

# Optimal Design and Experimental Assessment of a Wireless Power Transfer System for Home-Cage Monitoring

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**Abstract**—Techniques of long-term *in vivo* electrophysiological recording play important roles in brain research and neural rehabilitation. To avoid interruption of experiment and risk of infection, use of wireless power transfer (WPT) technique has been suggested to eliminate cumbersome wires and batteries attached to the animals in rodent electrophysiological applications. This paper presents a holistic assessment of the relationships among the physical sizes of the transmitting and receiving coils, power transfer characteristics, and specific absorption rate (SAR) in animals of a simple WPT system using two rectangular coaxial transmitting coils. With given space for the animal and size of the receiving coil, a procedure for designing the minimum driving current, and the transmitting coil dimensions and separation to deliver sufficient power to the receiver, and interactions between the transmitting and receiving coils is derived. A  $\pi$ -capacitor network that can match the impedances of the receiving coil and the load to operate the receiver at the maximum power transfer condition is proposed. It is also optimized for the overall volume. A 100-mW prototype with an operating zone of  $400 \times 240 \times 40 \text{ mm}^3$  and a receiving coil with a diameter of 11.45 mm is built and studied. The SAR in the animal is evaluated and compared with the recommended restriction level.

**Index Terms**—Electrophysiological experiments, impedance matching circuit, magnetic flux density, specific absorption rate (SAR), wireless power transfer (WPT).

## I. INTRODUCTION

TECHNIQUES of long-term *in vivo* electrophysiological recording play important roles in brain research and neural rehabilitation, such as deep brain stimulation and treatment

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Efforts on simplifying the system have been made. In [10] and [19], the position tracking system is eliminated by connecting all resonator coils in parallel. The transmitting coil delivers power to the receiver through the resonator coils, close to the receiving coil physically. However, the power losses will increase with the number of coils in the array as all the coils in parallel connection are concurrently energized. The SAR has not been fully evaluated.

The design of transmitting coil has also attracted a lot of attention to achieve a simple system, [16], [20]–[23]. In [16], the inductive link was implemented by using a single, large transmitting coil to produce a magnetic field in the cage. However, as reported in [8] and [24], such a large coil causes self-resonance at low frequency. A single transmitting coil mounted on a mechanical *XY* moving table has been proposed in [20]. By using a permanent magnet to keep tracking the position of the receiver, the transmitting coil is moved to a location close to the receiving coil. However, the fast-moving mechanical parts could produce unwanted acoustic noise and vibration, adversely affecting the animal behavior [25]. WPT systems with large columnar- and planar-shaped resonating coils have been presented and compared in [21]. The columnar-shaped resonating coils can generate a relatively uniform magnetic flux for the receiver. One of the main challenges is their bulk sizes, which limit the flexibility in the coil optimization. Multiple coils with different orientations have been implemented in the inductive link to minimize the sensitivity of coil misalignment by authors in [22] and [23]. Intelligent tracking systems and high-performance feedback subsystems are required and will lead to a more complicated system.

A WPT system without dedicated position tracking circuit or feedback control systems is proposed. The transmitting coil comprises two large coaxial rectangular windings to produce magnetic flux density with allowable fluctuations. The transmitting coil is divided into multiple segments with resonant capacitors to reduce the voltage over the transmitting coil to a safer level and eliminate self-resonance [24], [26]. A holistic assessment of the relationships among the physical sizes of the coils, power transfer characteristics, interactions between transmitting and receiving coils, is conducted. Moreover, a  $\pi$ -capacitor matching circuit that can match the receiving coil and the load is designed to operate the receiver at the maximum power transfer condition and minimize the transmitting coil current as well as the SAR in animal tissues. The matching circuit is also optimized for the overall volume. A 100-mW prototype is built and studied. Finally, the SAR in the animal is evaluated and compared with the recommended restriction level.

## II. OVERVIEW OF THE PROPOSED SYSTEM

Several practical considerations should be taken into account. First, the system should be simple and low cost, and does not block the line of sight to observe animal activities. Second, the receiver can receive sufficient power from the transmitter, even if the animal is moving rapidly in the cage. Third, the SAR

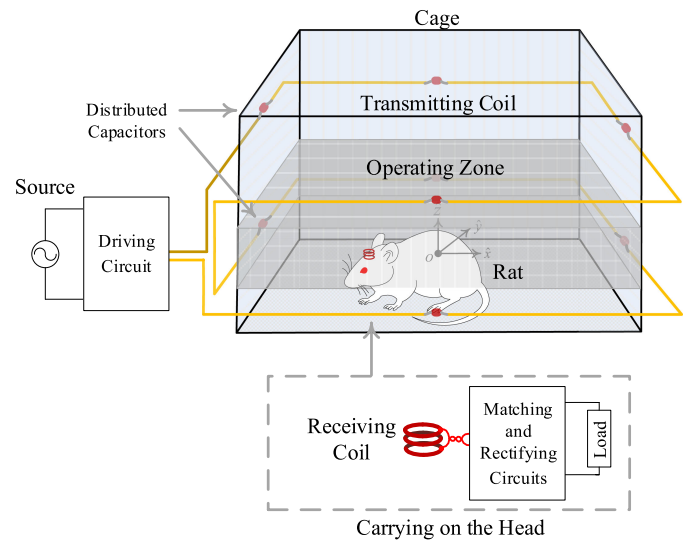


Fig. 1. Configuration of the proposed WPT system.

in animal must be lower than the limit recommended by some international safety standards [27], aiming to protect the body from adverse heating effect under exposures to electromagnetic fields. The recommended basic restriction (BR) is protective against tissue temperature increases of more than a small fraction of 1 °C. As discussed in [9], the allowable SAR level for rodents should be five times lower than the recommended limit for humans, as small animals have a less effective thermoregulatory system [28]–[30].

Fig. 1 shows the proposed transmitting coil. It is composed of two series-connected coaxial rectangular windings: one upper and one lower. The cage is placed inside the coil. Its shape is rectangular, instead of square, as the animal would feel more secure [25]. The receiver is carried by the head of the animal. The operating zone for the receiving coil is defined within the cage. It has the same footprint as the cage and the same height as the receiver carried by the animals. To avoid the coil from blocking line of sight, the thickness of each winding should be kept small.

Fig. 2 shows the equivalent circuit. The coupling between the transmitting and receiving coils is represented by a transformer model [31].  $v_{in}$  and  $i_{in}$  denote the transmitter input voltage and transmitting coil current in an rms value, respectively. The voltages induced in the transmitting and receiving coils are denoted by  $\varepsilon_1$  and  $\varepsilon_2$ , respectively. The self-inductances and winding resistances of the transmitting and receiving coils are  $L_1$ ,  $L_2$ ,  $r_1$ , and  $r_2$ , respectively.  $C_1$  represents the equivalent capacitance of the series resonant capacitors distributed over the capacitor-segmented transmitting coil. Such technique can reduce the operating coil voltage to a safer level [24], [26]. The transmitting coil is tuned to the operating frequency by adjusting  $C_1$  to maximize power transfer. A  $\pi$ -type impedance matching circuit, formed by  $C_{21}$ ,  $C_{22}$ , and  $C_{23}$ , is connected between the receiving coil and the diode-bridge rectifier to maximize the power received. Thus, the transmitting coil current and SAR are minimized. The output voltage of the impedance matching

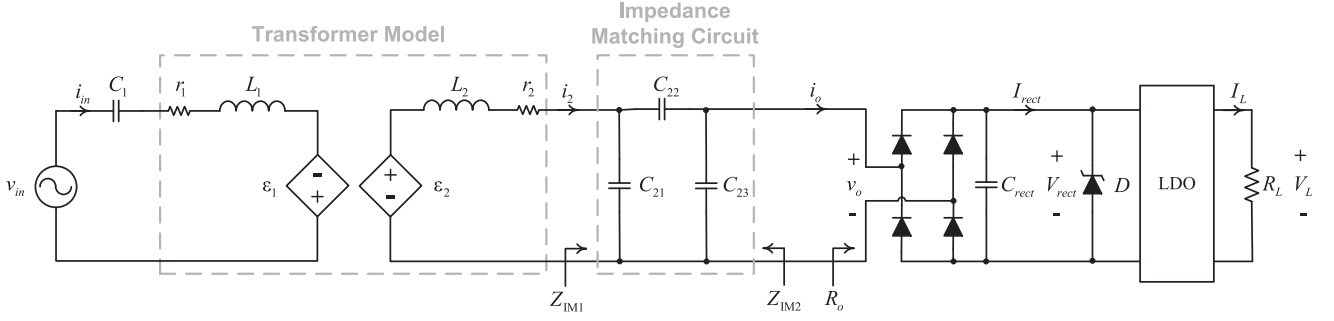


Fig. 2. Equivalent circuit of the WPT system.

circuit,  $v_o$ , is rectified by a diode bridge and stabilized by a ceramic capacitor and a supercapacitor to avoid power interruption, due to coil misalignment. The total capacitance of the two capacitors is  $C_{\text{rect}}$ . The rectified average voltage and current are denoted by  $V_{\text{rect}}$  and  $I_{\text{rect}}$ , respectively. A zener diode,  $D$ , is added to protect the supercapacitor from overvoltage. A low-dropout (LDO) regulator is used to regulate the load voltage  $V_L$ .  $I_L$  represents the load current.

When an animal walks or rests in the cage, the receiving coil placed on the animal's head is practically parallel to the transmitting coil. When it climbs and leans on the cage wall, the receiving coil is almost perpendicular to the transmitting coil and the power transfer will be affected. As discussed in [32], the duration of power interruption is usually less than 5 s. This issue can be solved by adding a supercapacitor or a low-capacity rechargeable miniature battery [33], in the receiver to maintain the load power [9], [10], [17], [18]. Alternatively, the coil structures with different oriented windings can be used to stabilize the output power when angular coil misalignment occurs [22], [23], [34], [35]. For the sake of simplicity, a supercapacitor is used. The chosen value of the supercapacitor in the prototype is designed to sustain load power for around 5 s. Thus, the current design can deal with majority of events. Nevertheless, the time duration can be lengthened by further increasing the value of the capacitor.

### III. IMPEDANCE MATCHING CIRCUIT FOR ACHIEVING MAXIMUM OUTPUT POWER

As the receiving coil is much smaller than the transmitting coil, the coupling coefficient is small. The input impedance and generated magnetic field pattern are not noticeably affected by the loading condition on the receiver side. The effects of the nonlinear characteristic of the diode-bridge rectifier on the input impedance, as reported in [31], become insignificant.

#### A. Allowable Ranges of $P_o$ and $R_o$

The equivalent output impedance of the link is modeled by  $R_o$ . The output power of the link is  $P_o$ . Assuming that the input voltage of the LDO,  $V_{\text{rect}}$ , is allowed to vary between  $V_{\text{rect,min}}$

and  $V_{\text{rect,max}}$ , the minimum and maximum values of  $P_o$  are

$$P_{o,\text{min}} = (V_{\text{rect,min}} + 2V_f) \frac{P_L}{V_L} \quad (1a)$$

$$P_{o,\text{max}} = (V_{\text{rect,max}} + 2V_f) \frac{P_L}{V_L} \quad (1b)$$

where  $V_f$  is the total forward diode voltage drop in the bridge,  $P_L$  is the maximum load power, and  $V_L$  is the load voltage.

The equivalent output resistance,  $R_o$ , which varies between  $R_{o,\text{min}}$  and  $R_{o,\text{max}}$ , is [37]

$$R_{o,\text{min}} = \frac{8V_L}{\pi^2} \left( \frac{V_{\text{rect,min}} + 2V_f}{P_L} \right) \quad (2a)$$

$$R_{o,\text{max}} = \frac{8V_L}{\pi^2} \left( \frac{V_{\text{rect,max}} + 2V_f}{P_L} \right). \quad (2b)$$

#### B. Maximum Power Transfer Condition on the Receiver

With the same output power, operating the system at the maximum power transfer condition requires lower transmitting coil current than that at the maximum efficiency condition. The generated magnetic flux density is reduced by decreasing the transmitting coil current. It is thus preferable to operate the system at the maximum power transfer condition to minimize the SAR. Although the system is not operated at the maximum efficiency, the power losses in the coils do not cause noticeable temperature rise in the coils and cage, as the power level of this kind of applications is low, typically less than 100 mW [8]–[10], [16]–[21].

Fig. 2 shows a matching circuit. Its input impedance  $Z_{\text{IM1}}$  and output impedance  $Z_{\text{IM2}}$  are

$$Z_{\text{IM1}} = \frac{X_{C21}[X_{C22}X_{C23} + R_o(X_{C22} + X_{C23})]}{X_{C23}(X_{C21} + X_{C22}) + R_o(X_{C21} + X_{C22} + X_{C23})} \quad (3)$$

$$Z_{\text{IM2}} = \frac{X_{C23}[X_{C22}Z_2 + X_{C21}(X_{C22} + Z_2)]}{Z_2(X_{C22} + X_{C23}) + X_{C21}(X_{C22} + X_{C23} + Z_2)} \quad (4)$$

where  $X_{C21} = \frac{1}{j\omega C_{21}}$ ,  $X_{C22} = \frac{1}{j\omega C_{22}}$ ,  $X_{C23} = \frac{1}{j\omega C_{23}}$ , and  $Z_2 = r_2 + j\omega L_2$ .

The circuit is designed to receive sufficient power from the transmitter under the worst-case situation, where  $R_o = R_{o,\text{min}}$ .

TABLE I  
DIFFERENT COMBINATIONS OF CAPACITORS FOR THE IMPEDANCE MATCHING CIRCUIT

$\hat{C}_{21}$	$C_{21}$ (nF)	$C_{22}$ (nF)	$C_{23}$ (nF)	$C_{2,\text{sum}}$ (nF)	Size <sup>†</sup> (mm <sup>3</sup> )
<b>1.000</b>	<b>3.49*</b>	<b>0.13</b>	<b>0.00</b>	<b>3.62</b>	<b>130.0</b>
0.997	3.47	0.16	0.21	3.84	153.0
0.800	2.79	1.10	3.25	7.14	263.8
0.600	2.09	2.02	6.06	10.17	308.0
0.400	1.39	2.95	8.85	13.19	425.5
0.200	0.70	3.88	11.65	16.23	467.1
0.000	0.00	4.81	14.43	19.24	536.0

\* Assuming that  $C_{21} = 3.49$  nF, when  $\hat{C}_{21} = 1$ .

† Total volume occupied by the capacitors  $C_{21}$ ,  $C_{22}$ , and  $C_{23}$  [38].

Then, based on (3) and (4), the matching conditions are

$$\frac{X_{C21}[X_{C22}X_{C23} + R_{o,\min}(X_{C22} + X_{C23})]}{X_{C23}(X_{C21} + X_{C22}) + R_{o,\min}(X_{C21} + X_{C22} + X_{C23})} = r_2 - j\omega L_2 \quad (5)$$

$$\frac{X_{C23}[X_{C22}Z_2 + X_{C21}(X_{C22} + Z_2)]}{Z_2(X_{C22} + X_{C23}) + X_{C21}(X_{C22} + X_{C23} + Z_2)} = R_{o,\min}. \quad (6)$$

For a given value of  $C_{21}$

$$C_{22} = \frac{1}{\omega} \frac{\omega L_2 - \omega C_{21}(r_2^2 + \omega^2 L_2^2) + \sqrt{G}}{r_2(r_2 - R_{o,\min}) + \omega^2 L_2^2} \quad (7)$$

$$C_{23} = \frac{1}{\omega} \frac{\sqrt{G}}{r_2 R_{o,\min}} \quad (8)$$

where  $G = r_2^2(\omega^2 C_{21}^2 r_2 R_{o,\min} - 1) + r_2 R_{o,\min}(\omega^2 L_2 C_{21} - 1)^2$ .

In order to ensure that  $C_{22}$  and  $C_{23} \geq 0$ , the following condition should be satisfied:

$$C_{21} \leq \frac{\omega L_2 R_{o,\min} - \sqrt{r_2 R_{o,\min}(r_2^2 - r_2 R_{o,\min} + \omega^2 L_2^2)}}{\omega R_{o,\min}(r_2^2 + \omega^2 L_2^2)}. \quad (9)$$

### C. Minimization of the Size of the Impedance Matching Circuit

The total capacitor volumes with different combinations of  $C_{21}$ ,  $C_{22}$ , and  $C_{23}$  are compared. Let  $C_{2,\text{sum}}$  be the sum of the capacitance values

$$C_{2,\text{sum}} = C_{21} + C_{22} + C_{23}. \quad (10)$$

Let  $\hat{C}_{21}$  be normalized  $C_{21}$  by the value defined on the RHS of (9). Table I shows the values of  $C_{2,\text{sum}}$  and the total volume occupied with different values of  $\hat{C}_{21}$ . The values of  $C_{22}$  and  $C_{23}$  are determined by using (7) and (8), respectively. The capacitors are of mica type [38].

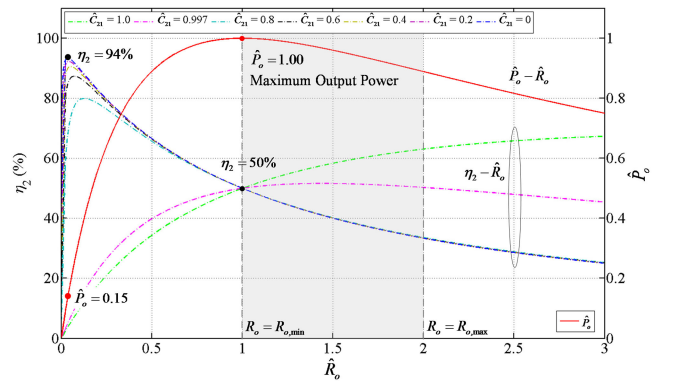


Fig. 3.  $\eta_2 - \hat{R}_o$  and  $\hat{P}_o - \hat{R}_o$  for  $\pi$ -capacitor impedance matching circuit.

### D. Maintaining the Power Efficiency of the Receiver Side Over 50%

In practice,  $R_o \in [R_{o,\min}, R_{o,\max}]$ . Let  $\hat{R}_o$  be the normalized value. Mathematically

$$\hat{R}_o = \frac{R_o}{R_{o,\min}}. \quad (11)$$

The output power of the link and the power efficiency of the receiver side,  $\eta_2$ , are

$$P_o = \frac{\hat{R}_o}{(1 + \hat{R}_o)^2} \frac{|\varepsilon_2|^2}{2r_2} \quad (12)$$

$$\eta_2 = \frac{P_o}{P_o + P_{\text{loss}2}} \quad (13)$$

where  $P_{\text{loss}2}$  is the power loss of the receiving coil, i.e.,  $P_{\text{loss}2} = |i_2|^2 r_2 / 2$ .  $i_2$  is the receiving coil current. It should be noted that  $\eta_2$  does not include the power loss of the transmitting coil.

Fig. 3 shows a family of normalized output power  $\hat{P}_o$  and efficiency  $\eta_2$  versus  $\hat{R}_o$  under different values of  $\hat{C}_{21}$  and with the same transmitting coil current. Since the circuit is operated at the matched condition, the curve  $\hat{P}_o - \hat{R}_o$  is independent of  $\hat{C}_{21}$ . However, the efficiency curve  $\eta_2 - \hat{R}_o$  varies with  $\hat{C}_{21}$ . In order to maintain the efficiency no less than 50% over the designed load range, i.e.,  $\hat{C}_{21} > 0.997$ . By combining the analysis of

Section III-C and D,  $\hat{C}_{21}$  is chosen to be equal to unity in the following discussion, and then  $C_{23}$  is equal to zero.

#### IV. DESIGN AND OPTIMIZATION OF THE INDUCTIVE LINK

##### A. Optimization of the Receiving Coil

The dimensions of the receiving coil are strictly limited by the rodent electrophysiological application and set as  $11.5 \times 6 \times 6 \text{ mm}^3$ . A single-layer helical coil is used in the receiver side. The coil self-inductance,  $L_2$ , coil resistance,  $r_2$ , and quality factor,  $Q_2$ , can be expressed as

$$L_2 = \mu_0 N_2 \left[ \ln \left( \frac{8d_r}{d_w} \right) - 1.75 \right] + \frac{\mu_0 d_r}{2} \left[ \sum_{i=1}^{N_2} \sum_{j=1}^{N_2} \left[ \left( \frac{2}{k_c} - k_c \right) K(k_c) - \frac{2}{k_c} E(k_c) \right] (1 - \psi_{ij}) \right] - \frac{\mu_0 N_2 d_r}{2} (k_s + k_m) \quad (14)$$

$$r_2 = \frac{4N_2 d_r}{d_w^2 \sigma_{Cu}} \Phi_{\text{cond}} \left( \frac{d_w}{2\delta} \right) + \frac{4\pi^2 d_r}{\sigma_{Cu}} \Phi_{\text{ind}} \left( \frac{d_w}{2\delta} \right) \sum_{p=1}^{N_2} \langle H_p^2 \rangle \quad (15)$$

$$Q_2 = \frac{\omega L_2}{r_2} \quad (16)$$

where  $\omega = 2\pi f$ ,  $\mu_0$  is the permeability of vacuum,  $N_2$  is the number of turns, and  $d_w$  is the circular wire diameters.  $L_2$  and  $r_2$  are presented in [39]–[42]. Rosa's inductance correction coefficients [40] have been applied to the coil inductance calculation in (14) to improve the accuracy. The expressions of the parameters are given in Appendix A.

Fig. 4 shows a family of  $Q_2$  and  $L_2$  versus  $N_2$  under different values of  $d_w$ . For the sake of comparison, the coils are kept at the same outer dimension by adjusting the coil diameters and winding separations. The results are calculated by (14)–(16) and simulated with COMSOL Multiphysics [43]. As  $d_w$  and  $N_2$  increase,  $Q_2$  increases and  $L_2$  decreases. However, when  $L_2$  is too small, the required  $C_{2,\text{sum}}$  and the size of the impedance matching circuit become too large and oversized. Thus, it is practically infeasible. In this design,  $N_2 = 4$  is chosen to maintain the value of  $L_2$  to be larger than 100 nH and  $d_w = 1.3 \text{ mm}$  is selected to maximize the value of  $Q_2$ .

##### B. Allowable Range and Variation of $B_z$

The rat has mostly its four limbs stepped on the cage, so the transmitting and receiving coils are oriented in parallel. Therefore, only the  $z$ -component of the magnetic flux density is considered. Based on the ranges of  $P_o$  and  $R_o$  in (1) and (2), the minimum and maximum values of the  $z$ -component of the

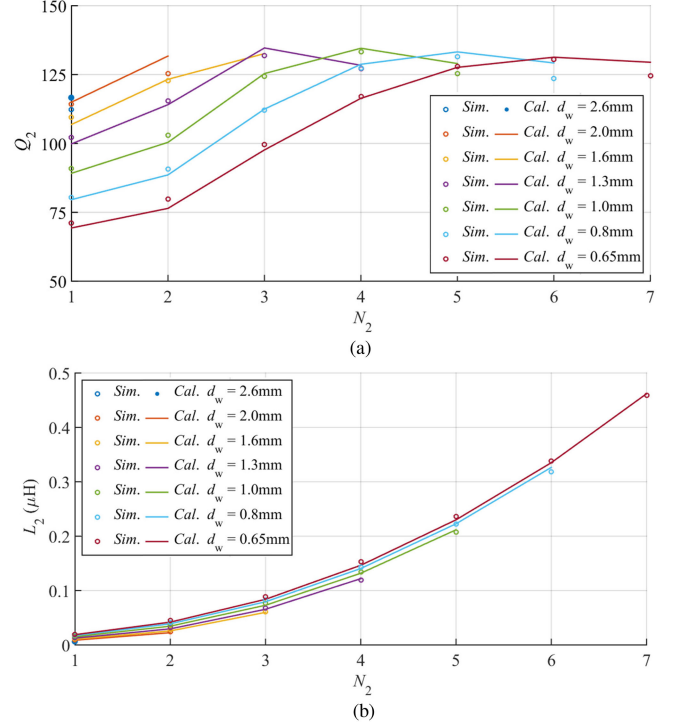


Fig. 4.  $Q_2 - N_2$  and  $L_2 - N_2$  under different  $d_w$  and with the same outer coil dimension ( $11.5 \times 6 \times 6 \text{ mm}^3$ ). (a) Quality factor. (b) Self-inductance.

magnetic flux density,  $B_{z,\text{min}}$  and  $B_{z,\text{max}}$ , respectively, are

$$B_{z,\text{min}} = \frac{\sqrt{R_{o,\text{min}} P_{o,\text{min}}}}{\omega N_2 A_2} \left| \frac{(R_{o,\text{min}} + X_{C22})(Z_{\text{IM1},\text{min}} + Z_2)}{R_{o,\text{min}} Z_{\text{IM1},\text{min}}} \right| \quad (17a)$$

$$B_{z,\text{max}} = \frac{\sqrt{R_{o,\text{max}} P_{o,\text{max}}}}{\omega N_2 A_2} \left| \frac{(R_{o,\text{max}} + X_{C22})(Z_{\text{IM1},\text{max}} + Z_2)}{R_{o,\text{max}} Z_{\text{IM1},\text{max}}} \right| \quad (17b)$$

where  $Z_{\text{IM1},\text{min}} = \frac{X_{C21}(X_{C22} + R_{o,\text{min}})}{X_{C21} + X_{C22} + R_{o,\text{min}}}$  and  $Z_{\text{IM1},\text{max}} = \frac{X_{C21}(X_{C22} + R_{o,\text{max}})}{X_{C21} + X_{C22} + R_{o,\text{max}}}$ .

Let  $\Delta B_z$  be the variation of  $B_z$

$$\Delta B_z = \frac{B_{z,\text{max}} - B_{z,\text{min}}}{B_{z,\text{min}}} \quad (18)$$

##### C. Optimization of the Transmitting Coil

Commercially available cages for rodent animals [44], [45] are selected. The dimensions are  $400 \times 240 \times 200 \text{ mm}^3$ . The operating zone has the same footprint as the cage and the height to cover the vertical movement of the receiver while the animal is walking and standing [8]–[10], [17]–[21]. The operating zone is  $400 \times 240 \times 40 \text{ mm}^3$ . The Cartesian coordinate system is defined in Fig. 5. The centers of the operating zone and the transmitting coil are the same and defined as the origin. The center of the operating zone is 70 mm above the floor of the cage. The dimensions of the upper and lower windings are the

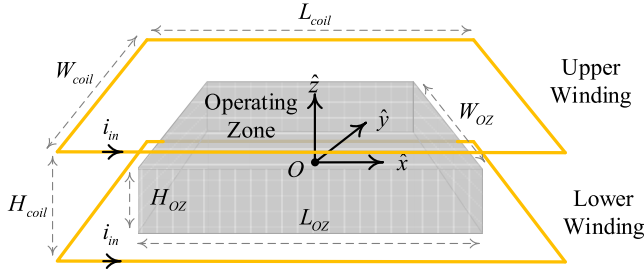


Fig. 5. Setup of transmitting coil and operating zone.

same. The coil length and width are denoted by  $L_{\text{coil}}$  and  $W_{\text{coil}}$ , respectively. The coil separation is denoted by  $H_{\text{coil}}$ . The length, width, and height of the operating zone are denoted by  $L_{\text{OZ}}$ ,  $W_{\text{OZ}}$ , and  $H_{\text{OZ}}$ , respectively.

The transmitting coil is designed to provide the same or lower variation of the magnetic flux density within the operating zone (see Section IV-C). The dimensions and separation of the two windings are minimized. The variation of the magnetic flux density is calculated numerically. To generalize the analysis of the generated magnetic field, the dimensions of the operating zone are normalized by the transmitting coil and three ratios, LR, WR, and HR, are defined as

$$\text{LR} = \frac{L_{\text{OZ}}}{L_{\text{coil}}} \quad (19a)$$

$$\text{WR} = \frac{W_{\text{OZ}}}{W_{\text{coil}}} \quad (19b)$$

$$\text{HR} = \frac{H_{\text{OZ}}}{H_{\text{coil}}}. \quad (19c)$$

Since  $L_{\text{OZ}} < L_{\text{coil}}$ ,  $W_{\text{OZ}} < W_{\text{coil}}$ , and  $H_{\text{OZ}} < H_{\text{coil}}$ , LR, WR, and HR all are less than 1. To simplify the analysis, the footprints of the operating zone and the coil have the same aspect ratios. Thus

$$\text{WR} = \text{LR}. \quad (20)$$

The ratio of the footprint areas between the operating zone and the coil, AR, is given by

$$\text{AR} = \text{LR}^2. \quad (21)$$

The z-component of the magnetic flux density at  $(x, y, z)$  [46] generated by the upper and lower windings,  $B_{1z}$  and  $B_{2z}$ , respectively, is

$$B_{1z}(x, y, z) = \frac{\mu_0 i_{\text{in}}}{4\pi L_{\text{coil}}} \sum_{k=1}^4 \frac{(-1)^k g_k}{\delta_{1k} [\delta_{1k} + (-1)^{(k+1)} e_k]} - \frac{e_k}{\delta_{1k} (\delta_{1k} + g_k)} \quad (22a)$$

$$B_{2z}(x, y, z) = \frac{\mu_0 i_{\text{in}}}{4\pi L_{\text{coil}}} \sum_{k=1}^4 \frac{(-1)^k g_k}{\delta_{2k} [\delta_{2k} + (-1)^{(k+1)} e_k]} - \frac{e_k}{\delta_{2k} (\delta_{2k} + g_k)} \quad (22b)$$

where  $g_k$ ,  $e_k$ ,  $\delta_{1k}$ , and  $\delta_{2k}$  are given in Appendix B.

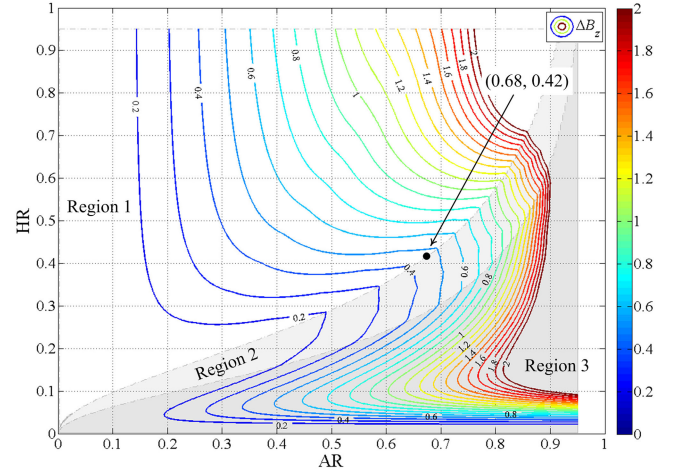


Fig. 6.  $\Delta B_z$  and position for  $B_{1A,\text{min}}$  versus HR and AR. ( $L_{\text{OZ}} \times W_{\text{OZ}} \times H_{\text{OZ}} = 400 \times 240 \times 40 \text{ mm}^3$ )

The z-component of the resultant magnetic flux density  $B_z$  is obtained by  $B_{1z}$  and  $B_{2z}$

$$B_z(x, y, z) = B_{1z}(x, y, z) + B_{2z}(x, y, z). \quad (23)$$

Since the transmitting coil and the operating zone are concentric and symmetric about the x-, y-, and z-axes, the profile of  $B_z$  is symmetric and only  $B_z$  in the positive coordinates is needed. The ranges of the Cartesian coordinates are confined by the dimensions of the operating zone, i.e.,  $x \in [0, L_{\text{OZ}}/2]$ ,  $y \in [0, W_{\text{OZ}}/2]$ , and  $z \in [0, H_{\text{OZ}}/2]$ .

$B_z$  at each point is calculated by using (11) and (13) with  $i_{\text{in}} = 1 \text{ A}$ . The minimum and maximum values of  $B_z$  are determined by a numerical approach and expressed as

$$B_{1A,\text{min}} = \arg \min_{x,y,z} B_z(x, y, z) \quad (24a)$$

$$B_{1A,\text{max}} = \arg \max_{x,y,z} B_z(x, y, z). \quad (24b)$$

$\Delta B_z$  is calculated by (18) and (24a) and (24b). Fig. 6 shows the contour lines with  $\Delta B_z$  under different AR and HR. The contours with  $\Delta B_z$  for four normalized operating zones are presented in [36].

The geometric parameters, AR and HR, with respect to the coil dimensions can be determined, while the variation of the magnetic flux density,  $\Delta B_z$ , can be confined within the designed allowable variation in Section IV-C. The transmitting coil size and separation are minimized by maximizing AR and HR. The combinations of AR and HR are chosen to be the tip of the curve with AR maximum, as marked in Fig. 6.  $L_{\text{coil}}$ ,  $W_{\text{coil}}$ , and  $H_{\text{coil}}$  are calculated by solving (19a), (19b), (19c)–(21).

#### D. Transmitting Coil Current

The rms value of the transmitting coil current,  $i_{\text{in}}$ , is thus determined by

$$i_{\text{in}} = \frac{B_{z,\text{min}}}{N_1 B_{1A,\text{min}}} \quad (25)$$

TABLE II  
COORDINATES OF  $B_{1A,\min}$  AT REGIONS 1–3 IN FIG. 6

Region	Coordinates for $B_{1A,\min}$		
	$x$	$y$	$z$
1	0	0	$H_{oz}/2$
2	0	$W_{oz}/2$	0
3	$L_{oz}/2$	$W_{oz}/2$	0

where  $N_1$  is the number of turns of the upper/lower winding in the transmitting coil, and  $B_{z,\min}$  is determined by (17a).

Fig. 6 shows the regions of the corresponding position of  $B_{1A,\min}$  with different  $\Delta B_z$ , AR, and HR. The coordinates of the positions are given in Table II.  $B_{1A,\min}$  can be obtained by substituting the coordinates and the coil dimensions into (22a), (22b), and (23).

## V. EXPERIMENTAL PROTOTYPE

The performances of the WPT system are verified and evaluated on a prototype shown in Fig. 7. The circuit schematic is shown in Fig. 2. The design specifications are shown in Table III. The system design is based on the considerations described in Sections III and IV. A transmitting coil with two turns, one for the upper winding and one for the lower winding, is designed. It is shown in Fig. 7(a). The centers of the operating zone and the transmitting coil are the same and 70 mm above the floor of the cage. The parameters and component values are tabulated in Table IV. Each winding is divided into four segments and each segment is connected to another segment through a capacitor, so as to reduce the coil voltage [24], [26] by canceling the effect of the self-inductance of each segment of the transmitting coil. The operating frequency is set to 6.78 MHz, within the industrial, scientific, and medical radio band. The details of the driver design have been presented in [36]. A prototype receiver, shown in Fig. 7(b), is built and the component values are given in Table V. The dimensions of the entire receiver are  $24.5 \times 13 \times 16 \text{ mm}^3$ . The electrical parameters of the coil are measured by an impedance analyzer (Hewlett Packard 4194A).

### A. Comparison on the Theoretical and Measured Magnetic Flux Density

Fig. 8 shows the contour lines of  $B_z$ , calculated by (22a), (22b), and (23), on the  $XY$  plane at  $z = 0$ .  $i_{in}$  equals 2 A. The shaded regions indicate the operating zone. The transmitting coil generates a uniform magnetic flux profile within the operating zone. The coil dimensions are optimized. The contour line density is significantly increased and  $B_z$  is suddenly changed outside the operating zone. The measured  $B_z$  are marked with “square boxes.” The calculated and measured results are in close agreement. Their mean and maximum differences are found to be 1.8% and 6.35%, respectively. The variation of the flux

density,  $\Delta|B_z|$ , found in the experimental prototype is 0.475, satisfying the allowable variation of 0.49 given in Table III. The calculated and measured values of  $B_z$  at  $z = -20 \text{ mm}$  and  $z = 20 \text{ mm}$  are given in the media file.

### B. Performance of the WPT System

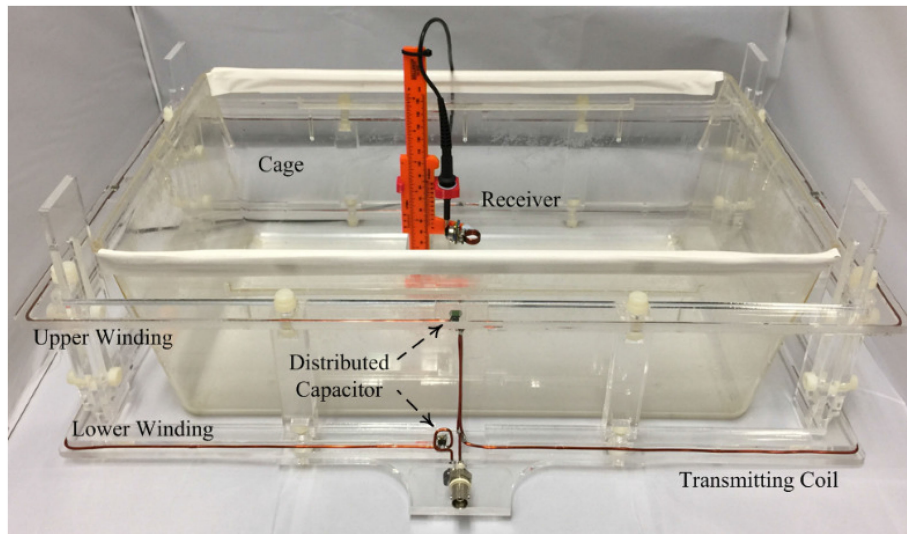
The output power of the receiver is studied on a constant output resistor. The rectifying circuit is replaced by an output resistor of  $46.2 \Omega$ . Fig. 9 shows the output power  $P_o$  on  $R_{o,mea}$  over  $XY$  plane at  $z = 0 \text{ mm}$ . The results of  $P_o$  at  $z = -20 \text{ mm}$  and  $z = 20 \text{ mm}$  are given in the media file. The calculated and measured results are in close agreement. Their mean and maximum absolute differences are found to be 3.17% and 7.60%, respectively. The error is relatively significant near the boundary of the operating zone due to the abrupt change of the magnetic flux density. The minimum  $P_o$  is 173 mW, which can meet the design requirement of 170 mW.

The operation of the diode-bridge rectifier and the LDO is taken into consideration. The output voltage of the diode-bridge rectifier,  $V_{rect}$ , is estimated and verified experimentally. Fig. 10 shows the profile of the rectifier voltage  $V_{rect}$  on  $XY$  plane at  $z = 0 \text{ mm}$ . The results of  $V_{rect}$  at  $z = -20 \text{ mm}$  and  $z = 20 \text{ mm}$  are given in the media file. The calculated and measured results are in close agreement. Their mean and maximum absolute differences are 2.81% and 6.98%, respectively.  $V_{rect,cal}$  varies between 2.52 and 5.46 V, within the requirement in Table III.

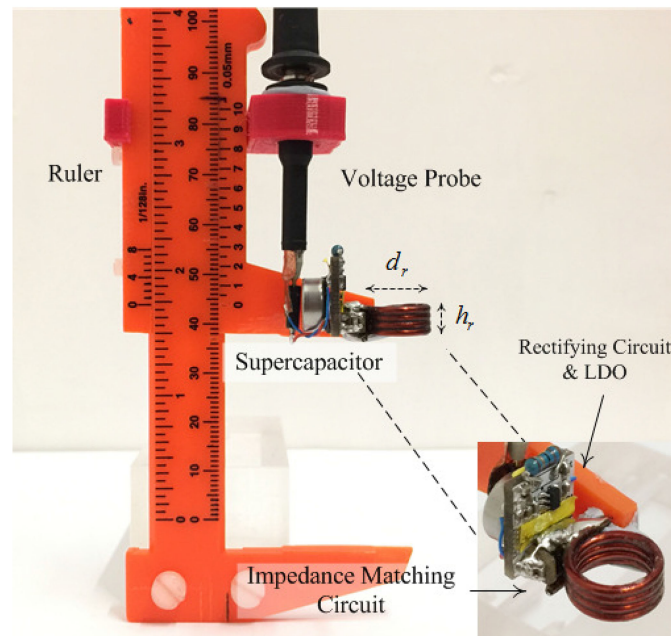
## VI. EVALUATION OF SAR

BRs and maximum permissible exposures (MPEs) are recommended in [27] as safety levels to protect human body from adverse heating effects under exposures to electromagnetic fields. The BR of localized exposure for the general public is measured by SAR and is equal to 2 W/kg, which is an averaged value over any 10 g of tissue. Based on the BRs, the MPEs measured by the magnetic field strength are introduced and obtained by mathematical modeling and extrapolation from the experimental results at specific frequencies. It is mentioned in [27] that, in near-field applications, MPEs may not ensure compliance with the BR on local SAR and it may be necessary to directly evaluate the level of local SAR. Therefore, exposures to electromagnetic fields in WPT applications should be directly evaluated by the BRs, i.e., local SAR, instead of MPEs, i.e., the magnetic field strength.

The SAR level in the animal is contributed by the magnetic field generated by the current passing through the transmitting coil and receiving coil. In [36], only the magnetic field of the transmitting coil is studied. However, as the receiving coil is just attached on the animal, they are closely coupled. The SAR level caused by the receiving coil could be relatively significant. The local SAR level with the rat model is simulated by COMSOL Multiphysics [43]. Fig. 11 shows the geometrical setup of the simulation. The dimensions of the transmitting coil and the transmitting coil current are given in Table IV. The dimensions of the receiving coil are given in Table V and the receiving coil



(a)



(b)

Fig. 7. Experimental setup. (a) Overall system. (b) Receiver and load.

TABLE III  
DESIGN PARAMETERS AND ELECTRONIC COMPONENTS FOR THE WPT SYSTEM

$P_L$ (mW)	$V_L$ (V)	$V_{rect}$ (V)	$P_o$ (mW)	$R_o$ ( $\Omega$ )	LDO	Diodes
100	1.80	2.5 ~ 5.5	170 ~ 340	45.3 ~ 89.0	LP2985	DB2J20900L

current is determined with the equivalent circuit in Fig. 2. A rat model composed of muscle tissue is used in the simulation, [47]–[48]. The physical parameters and electrical properties of the rat model used in the SAR simulation are summarized in Table VI.

The SAR on the rat model is determined by the maximum averaged value over a 10 g tissue. The maximum averaged SAR

at different positions is determined and given in Table VII. The value of SAR is much lower than the BR recommended in [27]. The highest SAR is around one-hundredth of the restriction level when the rat model is located at  $x = 150$  mm and  $y = -40$  mm. This implies that there is a room for further increasing the transferred power and reducing the size of the receiving coil. Local SAR normalized by the BR in dB value,  $\hat{S}AR$ , is defined

TABLE IV  
 PARAMETERS OF THE TRANSMITTING COIL AND THE OPERATING ZONE USED IN THE EXPERIMENT

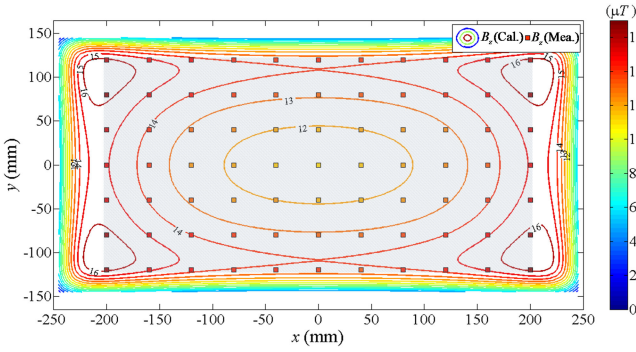
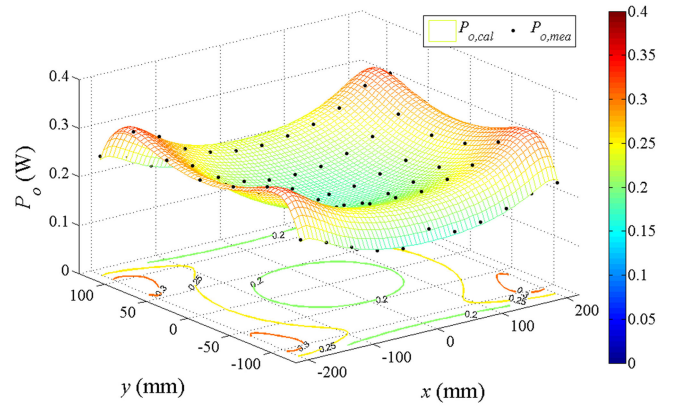
$C_1$ (nF)	$L_1$ ( $\mu$ H)	$r_1$ ( $\Omega$ )	$N_1$	$i_{in}$ (A)	$f$ (MHz)
0.141	3.91	1.01	1	2.00	6.78
$B_{1A,min}$ ( $\mu$ T)	$L_{coil}$ (mm)	$W_{coil}$ (mm)	$H_{coil}$ (mm)	AR, HR	Wire size
5.68	490	290	95	0.68, 0.42	14 AWG

\* $C_1$  is the equivalent capacitance of the series resonant capacitors distributed over the transmitting coil.

 TABLE V  
 PARAMETERS OF THE RECEIVING COIL AND IMPEDANCE MATCHING CIRCUIT USED IN THE EXPERIMENT

$C_{rect}$ (mF)	$C_{21}$ (nF)	$C_{22}$ (nF)	$L_2$ ( $\mu$ H)	$r_2$ ( $\Omega$ )	$N_2$
100	3.48	0.13	0.153	0.057	4
$B_z$ ( $\mu$ T)	$\Delta B_z$	$d_r$ (mm)	$h_r$ (mm)	Wire size	Weight (g)*
11.3 ~ 16.8	0.49	11.45	5.80	16 AWG	4.80

\*Total weight of the receiver, including the receiving coil, matching capacitors, supercapacitors, LDO, and the load.

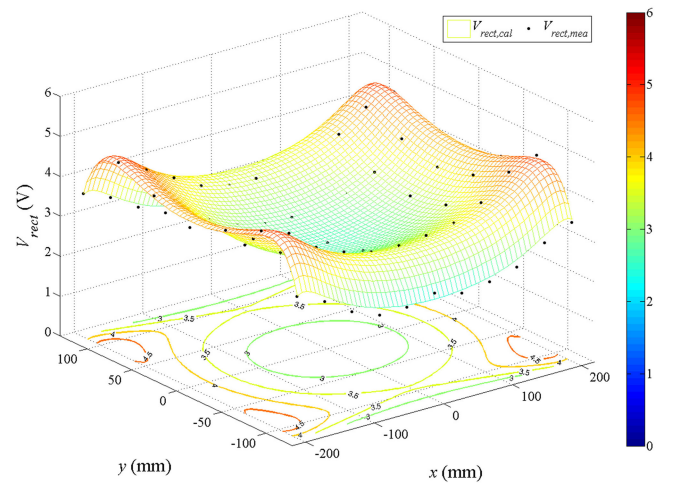

 Fig. 8. Calculated and measured  $B_z$  at  $z = 0$  mm.

 Fig. 9. Calculated and measured  $P_o$  on  $R_{o,mea}$  at  $z = 0$  mm.

as follows:

$$\hat{SAR} = \log_{10} \left( \frac{SAR_{sim}}{SAR_{BR}} \right) \quad (26)$$

where  $SAR_{sim}$  and  $SAR_{BR}$  are the simulated local SAR level and BR, respectively.

A zero value of  $\hat{SAR}$  represents  $SAR_{sim}$  equals the BR. Fig. 12 shows the normalized local SAR located at  $x = 150$  mm and  $y = -40$  mm. The maximum and minimum  $\hat{SAR}$  are  $-0.1$  and  $-6.2$ , respectively. The magnetic flux density distribution in the rat model at the same position is shown in Fig. 13. The distributions viewed at different angles are given in the media file. The maximum and minimum magnetic flux densities are around 187 and 1.37  $\mu$ T, respectively. For the frequency of 6.78 MHz, MPEs in term of the magnetic flux density [27] equals 3.02  $\mu$ T. Although the magnetic field exposure is over five times higher than the MPEs as suggested in [27], the averaged SAR over 10 g tissue is much lower than the BR. Thus, evaluation on the local SAR is required.


 Fig. 10. Calculated and measured  $V_{rect}$  at  $z = 0$  mm.

## VII. DISCUSSIONS

Based on the aforementioned investigations, the following observations are noted.

TABLE VI  
PHYSICAL PARAMETERS AND ELECTRICAL PROPERTIES OF THE RAT MODEL

Length (mm)	Width (mm)	Height (mm)	Weight (g)	Density (kg/mm <sup>3</sup> )	Relative Permittivity	Electrical Conductivity (S/m)
160	50	70	580	1040	233.27	0.602

TABLE VII  
MAXIMUM AVERAGED SAR OVER 10 g OF TISSUE ON THE RAT MODEL

SAR (mW/kg)							
x (mm) \ y (mm)	-150	-100	-50	0	50	100	150
40	10.64	9.41	8.91	8.80	9.02	9.69	14.15
-40	12.12	11.16	10.87	10.95	11.47	12.74	15.80

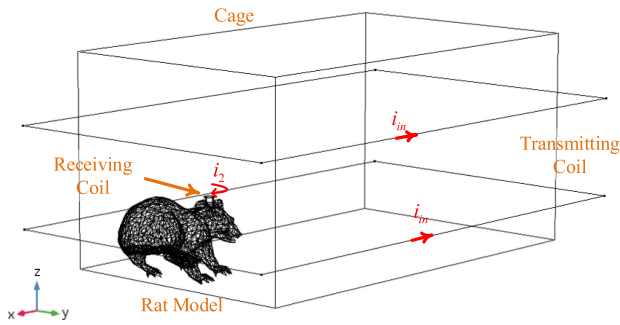


Fig. 11. Geometrical setup of the SAR simulation on the rat model.

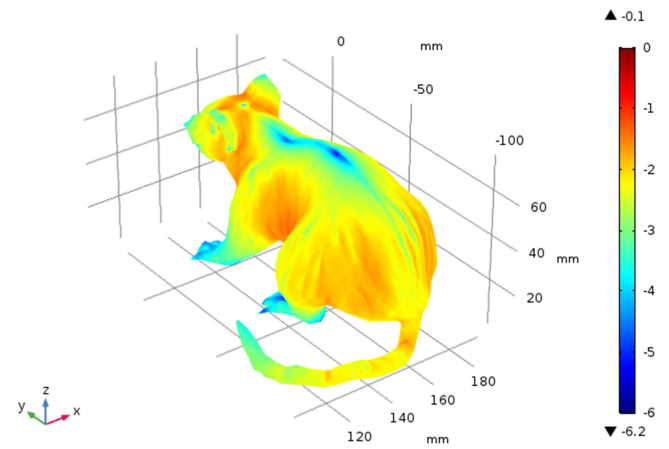


Fig. 12. Normalized local SAR on the rat model in dB value.

- 1) The proposed system does not require dedicated position tracking circuit or wireless communication link. It delivers sufficient and regulated power to the load over a commonly used cage footprint. The transmitting coil is in reasonable dimensions and the receiving coil is relatively small. The SAR level is simulated to be much lower than the BR. Table VIII shows a comparison on the proposed system design with prior art.
- 2) The steps of designing the dimensions of the transmitting coil are given in Sections III and IV. The magnetic flux density will vary within the design range. The load can still receive sufficient power, even if the receiving coil is located at a location with minimum flux density.
- 3) The magnetic field flux density can be made more homogeneous in the operating zone by increasing the size, but the excitation current needs to be increased accordingly to achieve the same field strength.
- 4) Angular misalignments will affect the power transmitted from the transmitter to the receiver. Since the output power to the load is regulated,  $V_{\text{rect}}$  will decrease as angular misalignment increases. As shown in Fig. 10, without angular misalignment, the minimum value of  $V_{\text{rect}}$ ,  $V_{\text{rect,min}}$ , within the operating zone is 2.5 V. As  $V_{\text{rect}}$  further decreases, the voltage regulation capability of the LDO will be affected. However, as discussed in

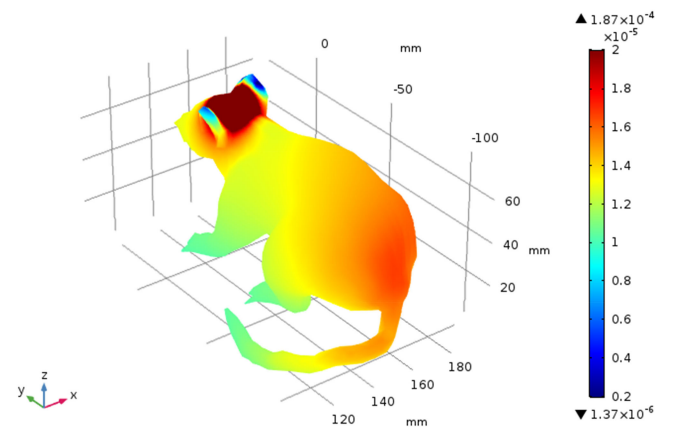
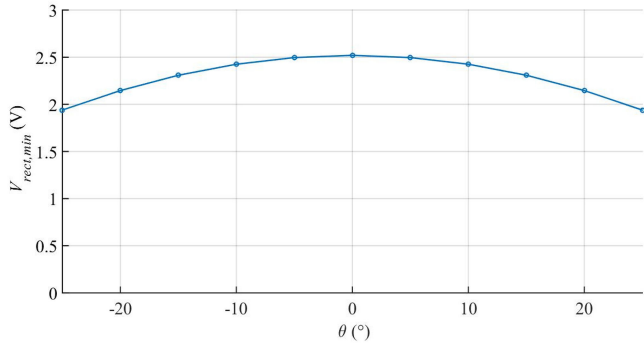
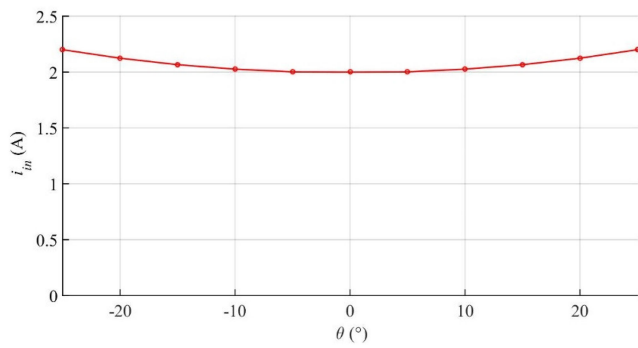


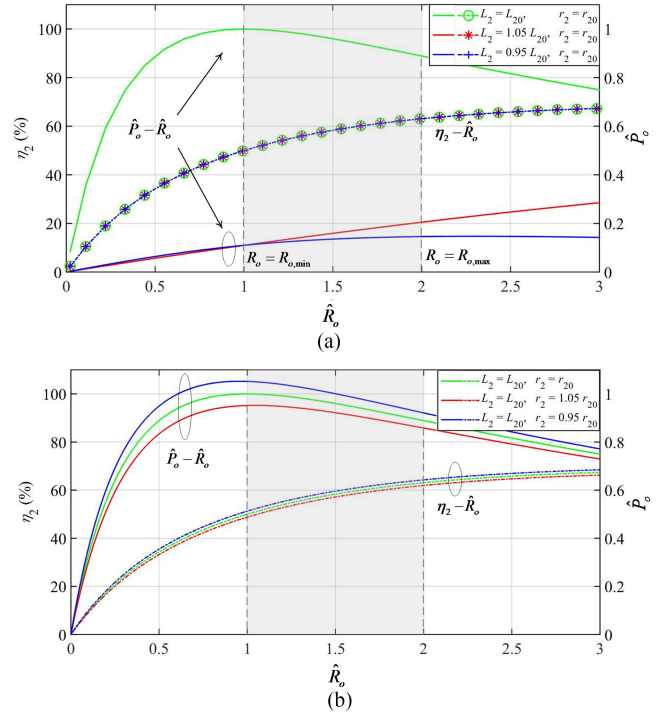
Fig. 13. Magnetic flux density distribution on the rat model.

[32], [49], and [50], the animals have their four limbs mostly stepped on the cage, so the angular misalignment, due to the head shaking and body movement, will not be large. As discussed in [50], the angular misalignment ranges between  $-25^\circ$  and  $+25^\circ$ . Fig. 14 shows that  $V_{\text{rect}}$


 Fig. 14.  $V_{\text{rect},\text{min}}$  versus angular misalignment with  $i_{\text{in}} = 2$  A.

 Fig. 15. Required value of  $i_{\text{in}}$  versus angular misalignment with  $V_{\text{rect},\text{min}} = 2.5$  V.

reduces from 2.5 to 2 V within the aforementioned range of angular misalignment. In order to maintain  $V_{\text{rect},\text{min}}$  at 2.5 V, the transmitting coil current  $i_{\text{in}}$  needs to be increased to 2.2 A. Thus, as illustrated in Fig. 15, the effect of angular misalignment, due the movement of the head of the animal, can be tackled by increasing the transmitting coil current by 10%.

- 5) Since the designed transmitting coil is placed between the top and bottom of the cage to cover the operating zone of the receiving coil (rat model), the coupling coefficient between the transmitting coil and the receiving coil is larger than that generated by the transmitting coil (or array of coils) placed at the bottom and/or at the top of the cage [8]–[10], [17]–[21]. Regardless of which arrangement of the transmitting coil is used, the required magnetic flux density at the receiving coil should be the same in order to deliver the same load power. However, when the transmitting coils are placed at the bottom and/or the top of the cage, the magnetic flux and its variation around the bottom and/or the top of the cage would be higher than the proposed arrangement [9].
- 6) The system operates at the maximum power transfer to minimize the SAR in the animal tissues. In Fig. 3, take  $\hat{C}_{21} = 0$ . At the maximum power transfer condition,  $\eta_2 = 50\%$  and  $\hat{P}_o = 1.00$ . At the maximum efficiency condition,  $\eta_2 = 94\%$  and  $\hat{P}_o = 0.15$ . With the same output power, operating the system at the maximum power


 Fig. 16.  $\eta_2$ – $\hat{R}_o$  and  $\hat{P}_o$ – $\hat{R}_o$  with the same transmitting coil current and matching circuit. (a) Variation of  $L_2$ . (b) Variation of  $r_2$ .

transfer condition requires lower transmitting coil current than that at the maximum efficiency condition. It is thus preferable to operate the system at the former condition to minimize the SAR.

- 7) The impedance matching is crucial in the WPT technology [51]. Fig. 16 shows the normalized output power  $\hat{P}_o$  and efficiency  $\eta_2$  versus  $\hat{R}_o$  with the same transmitting coil current and matching circuit. Fig. 16(a) shows the results with the variations of the receiving coil inductance  $L_2$ . When  $L_2$  has variation of 5%,  $\eta_2$  remains almost unchanged but  $\hat{P}_o$  decreases. Fig. 16(b) shows the results with the variations of the receiving coil resistance  $r_2$ . When  $r_2$  has variation of 5%,  $\eta_2$  varies less than 2% and  $\hat{P}_o$  has variation of 5%. The matching circuit in the prototype achieves a good matching condition. The measured results in Figs. 9 and 10 are in close agreement with the design.
- 8) The commercially available capacitors can provide sufficient accuracy to achieve good matching condition. The capacitors are of mica type [38]. The matching circuit is designed to receive sufficient power from the transmitter under the worst-case situation, where  $R_o = R_{o,\text{min}}$ .  $R_{o,\text{min}} = 45.3 \Omega$ . The measured output impedance  $Z_{\text{IM2,mea}}$  of the matching circuit is measured by HP 4194A and is shown in Fig. 17. The value of  $Z_{\text{IM2}}$  is equal to  $46.1 \angle -0.72^\circ \Omega$ . The difference between the matching circuit and the output load is less than 2%. Therefore, the matching circuit can well match the receiving coil with the rectifier circuit.

TABLE VIII  
COMPARISON WITH PRIOR ART

	2014 [17]	2015 [9]	2015 [18]	2016 [10]	2017 [23]	This work
Cage footprint (mm <sup>2</sup> )	580×610	360×180	300×300	225×225	460×240	400×240
Outer Dimension of Transmitting Coil Set (mm <sup>2</sup> /mm <sup>3</sup> )	1030×900	540×300	280×80	270×270×160	440×240×200	490×290×95
Outer Dimension of Receiving Coil Set (mm <sup>2</sup> /mm <sup>3</sup> )	40×40	40×40×20	25×25	44×44	22×20×11	11.5×11.5×5.8
DC Output Power (mW)	20	215	24	100	40	100
Excitation frequency (MHz)	13.56	1.5	13.56	13.56	13.56	6.78
Wireless communication	Yes	No	Yes	No	Yes	No
Intelligent Checking System	Yes	Yes	Yes	No	No	No
Simulation of SAR in the animal	No	No	No	No	Yes	Yes

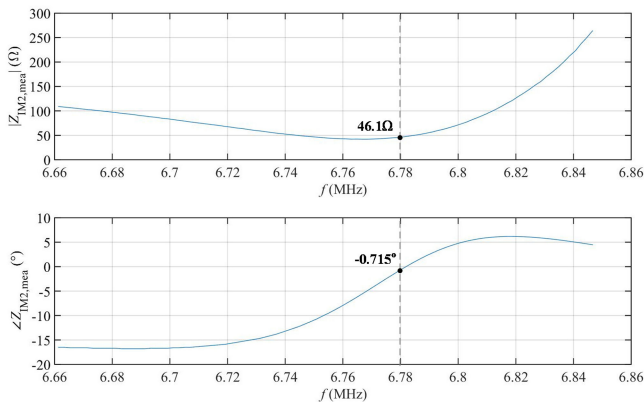


Fig. 17. Measured output impedance  $Z_{IM2,mea}$  of the matching circuit versus frequency.

- 9) Compared with the multi-coil structures with intelligent control to excite the coil(s) placed under the rat model, the proposed arrangement is not optimized at the maximum power transfer efficiency. However, the power level of electrophysiological applications is usually low (less than 100 mW). Although the power transfer efficiency is between 7.5% and 3.8%, the power loss on the transmitting coil is only around 4 W. The transfer efficiency is not a major concern in this application. Instead, the circuit elegance is the primary consideration. In fact, driving the coils in an intelligent way would cause extra power consumption that might be higher than the power loss of the entire system. For example, a lot of power is consumed on the computer to operate the intelligent tracking system.
- 10) The optimal circuit configuration for matching the impedance between the receiving coil and the load to achieve maximum power transfer is found to be a shunt-series capacitor network. It can minimize the overall size

of the matching circuit and maintain the power efficiency of the receiver over 50%.

- 11) As the transmitting coil wires wound around the cage are thin, the coil does not noticeably block the line of sight to observe the behavior and movement of the animal. Such an arrangement has such merit over the one having multiple coils placed on the top of the cage. The proposed system also allows conducting experiments with multiple animals in the cage.
- 12) Currently, the receiving coil is fixed on the head of the animal and the wireless power is transferred through the air. In the future, the receiving coil with biocompatible packaging is possible to be implanted into the animal's body [52].

## VIII. CONCLUSION

A generalized design approach for the WPT system with the transmitting coil made of two rectangular coaxial windings connected in series and wrapped around an animal cage for electrophysiological application has been presented. The generated magnetic flux density with different transmitting coil dimensions and the operating zone has been assessed. An impedance matching circuit in the receiver is designed to maximize output power instead of power transfer efficiency to minimize the transmitting coil current and the SAR. The physical volume of the matching circuit is optimized. A testing prototype has been fabricated. Experimental results have been verified that the WPT system can deliver an output power of 100 mW dc with an 11.45-mm receiving coil in the cage footprint of  $400 \times 240$  mm<sup>2</sup>. The SAR is evaluated with finite-element simulation. The highest SAR level is found to be much lower than the limit suggested by the international standards [27]. Moreover, evaluation on the local SAR is required.

## APPENDIX

## A. Expressions of the Parameters in (15) and (16)

$$\begin{aligned}
 k_c &= \sqrt{\frac{d_r^2}{d_r^2 + \Delta_{ij}^2}}, k_m = 0.3379 \left(1 - \frac{1 - 0.01711}{N_2 - 0.01711}\right) \\
 &+ \ln(N_2) \left(\frac{-0.16641}{N_2} + \frac{0.00479}{N_2^2} + \frac{0.001772}{N_2^3}\right) \\
 k_s &= \frac{5}{4} - \ln\left(\frac{2d_t}{d_w}\right), \Delta_{ij} = \frac{h_r - d_r}{N_2 - 1} |i - j|, \delta = \frac{1}{\sqrt{\mu_0 \sigma \pi f}}, \\
 \Phi_{\text{cond}}(x) &= \text{Re} \left\{ \frac{(-1 + j)x}{2} \frac{J_0[(-1 + j)x]}{J_1[(-1 + j)x]} \right\} \\
 \Phi_{\text{ind}}(x) &= \text{Re} \left\{ jx^2 \frac{J_2[(-1 + j)x]}{J_1[(-1 + j)x]} \right\}, \langle H_p^2 \rangle \\
 &= \sum_{i=1}^{N_2} \sum_{j=1}^{N_2} (H_z^2 + H_r^2) (1 - \psi_{ij}), H_z = \frac{K(k_c) - E(k_c)}{2\pi \sqrt{\Delta_{ij}^2 + d_r^2}}.
 \end{aligned}$$

$H_r = \frac{\Delta_{ij}}{\pi d_r \sqrt{\Delta_{ij}^2 + d_r^2}} \left[ \frac{2\Delta_{ij}^2 + d_r^2}{2\Delta_{ij}^2} E(k_c) - K(k_c) \right], \psi_{ij} = 1$ 
 for  $(i = j)$ ,  $d_r$  and  $h_r$  are the diameter and the height of the receiving coil, respectively,  $d_t$  is the diameter of the conducting wire with insulation layer,  $K$  and  $E$  are the complete elliptic integral of the first and second kind, respectively,  $\sigma_{\text{Cu}}$  is the electrical conductivity of copper,  $\langle H_p^2 \rangle$  is the average of the square field over the turn  $p^{\text{th}}$  per ampere of current,  $J_0$ ,  $J_1$ , and  $J_2$  are the Bessel functions of the first kind and order 0, 1, and 2, respectively.

## B. Expressions of the Parameters in (22a) and (22b)

$$\begin{aligned}
 \delta_{11} &= \sqrt{\left(\frac{L_{\text{coil}}}{2} + x\right)^2 + \left(y + \frac{W_{\text{coil}}}{2}\right)^2 + \left(z - \frac{H_{\text{coil}}}{2}\right)^2}, \\
 \delta_{12} &= \sqrt{\left(\frac{L_{\text{coil}}}{2} - x\right)^2 + \left(y + \frac{W_{\text{coil}}}{2}\right)^2 + \left(z - \frac{H_{\text{coil}}}{2}\right)^2}, \\
 \delta_{13} &= \sqrt{\left(\frac{L_{\text{coil}}}{2} - x\right)^2 + \left(y - \frac{W_{\text{coil}}}{2}\right)^2 + \left(z - \frac{H_{\text{coil}}}{2}\right)^2}, \\
 \delta_{14} &= \sqrt{\left(\frac{L_{\text{coil}}}{2} + x\right)^2 + \left(y - \frac{W_{\text{coil}}}{2}\right)^2 + \left(z - \frac{H_{\text{coil}}}{2}\right)^2}, \\
 \delta_{21} &= \sqrt{\left(\frac{L_{\text{coil}}}{2} + x\right)^2 + \left(y + \frac{W_{\text{coil}}}{2}\right)^2 + \left(z + \frac{H_{\text{coil}}}{2}\right)^2}, \\
 \delta_{22} &= \sqrt{\left(\frac{L_{\text{coil}}}{2} - x\right)^2 + \left(y + \frac{W_{\text{coil}}}{2}\right)^2 + \left(z + \frac{H_{\text{coil}}}{2}\right)^2}, \\
 \delta_{23} &= \sqrt{\left(\frac{L_{\text{coil}}}{2} - x\right)^2 + \left(y - \frac{W_{\text{coil}}}{2}\right)^2 + \left(z + \frac{H_{\text{coil}}}{2}\right)^2},
 \end{aligned}$$

$$\begin{aligned}
 \delta_{24} &= \sqrt{\left(\frac{L_{\text{coil}}}{2} + x\right)^2 + \left(y - \frac{W_{\text{coil}}}{2}\right)^2 + \left(z + \frac{H_{\text{coil}}}{2}\right)^2} \\
 e_1 &= \frac{L_{\text{coil}}}{2} + x, e_2 = \frac{L_{\text{coil}}}{2} - x, e_3 = -\left(\frac{L_{\text{coil}}}{2} - x\right), \\
 e_4 &= -\left(\frac{L_{\text{coil}}}{2} + x\right), g_1 = y + \frac{W_{\text{coil}}}{2}, g_2 = g_1, \\
 g_3 &= y - \frac{W_{\text{coil}}}{2}, \text{ and } g_4 = g_3.
 \end{aligned}$$

## REFERENCES

- [1] Y. Lin *et al.*, "A battery-less, implantable neuro-electronic interface for studying the mechanisms of deep brain stimulation in rat models," *IEEE Tran. Biomed. Circuits Syst.*, vol. 10, no. 1, pp. 98–112, Mar. 2015.
- [2] K. Nowak *et al.*, "Optimizing a rodent model of Parkinson's disease for exploring the effects and mechanisms of deep brain stimulation," *Parkinson's Dis.*, vol. 2011, pp. 1–19, Apr. 2011, doi: [10.4061/2011/414682](https://doi.org/10.4061/2011/414682).
- [3] M. A. Lebedev and M. A. L. Nicolelis, "Brain-machine interfaces: Past, present and future," *Trends Neurosci.*, vol. 29, no. 9, pp. 536–546, Jul. 2006.
- [4] C. Hamani, M. Diwan, S. Isabella, A. Lozano, and J. N. Nobrega, "Effects of different stimulation parameters on the antidepressant-like response of medial prefrontal cortex deep brain stimulation in rats," *J. Psychiatric Res.*, vol. 44, no. 11, pp. 683–687, Jan. 2010.
- [5] A. Aravanis *et al.*, "An optical neural interface: In vivo control of rodent motor cortex with integrated fiberoptic and optogenetic technology," *J. Neural Eng.*, vol. 4, no. 3, pp. 143–156, 2007.
- [6] R. Normann, E. Maynard, P. Rousche, and D. Warren, "A neural interface for a cortical vision prosthesis," *Vis. Res.*, vol. 39, no. 15, pp. 2577–2587, 1999.
- [7] Q. Wang, H. R. Brunner, and M. Burnier, "Determination of cardiac contractility in awake unsedated mice with a fluid-filled catheter," *Amer. J. Physiol. Heart Circle Physiol.*, vol. 286, no. 2, pp. 806–814, 2004.
- [8] U. Jow, M. Kiani, X. Huo, and M. Ghovanloo, "Towards a smart experimental arena for long-term electrophysiology experiments," *IEEE Trans. Biomed. Circuits Syst.*, vol. 6, no. 5, pp. 414–423, Oct. 2012.
- [9] N. Soltani, M. S. Aliroth, M. T. Salam, J. Luis, and P. Velazquez, "Low-radiation cellular inductive powering of rodent wireless brain interfaces: Methodology and design guide," *IEEE Trans. Biomed. Circuits Syst.*, vol. 10, no. 4, pp. 920–932, Aug. 2016.
- [10] S. A. Mirbozorgi, H. Bahrami, M. Sazan, and B. Gosselin, "A smart cage with uniform wireless power distribution in 3D for enabling long-term experiments with freely moving animals," *IEEE Trans. Biomed. Circuits Syst.*, vol. 10, no. 2, pp. 424–434, Apr. 2016.
- [11] D. Budgett *et al.*, "Novel technology for the provision of power to implantable physiological devices," *J. Appl. Phys.*, vol. 102, no. 4, pp. 1658–1663, 2007.
- [12] A. Bagheri *et al.*, "Massively-parallel neuromonitoring and neurostimulation rodent headset with nanotextured flexible microelectrodes," *IEEE Trans. Biomed. Circuits Syst.*, vol. 7, no. 5, pp. 601–609, Oct. 2013.
- [13] A. M. Sodagar, G. E. Perlin, Y. Yao, K. Najafi, and K. D. Wise, "An implantable 64-channel wireless microsystem for single-unit neural recording," *IEEE J. Solid-State Circuits*, vol. 44, no. 9, pp. 2591–2604, Sep. 2009.
- [14] T. A. Szuts *et al.*, "A wireless multi-channel neural amplifier for freely moving animals," *Nature Neurosci.*, vol. 14, no. 2, pp. 263–269, Feb. 2011.
- [15] A. Schwartz, X. Cui, D. Weber, and D. Moran, "Brain-controlled interfaces: Movement restoration with neural prosthetics," *Neuron*, vol. 52, no. 1, pp. 205–220, Oct. 2006.
- [16] P. Cong, N. Chaimanonart, W. H. Ko, and D. J. Young, "A wireless and batteryless 10-bit implantable blood pressure sensing microsystem with adaptive RF powering for real-time laboratory mice monitoring," *IEEE J. Solid-State Circuits*, vol. 44, no. 12, pp. 3631–3644, Dec. 2009.
- [17] U. Jow, P. McMenamin, M. Kiani, J. R. Manns, and M. Ghovanloo, "EnerCage: A smart experimental arena with scalable architecture for behavioral experiments," *IEEE Trans. Biomed. Eng.*, vol. 61, no. 1, pp. 139–148, Jan. 2014.
- [18] B. Lee, M. Kiani, and M. Ghovanloo, "A smart wirelessly-powered homecage for long-term high-throughput behavioral experiments," *IEEE Sens. J.*, vol. 15, no. 9, pp. 4905–4916, Sep. 2015.
- [19] S. Mirbozorgi, H. Bahrami, M. Sazan, and B. Gosselin, "A smart multicoil inductively coupled array for wireless power transmission," *IEEE Trans. Ind. Electron.*, vol. 61, no. 11, pp. 6061–6070, Nov. 2014.

- [20] E. Kilinc, G. Conus, C. Weber, B. Kawkabani, F. Maloberti, and C. Dehollain, "A system for wireless power transfer of micro-systems in-vivo implantable in freely moving animals," *IEEE Sens. J.*, vol. 14, no. 2, pp. 522–531, Feb. 2014.
- [21] K. Eom *et al.*, "A wireless power transmission system for implantable devices in freely moving rodents," *Med. Biol. Eng. Comput.*, vol. 52, no. 8, pp. 639–651, Aug. 2014.
- [22] S. A. Mirbozorgi, Y. Jia, D. Canales, and M. Ghovanloo, "A wirelessly-powered homecage with segmented copper foils and closed-loop power control," *IEEE Trans. Biomed. Circuits Syst.*, vol. 10, no. 5, pp. 979–989, Oct. 2016.
- [23] Y. Jia *et al.*, "Position and orientation insensitive wireless power transmission for energe-homecage system," *IEEE Trans. Biomed. Eng.*, vol. 64, no. 10, pp. 2439–2449, Oct. 2017.
- [24] S. C. Tang and N. J. McDannold, "Power loss analysis and comparison of segmented and unsegmented energy coupling coils for wireless energy transfer," *IEEE J. Emerg. Sel. Topics Power Electron.*, vol. 3, no. 1, pp. 215–225, Mar. 2015.
- [25] Animal Research Review Panel (ARRP) Guideline 20: Guideline for the Housing of Rats in Scientific Institutions, 2007.
- [26] S. C. Tang, "A low-operating-voltage wireless intermediate-range scheme for energy and signal transmission by magnetic coupling for implantable devices," *IEEE J. Emerg. Sel. Topics Power Electron.*, vol. 3, no. 1, pp. 242–251, Mar. 2015.
- [27] *Standard for Safety Levels With Respect to Human Exposure to Radio Frequency Electromagnetic Fields, 3 kHz to 300 GHz*, IEEE Std C95.1-2005 (Revision of IEEE Std C95.1-1991), 2006.
- [28] J. Gordon, "Effects of ambient temperature and exposure to 2450-MHz microwave radiation on evaporative heat loss in the mouse," *J. Microw. Power*, vol. 17, pp. 145–150, 1982.
- [29] J. Gordon, "Note: Further evidence of an inverse relation between mammalian body mass and sensitivity to radio-frequency electromagnetic radiation," *J. Microw. Power*, vol. 18, pp. 377–383, 1983.
- [30] A. Guy, P. Kramar, C. Harris, and C. Chou, "Long-term 2450-MHz CW microwave irradiation of rabbits: Methodology and evaluation of ocular and physiologic effects," *J. Microw. Power*, vol. 15, pp. 37–44, 1980.
- [31] J. Chow, H. Chung, and C. S. Cheng, "Use of transmitter-side electrical information to estimate mutual inductance and regulate receiver-side power in wireless inductive link," *IEEE Trans. Power Electron.*, vol. 31, no. 9, pp. 6079–6091, Feb. 2016.
- [32] I. J. Makowska and D. M. Weary, "The importance of burrowing, climbing and standing upright for laboratory rats," *Royal Soc. Open Sci.*, vol. 3, no. 6, pp. 1–12, Jun. 2016.
- [33] *MS Lithium Rechargeable Battery*, Seiko Instruments, Inc. [Online]. Available: <http://www.sii.co.jp/en/me/battery/products/ms-lithium-2/>
- [34] J. Chow, N. Chen, H. Chung, and L. Chan, "An investigation into the use of orthogonal winding in loosely-coupled link for improving power transfer efficiency under coil misalignment," *IEEE Trans. Power Electron.*, vol. 30, no. 10, pp. 5632–5649, Nov. 2014.
- [35] B. H. Choi, E. S. Lee, Y. H. Sohn, G. C. Jang, and C. T. Rim, "Six degrees of freedom mobile inductive power transfer by crossed dipole Tx and Rx coils," *IEEE Trans. Power Electron.*, vol. 31, no. 4, pp. 3252–3272, Apr. 2016.
- [36] J. Chow, H. Chung, L. Chan, N. McDannold, and S. C. Tang, "Design of a wireless power transfer system for devices carried by a freely moving animal in cage," in *Proc. IEEE Energy Convers. Congr. Expo.*, Oct. 2017, pp. 4398–4405.
- [37] H. S. Choim, "Half-bridge LLC resonant converter design using FSFA-series Fairchild power switch," Fairchild Semiconductor, San Jose, CA, USA, Appl. Note AN-151, 2007.
- [38] *Types MC multilayer RF capacitors*, Cornell Dubilier Electronics, Datasheet, 2008. [Online]. Available: <http://www.cde.com/resources/catalogs/MC.pdf>
- [39] X. Li *et al.*, "A wireless magnetic resonance energy transfer system for micro implantable medical sensors," *Sensors*, vol. 12, no. 8, pp. 10292–10308, Jul. 2012.
- [40] E. B. Rosa and F. W. Grover, "Formulas and tables for the calculation of mutual and self inductance," *Bull. Bur. Standards*, vol. 8, pp. 1–237, Jan. 1912.
- [41] J. Acero, C. Carretero, R. Alonso, and J. M. Burdío, "Quantitative evaluation of induction efficiency in domestic induction heating applications," *IEEE Trans. Magn.*, vol. 49, no. 4, pp. 1382–1389, Apr. 2013.
- [42] J. Simpson, J. Lane, and R. Youngquist, "Simple analytic expressions for the magnetic field of a circular current loop," NASA Technical Documents, 2001.
- [43] *COMSOL Multiphysics*, 2019. [Online]. Available: <http://www.comsol.com>
- [44] *Lab Products, Inc., Rat Cage*, 2019. [Online]. Available: <http://labproductsinc.com/products/conventional-cages/>
- [45] *American Fancy Rat & Mouse Association, Rat Lab Cage*, 2015. [Online]. Available: <http://www.afrma.org/house4mousep2.htm>
- [46] M. Misakian, "Equations for the magnetic field produced by one or more rectangular loops of wire in the same plane," *J. Res. Nat. Inst. Stand. Technol.*, vol. 105, no. 4, pp. 557–564, Aug. 2000.
- [47] C. Gabriel, "Compilation of the dielectric properties of body tissues at RF and microwave frequencies," Radiofrequency Radiation Division, Brooks AFB, San Antonio, TX, USA, Contract AL/OE-TR-1996-0037, 1996.
- [48] C. Gabriel, S. Gabriel, and E. Corthout, "The dielectric properties of biological tissues: II. Measurements in the frequency range of 10 Hz to 20 GHz," *Phys. Med. Biol.*, vol. 41, pp. 2251–2269, 1996.
- [49] J. N. Crawley, *What's Wrong With My Mouse?: Behavioral Phenotyping of Transgenic and Knockout Mice*, 2nd ed. Hoboken, NJ, USA: Wiley, 2007.
- [50] A. F. Meyer, J. Poort, J. O'Keefe, M. Sahani, and J. F. Linden, "An ultralight head-mounted camera system integrates detailed behavioral monitoring with multichannel electrophysiology in freely moving mice," *bioRxiv*, Apr. 2018.
- [51] J. Chow, H. Chung, C. S. Cheng, and W. Wang, "Use of transmitter-side electrical information to estimate system parameters of wireless inductive links," *IEEE Trans. Power Electron.*, vol. 32, no. 9, pp. 7169–7186, Sep. 2017.
- [52] K. Silay, C. Dehollain, and M. Declercq, "Inductive power link for a wireless cortical implant with biocompatible packaging," in *Proc. IEEE Sensors*, 2010, pp. 94–98.



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