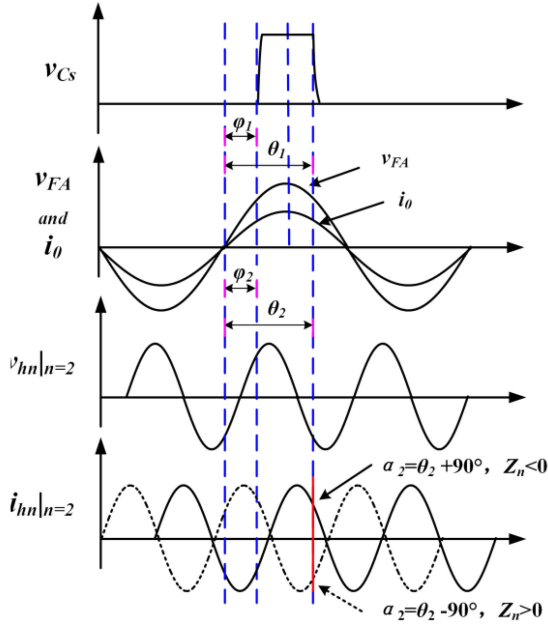


Fig. 7. Phase relationship between different waveforms.

the phase of  $i_n$  should in the range of  $[0, \pi]$ . Therefore, to achieve ZVS,  $\alpha_n$  should satisfy the following:

$$\alpha_n \in [2\pi m, \pi + 2\pi m], m = 1, 2, \dots \quad (18)$$

Based on the above analysis, the key point to design strategy is to set  $Z_n$  appropriately, and to satisfy (16) and (18) for ZVS condition.  $|Z_n|$  can be calculated by (18), and its sign can be designed according to (17) and (18)

$$|Z_n| = \frac{V_{hn}}{I_n} \quad (19)$$

Then, the relationship between  $L_n$  and  $C_n$  can be calculated by (20). After one of the two parameters is selected, the other one can be obtained as well

$$L_n = \frac{Z_n}{\omega n} + \frac{1}{C_n \cdot (\omega n)^2} \quad (20)$$

The design strategy introduced above is under the fixed  $k$  and  $R_L$  (namely, the fixed  $R_e$ ). In practical,  $k$  and  $R_L$  in the WPT system varies frequently and  $R_e$  can hardly be fixed. To illustrate the ZVS characteristics more clearly, Fig. 8 is given, where  $k$  is considered as the variable and  $R_L$  is fixed.

Three curves are shown in Fig. 8. The orange curve shows the amplitude of practical harmonic current  $I_n$ , it will be independent to  $k$  after the harmonic circuit is designed. The red curve denotes  $R_e$  calculated by (2). Notice, for the WPT system of SS type, there is positive relationship between  $k$  and  $R_e$ . Namely, a larger  $k$  means a larger  $R_e$ , and finally results in a smaller  $Q_t$  in shunt capacitor. Correspondingly, as the blue curve shows, a smaller harmonic current is required for ZVS. Therefore, ZVS could always be maintained at  $R_e \geq R_{opt}$ .

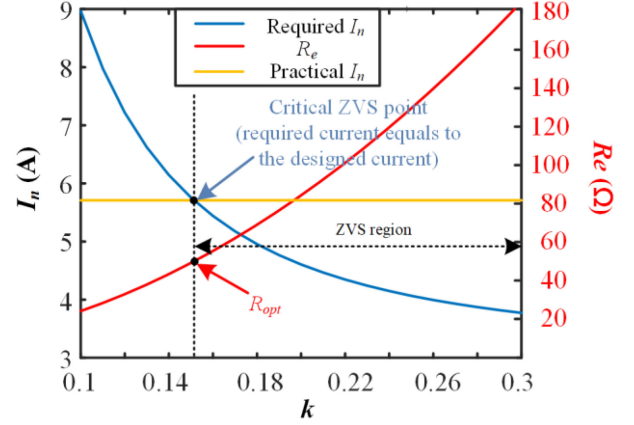


Fig. 8. Relationship among  $k$ ,  $R_e$  and ZVS region ( $f = 200$  kHz,  $L_1 = L_{11} = 110$   $\mu$ H,  $C_1 = C_{11} = 5.918$  nF,  $R_L = 10$   $\Omega$ ).

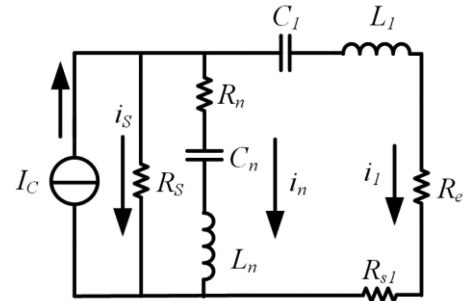


Fig. 9. Equivalent circuit of the proposed topology for efficiency analysis.

In Fig. 8, only  $k$  is considered as a variable to change  $R_e$ . Actually, if  $R_L$ , or both  $R_L$  and  $k$  are designed as variables, similar conclusion could also be obtained: when  $R_e \geq R_{opt}$ , ZVS could always be maintained.

### B. Efficiency Analysis

While calculating the efficiency of the primary side, the parasitic resistance of  $L_1$  and  $C_1$  (named  $R_{s1}$ ), the conduction resistances of  $S_a$  and  $S$  (named  $R_S$ ), and the parasitic resistance of  $L_n$  and  $C_n$  (named  $R_n$ ) are considered. Recalling in Fig. 2, there is only one switch turned ON at each moment, therefore, the equivalent circuit shown in Fig. 9 yields. The total power loss  $P_t$  can be expressed as follows:

$$P_t = P_S + P_{Rn} + P_{R_{s1}} \quad (21)$$

where  $P_S$ ,  $P_{Rn}$ , and  $P_{R_{s1}}$  denote the power loss on  $R_S$ ,  $R_n$ , and  $R_{s1}$ , respectively.

The power loss  $P_{R_{s1}}$  can be calculated by the following:

$$P_{R_{s1}} = \frac{I_1^2}{2} R_{s1} \quad (22)$$

where  $I_1$  is the amplitude of  $i_1$  and can be calculated by the following [30]:

$$I_1 = \frac{V_{fa}}{R_e + R_{s1}} = \frac{V_{DD} \sqrt{2(1 - \cos(2\pi D))}}{\pi(1-D)(R_e + R_{s1})} \quad (23)$$

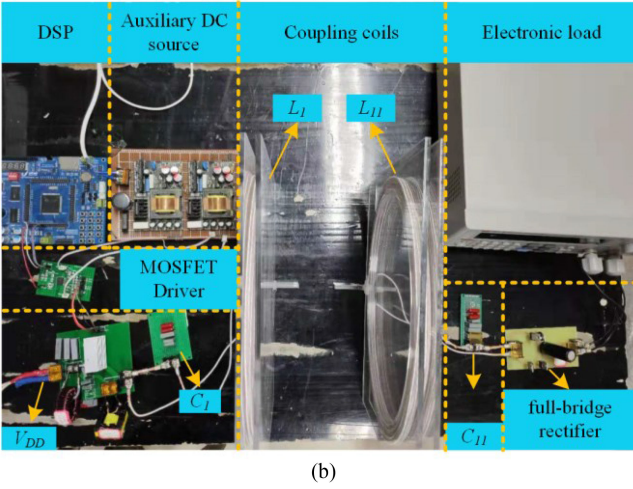
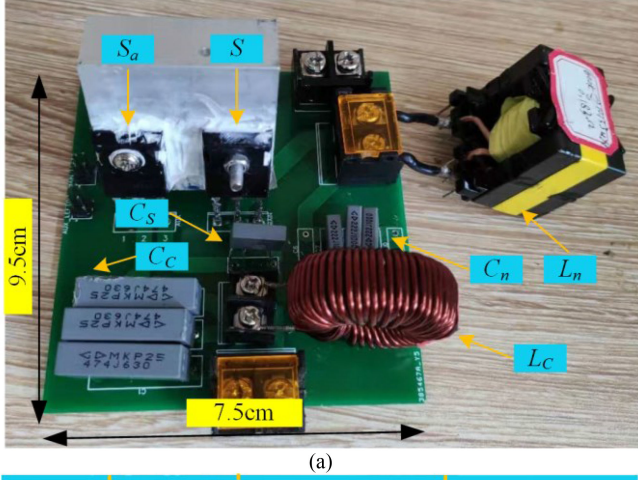


Fig. 10. Prototype of the proposed WPT system. (a) Proposed topology. (b) Entire WPT system.

The power loss  $P_{Rn}$  can be calculated by the following:

$$P_{Rn} = \frac{1}{T} \int_0^T i_n^2 R_n dt = \frac{(Q_t \omega n)^2}{2(\cos(\omega n t_r + \alpha_n) - \cos(\alpha_n))^2} R_n \quad (24)$$

The power loss  $P_S$  on  $R_S$  can be calculated by the following:

$$P_S = \int_0^T (i_n + i_1 + I_C)^2 R_S dt = \left( \frac{(I_n + I_1)^2}{2} + I_C^2 \right) R_S \quad (25)$$

In (25),  $I_C$  and  $I_n$  are unknown variables, and to solve their values, according to the energy conservation balance, it yields the following:

$$V_{DD} I_C = P_t + \frac{I_t^2}{2} R_e \quad (26)$$

After  $V_{DD}$ ,  $D$ , and  $t_r$  are fixed,  $I_C$  and  $I_n$  can be calculated by (15) and (26) in MATLAB. Then, the efficiency  $\eta_p$  of the primary side can be calculated by (27) and the efficiency  $\eta_w$  of the WPT system can be calculated by (28)

$$\eta_p = 1 - \frac{P_t}{V_{DD} I_C} \quad (27)$$

TABLE I  
SPECIFICATIONS OF THE PROTOTYPE

Parameters	Value	Parameters	Value
$f$	200 kHz	$R_S$	40m $\Omega$
$L_C$	0.5 mH	$R_n$	0.33 $\Omega$
$L_l, L_{l1}$	110 $\mu$ H	$R_{s1}, R_{s11}$	0.67 $\Omega$
$C_l, C_{l1}$	5.75 nF	$R$	37 $\Omega$
$C_S$	3.3 nF	$I_O$	1.18 A
$C_C$	1.41 $\mu$ F	$V_F$	2.1 V
$k$	0.068~0.178	Total output power	55 W
$C_o$	150 $\mu$ F	$V_{DD}$	22~35V
$D_1, D_2, D_3, D_4$	RHRP3060	$R_L$	33.6 $\Omega$
$S, S_a$	IRFP260NPbF		

TABLE II  
THREE CASES OF SELECTED  $C_n$  AND  $L_n$  FOR ZVS VERIFICATION

$t_r$ (ns)	$D$	$L_n$ ( $\mu$ H)	critical $k$	Harmonic order $n$	$C_n$ (nF)	
					ideal	real
I	250	0.5	0.103	3	7.47	7.6
II	250	0.5	0.178	3	8.18	8.2
III	250	0.65	0.178	2	17.1 7	17.05

$$\eta_w = \eta_p \frac{R_L}{R_L + R_{s11}} \quad (28)$$

#### IV. EXPERIMENTAL RESULTS

As analyzed above, both  $k$  and  $R_L$  could influence ZVS through changing  $R_e$ . Due to the similar principle, in the experiments, only  $k$  (mirror the coils distance change) is employed as variable for verification.

A platform shown in Fig. 10, with the output power of 50 W, was implemented in the laboratory. The employed dc source and electronic load are FTP065-800-16 and RK8512, respectively. The switching frequency of  $S$  and  $S_a$  and the resonant frequency of the receiver were set to be 200 KHz. Specifications of the platform are listed in Table I. The CBB capacitors were utilized for resonant and harmonic circuits.

The real values of the components were measured based on the WK-6500B impedance analyzer. In addition, as shown in Table I, the input voltage  $V_{DD}$  is unfixed. This is because, in the comparative experiment, the coils distance can influence the output power. To ensure the output power to have a constant value of 55 W,  $V_{DD}$  is considered to be adjusted.

Based on the platform, three groups of harmonic circuits with different  $C_n$  and  $L_n$ , were first designed to verify the harmonic analysis and parameter design strategy. Corresponding parameters are listed in Table II. Then, one group of parameters was selected to make comparison with typical class-E converter on voltage stress, ZVS region and efficiency.

Ideally, under the three groups of the parameter, following phenomena will be observed in the experimental results.

- 1) Based on the cases I and II, the third harmonic was selected and the frequency of the current  $i_n$  should be  $3f$  (600 kHz). At the falling edge of  $v_{C_S}$ ,  $i_n$  should be positive, and its phase should be close to  $90^\circ$ . Furthermore, under the case I, the charge in  $C_S$  should be completely extracted after 250 ns when critical  $k = 0.103$ , and ZVS could

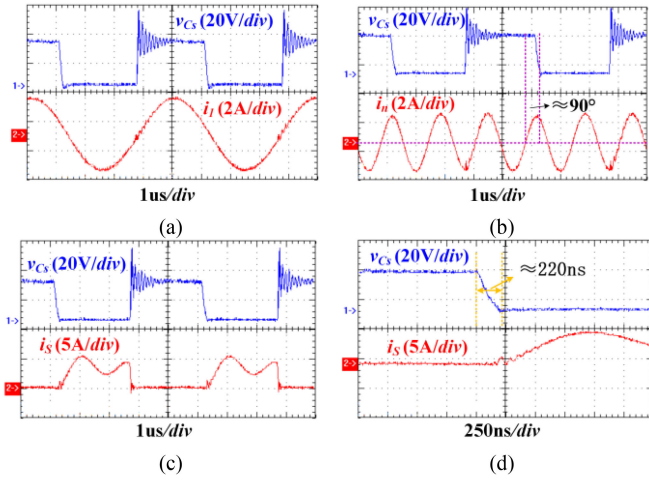


Fig. 11. Voltage/current curves at case I ( $L_n = 10.17 \mu\text{H}$ ,  $C_n = 7.6 \text{ nF}$ ,  $D = 0.5$  and critical  $k = 0.103$ ). (a)  $v_{Cs}$  and  $i_1$ . (b)  $v_{Cs}$  and  $i_n$ . (c)  $v_{Cs}$  and  $i_S$ . (d) Zoomed-in  $v_{Cs}$  and  $i_S$ .

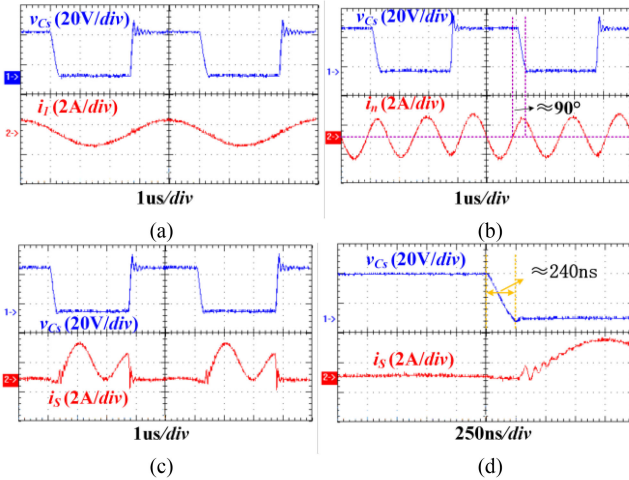


Fig. 12. Voltage/current curves at case II ( $L_n = 10.17 \mu\text{H}$ ,  $C_n = 8.2 \text{ nF}$ ,  $D = 0.5$  and critical  $k = 0.178$ ). (a)  $v_{Cs}$  and  $i_1$ . (b)  $v_{Cs}$  and  $i_n$  of. (c)  $v_{Cs}$  and  $i_S$ . (d) zoomed-in  $v_{Cs}$  and  $i_S$ .

always be realized when  $k \in [0.103, 1]$ . Similarly, under the case II,  $C_S$  should be completely discharged after 250 ns when critical  $k = 0.178$ , and ZVS could always be realized when  $k \in [0.178, 1]$ .

- Based on case III, the second harmonic was selected, the frequency of the current  $i_n$  should be  $2f$  (400 kHz) and at the falling edge of  $v_{Cs}$ , the phase of  $i_n$  needs to be  $127^\circ$ . Furthermore, the charge in  $C_S$  should be completely extracted after 250 ns when critical  $k = 0.178$ , and ZVS could always be realized when  $k \in [0.178, 1]$ .

Corresponding experimental results are shown in Figs. 11, 12, and 13, respectively. From Figs. 11(a), 12(a) and 13(a), obviously, the phase of  $i_1$  is  $90^\circ$  at the center line of  $v_{Cs}$ . As the phase of  $v_{fa}$  is  $90^\circ$  at the center line of  $v_{Cs}$  as well, it suggests almost no phase difference between  $i_1$  and  $v_{fa}$ . That is to say, different from the traditional class-E system, there is

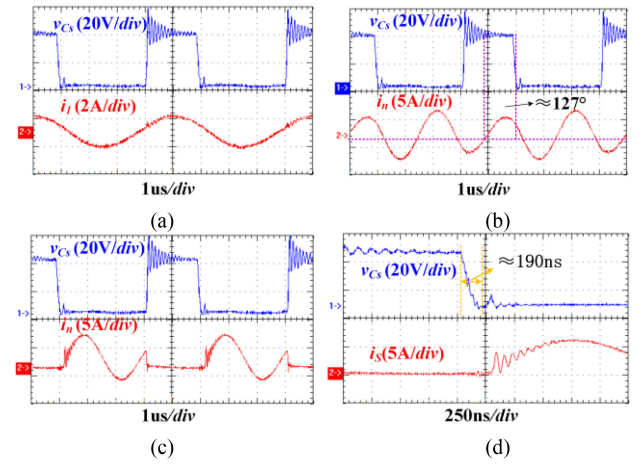


Fig. 13. Voltage/current curves at case III:  $L_n = 10.17 \mu\text{H}$ ,  $C_n = 17.05 \text{ nF}$ ,  $D = 0.65$  and critical  $k = 0.178$ . (a)  $v_{Cs}$  and  $i_1$ . (b)  $v_{Cs}$  and  $i_n$ — $n=2$  of. (c)  $v_{Cs}$  and  $i_S$ . (d) Zoomed-in  $v_{Cs}$  and  $i_S$ .

zero reactive power during the power injection process for the proposed topology.

In Figs. 11(b), 12(b), and 13(b), at the falling edge of  $v_{Cs}$ , the phase of  $i_n$  approaches to the analysis value. The small difference between the experimental value and theoretical value comes from that  $v_{Cs}$  is a quasi-square wave and its falling edge is much less steep than the square wave.

In Figs. 11(c) and (d), and 12(c) and (d), obviously, the duration of discharging process approaches to 250 ns, fitting well with the preset discharging time  $t_r$ . In Fig. 13(c) and (d), the discharging time is about 190 ns and smaller than  $t_r$ . In addition,  $C_S$  is recharged before  $S$  is turned ON. This may be caused by the distortion of  $i_{n|n=2}$ : the second harmonic has a lower quality factor than the third harmonic, correspondingly, the current distortion is more serious (as shown in Figs. 11(b), 12(b), and 13(b),  $i_{n|n=3}$  more approaches sine wave than  $i_{n|n=2}$ ). The distortion can be decreased by using a larger inductor  $L_n$  in the harmonic circuit.

To further verify the validity of the harmonic analysis, the curves under the duty cycle of  $D = 0.5$  and  $D = 0.65$  are given in Fig. 14. Obviously in Table II, when  $L_n = 10.17 \mu\text{H}$  and  $C_n = 17.05 \text{ nF}$ , the harmonic circuit reveals small impedance for the second harmonic, however, as  $i_{n|n=2}$  is zero in Fig. 14(a), it is verified that there is no second harmonic component in the square waveform  $v_{Cs}$  when  $D = 0.5$ . Similarly, it is also shown in Fig. 14(b) that there is negligible third harmonic component when  $D = 0.65$ . In addition, it is notable that when  $S$  is turned OFF, there are distinct oscillations of  $i_{n|n=3}$  and  $v_{Cn|n=3}$  in Fig. 14(b). This is caused by the zero-state response in the harmonic circuit. As shown in Fig. 14(c), when  $S$  is turned OFF,  $v_{Cs}$  begins to charge the harmonic circuit,  $L_n$  and  $C_n$  begins to store energy. However, at the moment when  $S$  is turned ON, both  $i_n$  and  $v_{Cn}$  return to zero and no energy is stored in the harmonic circuit.

Based on the above experimental results and discussion, the validity of harmonic analysis is verified.

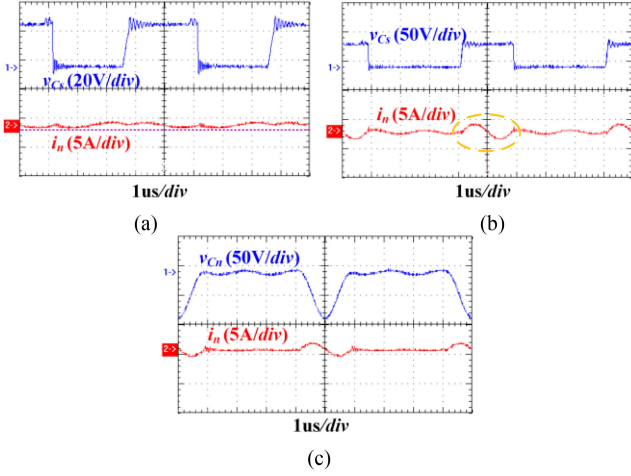


Fig. 14. Variation of the harmonic circuits voltage/current in respect to  $D$ . (a)  $v_{Cs}$  and  $i_{n|n=2}$  when  $L_n = 10.17 \mu\text{H}$ ,  $C_n = 17.05 \text{ nF}$  and  $D = 0.5$ . (b)  $v_{Cs}$  and  $i_{n|n=3}$  when  $L_n = 10.17 \mu\text{H}$ ,  $C_n = 7.6 \text{ nF}$ ,  $D = 0.65$ . (c)  $v_{Cs}$  and  $i_{n|n=3}$  when  $L_n = 10.17 \mu\text{H}$ ,  $C_n = 7.6 \text{ nF}$ ,  $D = 0.65$ .

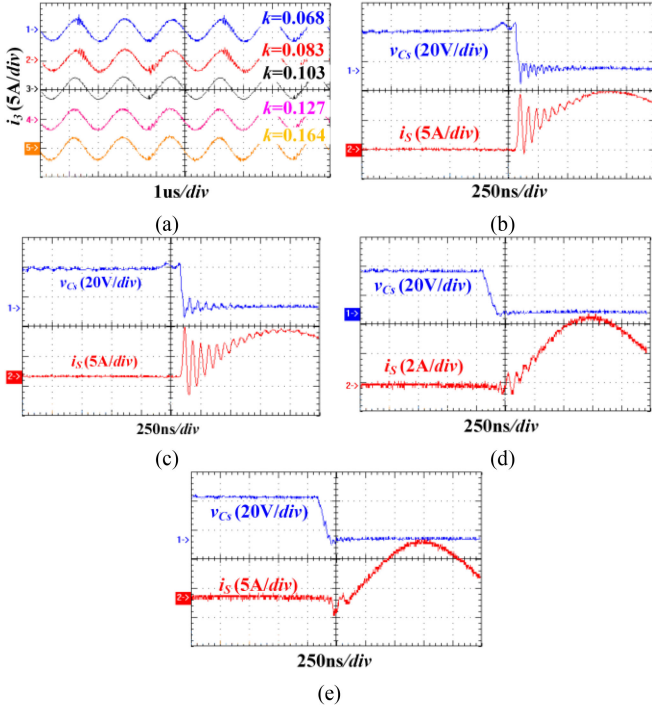


Fig. 15. Curves at case I ( $L_n = 10.17 \mu\text{H}$ ,  $C_n = 7.6 \text{ nF}$ ,  $D = 0.5$ ) in respect to  $k$ . (a)  $i_{n|n=3}$  under various  $k$ . (b) Zoomed-in  $v_{Cs}$  and  $i_{n|n=3}$  ( $k = 0.068$ ). (c) Zoomed-in  $v_{Cs}$  and  $i_{n|n=3}$  ( $k = 0.083$ ). (d) Zoomed-in  $v_{Cs}$  and  $i_{n|n=3}$  ( $k = 0.127$ ). (e) Zoomed-in  $v_{Cs}$  and  $i_{n|n=3}$  ( $k = 0.164$ ).

The following-up experimental results focus on verifying low voltage stress, ZVS characteristic and efficiency of the proposed topology. The prototype, which could exactly realize ZVS under  $k = 0.103$  and  $D = 0.5$ , were selected for experiments implementation ( $L_n = 10.17 \mu\text{H}$ ,  $C_n = 7.6 \text{ nF}$ ).

Fig. 15 shows the key waveforms of the proposed topology. Fig. 15(a) shows  $i_{n|n=3}$  under different  $k$ , and it is obvious that the amplitude and phase of  $i_{n|n=3}$  is never influenced by  $k$ . Fig. 15(b)–(e) show the zoomed-in waveforms of  $v_{Cs}$  and  $i_S$

under different  $k$ . When  $k$  is smaller than 0.103, ZVS will be lost, but if  $k$  is larger than 0.103, ZVS can be always achieved, fitting well with the preset ZVS region. Therefore, it is verified that the harmonic circuit can provide a stable current to extract charge, and ZVS could be realized over a wide range of coils distance.

Above experimental results have proved that ZVS turn-ON is realizable on  $S$ . Then, Fig. 16 gives the waveforms to further prove the ZVS feature of  $S$  and  $S_a$ . In Fig. 16(a),  $v_{Cs}$  rises slowly when  $S$  is OFF, therefore, the overlap of  $v_{Cs}$  and  $i_S$  can be effectively decreased comparing with hard switching. Fig. 16(b) and (c) are the curves of  $i_{Cc}$  and the drain–source voltage  $v_{S_a}$  of  $S_a$ . In Fig. 16(b), the current is negative after  $S$  is turned OFF, namely,  $i_{Cc}$  will flow through the body diode of  $S_a$  before  $S_a$  is turned ON. In Fig. 16(c), the overlap of  $i_{Cc}$  and  $v_{S_a}$  is negligible after  $S_a$  is OFF. To sum up, ZVS could always be realized on  $S$  and  $S_a$  due to the body diode of the switches and the voltage clamping feature of the shunt capacitor  $C_S$ .

A typical class-E converter based WPT system, which can exactly achieve ZVS when critical  $k = 0.103$ , is also designed for comparison, and the corresponding results are shown in Fig. 17. Obviously, when  $k$  becomes larger than 0.103, ZVS will be lost, leading to a lower efficiency. The efficiency curves of the proposed and typical class-E systems are shown in Fig. 18. It is notable that the power loss on the full-bridge rectifier (4.96 W) was also considered as a part of the output power, because the voltage drop  $V_F$  has also been considered when calculating  $R_L$ . As shown in Fig. 18, when  $k = 0.103$ , the efficiency of the WPT system based on typical class-E converter is 91.36%, about 2.91% higher than the proposed system due to additional loss on the harmonic circuit. However, when  $k$  increases, the efficiency of typical class-E system decreases rapidly. Instead, in the proposed topology, the efficiency could always be kept more than 87%, close to the calculation.

The power loss distribution under different  $k$  is calculated according to (21)–(28), and the pie charts are given in Fig. 19 to further analyze the changing trend of the power loss on each parasitic resistance. The conducting power losses  $P_{Rs1}$  on the primary coil and  $P_{Rn}$  on the harmonic circuit are the foremost in the WPT system.  $P_{Rs1}$  is much larger than  $P_{Rn}$  when  $k$  is small, then,  $P_{Rs1}$  will decrease and  $P_{Rn}$  will increase due to the incremental  $k$ . This is because a larger  $k$  will lead to a smaller  $i_1$ , namely, a lower conducting loss on  $R_{s1}$ . On the contrary, the harmonic current  $i_n$  will never be influenced by  $k$ , as a result, the weight of the loss caused by  $i_n$  is positively related to  $k$ . This is also the reason why the efficiency increases when  $k < 0.14$  and decreases at  $k > 0.14$ .

The comparison of voltage stress is shown in Fig. 20(a). Notice the output power is maintained at 55 W. Obviously, the voltage stress of the proposed topology increases when  $k$  becomes larger. Recall the relationship between  $R_e$  and  $k$ , a higher input voltage is required to maintain the output power with  $R_e$  increasing, meaning a higher voltage stress. On the contrary, the voltage stress of typical class-E converter will decrease with  $k$  increasing. As shown in Fig. 17, when  $k$  becomes larger, the curve of  $v_{ds}$  more approaches square waveform, namely, the fundamental waveform  $v_{FA}$  of  $v_{ds}$ , will become larger and a

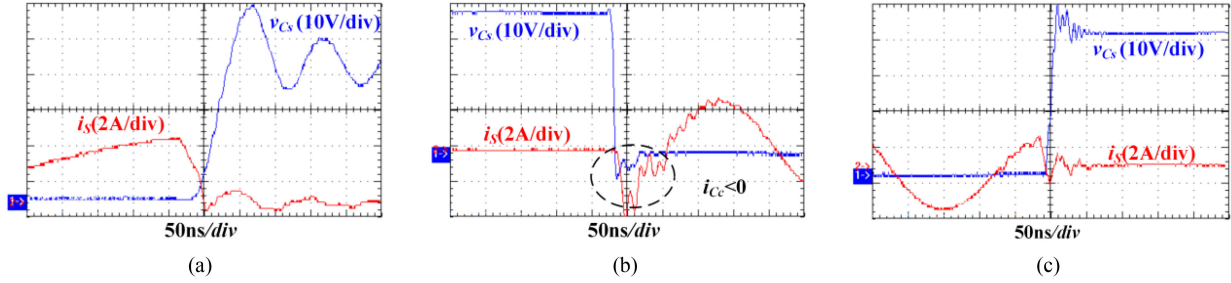


Fig. 16. Voltage and current curves of the switches at case I ( $L_n = 10.17 \mu\text{H}$ ,  $C_n = 7.6 \text{ nF}$ ,  $D = 0.5$  and critical  $k = 0.103$ ). (a)  $v_{Cs}$  and  $i_S$  when  $S$  is OFF. (b)  $v_{Sa}$  and  $i_{Cc}$  when  $S_a$  is ON. (c)  $v_{Sa}$  and  $i_{Cc}$  when  $S_a$  is OFF.

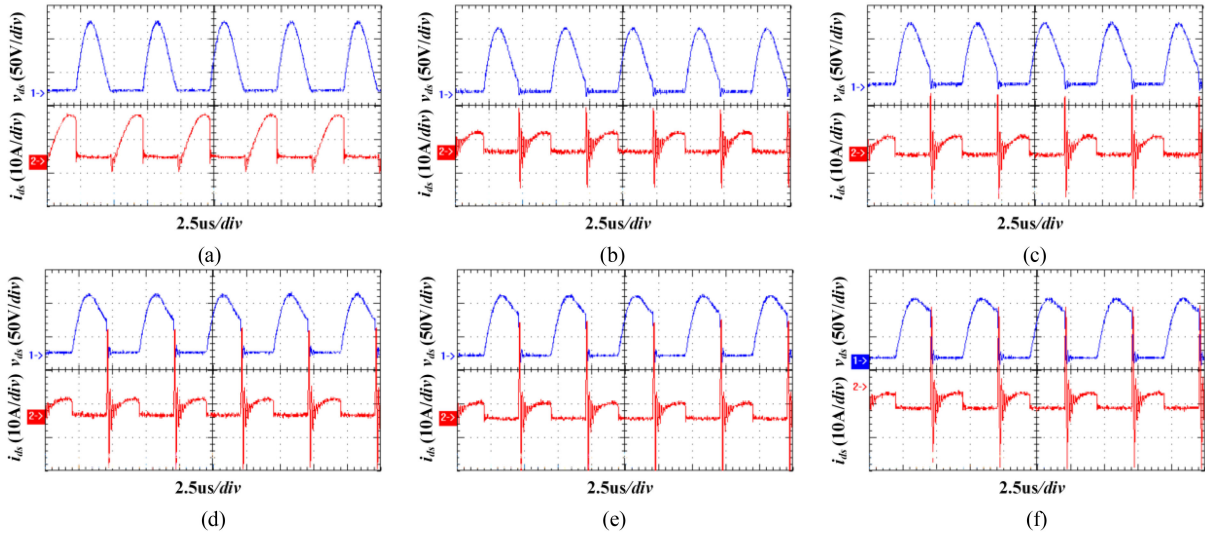


Fig. 17. Voltage and current curves of the switch in typical class-E WPT system ( $C_S = 15.47 \text{ nF}$ , critical  $k = 0.103$ ). (a)  $k = 0.103$ . (b)  $k = 0.112$ . (c)  $k = 0.127$ . (d)  $k = 0.141$ . (e)  $k = 0.162$ . (f)  $k = 0.178$ .

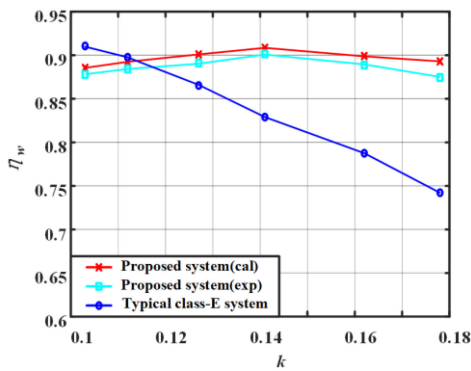


Fig. 18. Efficiency curves of the proposed and typical systems ( $D = 0.5$ ).

smaller input voltage can guarantee output power, resulting in a lower voltage stress. However, ZVS could never be realized in these cases.

Furthermore, observed from Fig. 20(a), when the converters are operated under optimum condition ( $k = 0.103$ ), the voltage stress of switch in the proposed topology will reduce down to be 41.7% of that in the typical class-E converter if they have

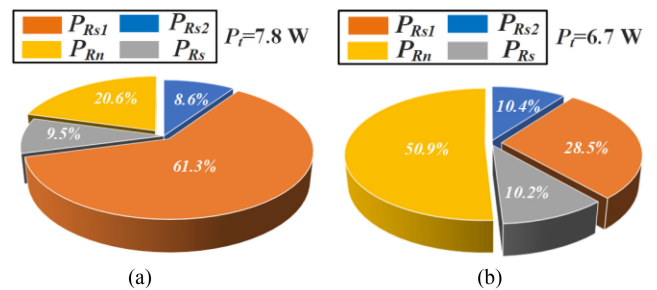


Fig. 19. Power loss distribution. (a)  $k = 0.103$ . (b)  $k = 0.178$ .

the same output power (with different  $V_{DD}$ ). Theoretically, the voltage stress of switch in the proposed topology will be 55.6% of that in the typical class-E converter under the same input voltage. Therefore, after the phase difference between  $v_{Cs}$  and  $i_1$  is eliminated, a lower input voltage could satisfy the same output power in the proposed system, meaning a lower voltage stress. Furthermore, the curves of  $V_{DD}$  and  $V_{out}$  are also given in Fig. 20(b) and (c). Comparing with Fig. 20(a) and (b), the voltage stress always doubles  $V_{DD}$  at  $D$  of 0.5, fitting will with (8). The validity of the theoretical analysis is further verified.

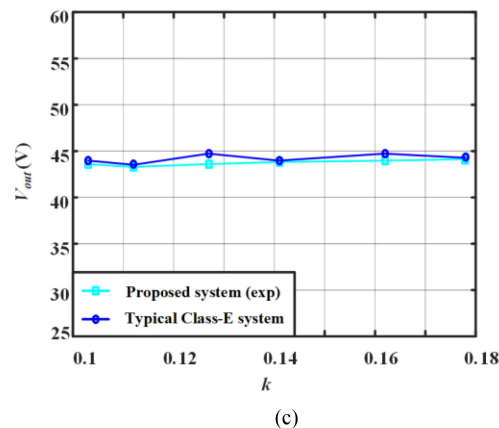
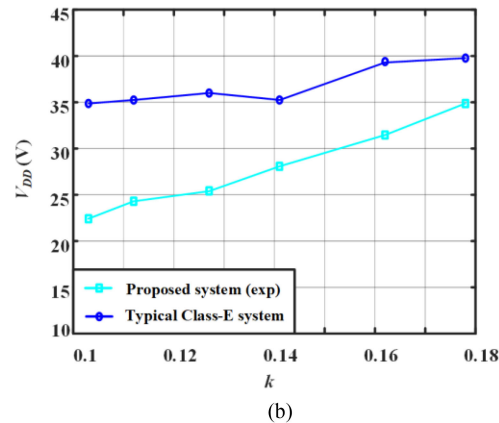
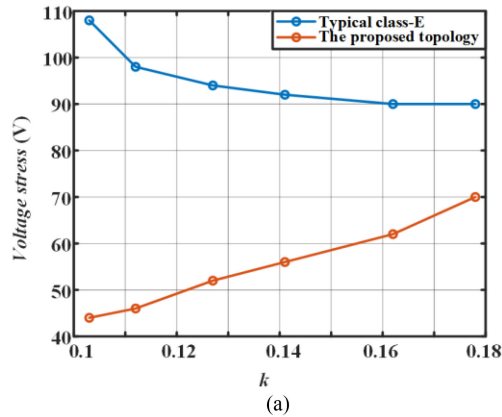


Fig. 20. Variation in voltage stress,  $V_{DD}$  and  $V_{out}$  with respect to  $k$ , under the same output power. (a) Voltage stress. (b)  $V_{DD}$ . (c)  $V_{out}$ .

In addition, it is also notable that the harmonic circuit brings additional conducting loss. Therefore, the relationship between switching loss and conducting loss is given in Fig. 21. Obviously, by designing the parameters properly, the harmonic circuit is helpful in improving the efficiency.

The ringing on the voltage curves in Figs. 11–15 is caused by the resonance between  $C_S$  and the parasitic inductance in the circuit. In the article, the parasitic inductance is introduced by the loose layout (a loose layout is much easier for voltage/current measurement). Measured by the impedance analyzer TH2839, the parasitic inductance is about 90 nH. It can be weakened by optimizing the layout of the circuit further.

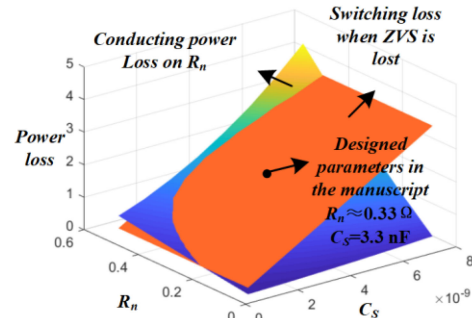


Fig. 21. Relationship among  $R_n$ ,  $C_S$ , and power loss.

## V. CONCLUSION

The article presents a clamped and harmonic injected class-E converter for WPT systems. The clamped circuit is employed to steadily decrease the voltage stress and the harmonic injection circuit is utilized to achieve ZVS over a wide range of coils distance. The prototype with three different critical conditions under given duty cycle was built. It has shown that the prototype can exactly satisfy ZVS at the preset critical coil distance, hence, ZVS could be realized when the coils distance is smaller than the critical coils distance. Furthermore, it could also be observed that when  $D = 0.5$  and  $D = 0.65$ , there has no second harmonic and third harmonic, respectively, fitting well with the harmonic analysis. Then, one case of the proposed converter was compared with typical class-E converter. WPT system based on the proposed converter could maintain ZVS when  $k$  ranging from 0.103 to 0.178, as a result, a relatively steady efficiency ranging from 85% to 88% could be maintained. As to the typical class-E converter based WPT system, ZVS could only be realized when  $k = 0.103$ , correspondingly, the efficiency rapidly decreases from 88% to 72% due to the lost ZVS. Furthermore, when both the converters could realize ZVS, about 58.3% of the voltage stress could be decreased in the proposed converter.

In general, Class-E converter will be operated at a fixed duty cycle. Under given duty cycle, the article provides an effective method to steadily decrease the voltage stress while maintaining ZVS over a wide range of coils distance for class-E converter in WPT system. In the future, the authors will focus on realizing ZVS realization over a wide range of coils distance even at various duty cycles, and optimizing the system parameters for higher efficiency.

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