

# Output-Series Connected Dual Active Bridge Converters for Zero-Voltage Switching Throughout Full Load Range by Employing Auxiliary LC Networks

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**Abstract**—This paper presents an output-series connected dual active bridge (DAB) converter for efficient zero-voltage switching (ZVS) by employing dual auxiliary LC networks in high-output voltage applications. The dual auxiliary LC networks are integrated into the converter for ZVS throughout full load range. The gate signals of the output side switches can control the current in the LC networks. By analyzing the working modes of the converter, the modulation trajectory is designed in terms of the boundaries of the ZVS range. The conduction loss caused by the auxiliary LC networks is adjusted according to the voltage and load power. The modulation scheme can achieve seamless transition between the adjacent working modes. The conduction loss of the proposed converter is compared with the conventional output-series DAB converter. Although the conduction loss is increased under light loads, all the switches can achieve ZVS. The reduced switching loss can improve the overall efficiency. Finally, a 1.3 kW experimental prototype was built to verify the effectiveness of the proposed converter and the modulation scheme, which demonstrates the ZVS performance and efficiency improvement.

**Index Terms**—Auxiliary LC networks, dual active bridge (DAB), output-series, zero-voltage switching (ZVS).

## I. INTRODUCTION

THE dual active bridge (DAB) converter was proposed in energy storage system for high efficiency and high power density applications [1]. By using the single phase shift (SPS) between two full bridges, the bidirectional power can be achieved. Because of the galvanic isolation and high voltage gain adjusted by turns ratio of the transformer, DAB converter has become a popular solution to energy storage system [2], [3]. However, only using single phase shifted control cannot achieve high efficiency over wide battery voltage range. When

Manuscript received April 17, 2018; revised July 11, 2018 and August 31, 2018; accepted September 3, 2018. Date of publication September 12, 2018; date of current version April 20, 2019. This work was supported by the National Natural Science Foundation of China under Grants 51807007 and 51577012. Recommended for publication by Associate Editor B. P. McGrath. (*Corresponding author: Zhiqiang Guo.*)

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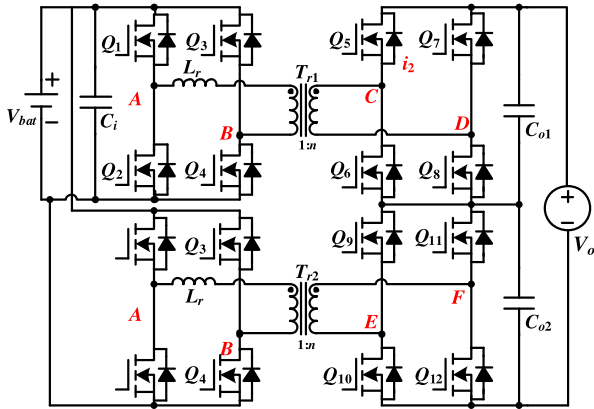


Fig. 1. Input-parallel output-series dual active bridge converter.

working modes on ZVS and RMS current optimization can be used for high efficiency [16]. However, the converter still cannot achieve ZVS under some circumstances. The TZM modulation with an inductor in parallel with the transformer can keep all the switches working in ZVS [17]. In ETH, DAB converters with full-load-range ZVS can be achieved by using commutation inductors in parallel with the active full bridges [18]. By using auxiliary commutation inductors with variable frequency and variable phase shift, DAB converter is extended to bidirectional ac–dc converters for full-operation-range ZVS [19], [20]. However, the commutation inductors have circulating current in all operation modes. Accordingly, the conduction loss is increased in all the operation modes. The T-type bridge leg used in DAB converter can achieve low RMS current [21], [22]. However, ZVS achievement for all switches becomes complex since there are more switches. In [23], a two-working-mode modulation scheme for the DAB converter with a dc blocking capacitor is proposed for wide voltage conversion range. However, there must be a gradual transition between the two working modes, which may affect the dynamic performance.

In order to meet high dc-link voltage requirement, the three-level or series-connected topologies permit low voltage rating switches to be used in this situation. A three-level DAB converter in different working modes is used in 1 kV dc bus voltage [24]. However, the converter still works in two-level modulation. Clamping diodes and flying capacitors have to be used to decouple the voltage stress of the outer and inner switches. Although the conduction loss is optimized in different operation modes, the switches still work in hard switching. A neutral-point clamped DAB converter is developed to improve the efficiency and balance the capacitor voltages [25]. However, the complicated modulation still cannot guarantee wide ZVS. In [26], a high-voltage DAB converter with series-connected half bridges is used in the high-voltage side. Likewise, Fig. 1 shows the input-parallel output-series DAB converter suitable for high output dc-link voltage [27]. By sharing the switches in battery side, the output-series dual active bridge (OSDAB) converter can be derived in Fig. 2. Compared with the three-level DAB converter, output-series DAB converter is more flexible in high-voltage applications. However, the converter still cannot achieve ZVS over wide battery voltage range and full load range.

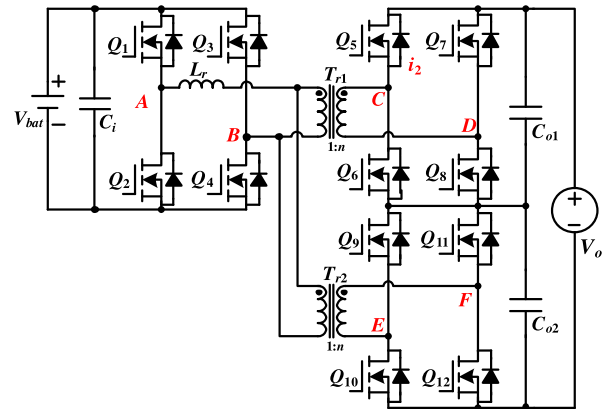


Fig. 2. Output-series dual active bridge converter.

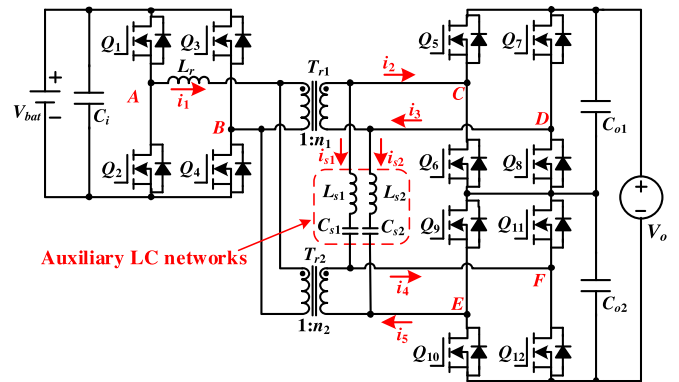


Fig. 3. Output-series dual active bridge converter with dual auxiliary LC network.

In this paper, an output-series DAB converter with dual auxiliary LC networks (OSDAB plus dual LC) is proposed in order to achieve ZVS throughout full load range. The dual LC networks are connected across the midpoints of the output full bridges. The phase shift of the output full bridge can control the current in the auxiliary LC networks. The current in the auxiliary LC networks can guarantee all the switches work in ZVS. In order to reduce the conduction loss caused by the LC networks, the modulation trajectory is designed according to the boundaries of the ZVS range. The currents in auxiliary LC networks can guarantee that all the switches work in the soft switching. When the converter can achieve ZVS without LC networks, the currents in the auxiliary LC networks are regulated to zero. The conduction loss caused by the auxiliary LC networks for different battery voltages and load power can be optimized.

This paper is organized as follows. An output-series DAB converter with dual auxiliary LC networks and its operation modes are described in Section II. The key feature and ZVS operating range of the proposed converter are analyzed in Section III. In terms of the ZVS boundaries, the modulation trajectory is investigated and the converter can achieve seamless transition between adjacent working modes. The experimental prototype is built to verify the performance of the proposed converter in Section IV. Finally, Section V provides the conclusion.

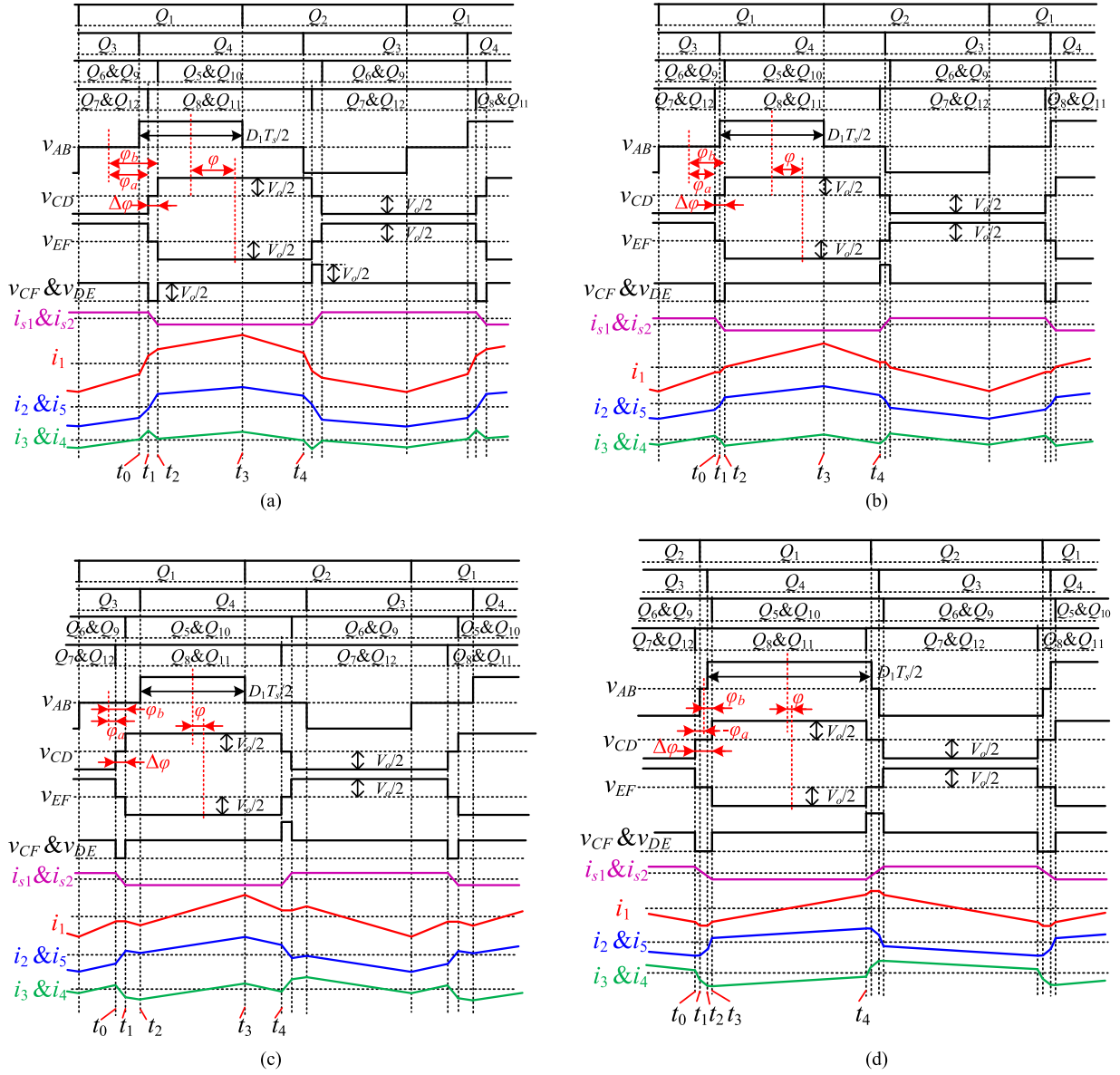


Fig. 4. Working modes in forward power flow. (a) Mode 1a. (b) Mode 2a. (c) Mode 3. (d) Mode 4.

## II. WORKING MODES OF THE PROPOSED CONVERTER

Fig. 3 shows the topology of the output-series DAB converter with dual auxiliary  $LC$  networks.  $V_{\text{bat}}$  is the battery voltage. On the battery side, the power stage is a full bridge. On the output side, the power stage is composed of two full bridges, whose output voltage is connected in series to form the output voltage.  $C_{o1}$  and  $C_{o2}$  are the output capacitors. The output voltage is  $V_o$ . There are two transformers. Their turns ratio are  $1:n_1$  and  $1:n_2$ , respectively, where  $n_1$  and  $n_2$  are equal to  $n$ .  $L_r$  is the series inductance. The three full bridges are linked with series inductor and two transformers. In the two transformers, the two windings in the battery side are parallel. The power transmitted from the battery to the output is defined as the forward power flow, conversely, is defined as the reverse power flow.  $L_{s1}$ ,  $L_{s2}$ ,  $C_{s1}$ , and  $C_{s2}$  constitute two auxiliary  $LC$  networks used to achieve wide ZVS. Taking the forward power flow into consideration, the

converter can work in four modes, which are shown in Fig. 4. The gate signals for  $Q_1 - Q_{12}$  are 50% duty cycle. As seen in Fig. 4, some switches are driven by the same gate signals.  $v_{AB}$  is the output voltage of the battery side full bridge.  $D_1$  is its effective duty cycle.  $T_s$  is the switching period.  $v_{CD}$  and  $v_{EF}$  are controlled by the phase shift of the two output-side full bridges, and their waveforms are symmetric in the horizontal coordinates.  $\varphi$  is the phase shift between  $v_{AB}$  and  $v_{CD}$ .  $\Delta\varphi$  is the phase shift between  $Q_8$  and  $Q_5$ .  $\varphi_a$  is equal to  $\varphi - \frac{\Delta\varphi}{2}$ , and  $\varphi_b$  is equal to  $\varphi + \frac{\Delta\varphi}{2}$ .  $\varphi_a$  and  $\varphi_b$  are illustrated in Fig. 4. Due to the symmetry of the forward and reverse power flow, there are also four working modes in reverse power flow. In terms of the range of  $\varphi_a$  and  $\varphi_b$ , the boundary conditions of the working modes are shown in Table I. Mode 1a and Mode 1b are the symmetrical working modes, and Mode 2a and Mode 2b are the symmetrical working modes. Mode 3 and Mode 4

TABLE I  
BOUNDARY CONDITION FOR EACH MODE

Forward Power Flow		Reverse Power Flow	
Working Mode	Boundary condition	Working Mode	Boundary condition
Mode 1a	$\frac{1}{2} - \frac{D_1}{2} \leq \frac{\phi_a}{\pi} \leq \frac{\phi_b}{\pi} \leq \frac{1}{2}$	Mode 1b	$-\frac{1}{2} \leq \frac{\phi_a}{\pi} \leq \frac{\phi_b}{\pi}$ $\leq -\left(\frac{1}{2} - \frac{D_1}{2}\right)$
Mode 2a	$-\left(\frac{1}{2} - \frac{D_1}{2}\right) \leq \frac{\phi_a}{\pi}$ $\leq \left(\frac{1}{2} - \frac{D_1}{2}\right) \leq \frac{\phi_b}{\pi} \leq \frac{1}{2}$	Mode 2b	$-\frac{1}{2} \leq \frac{\phi_a}{\pi} \leq -\left(\frac{1}{2} - \frac{D_1}{2}\right)$ $\leq \frac{\phi_b}{\pi} \leq \left(\frac{1}{2} - \frac{D_1}{2}\right)$
Mode 3	$-\left(\frac{1}{2} - \frac{D_1}{2}\right) \leq \frac{\phi_a}{\pi} \leq \frac{\phi_b}{\pi} \leq \left(\frac{1}{2} - \frac{D_1}{2}\right)$		
Mode 4	$\frac{\phi_a}{\pi} \leq -\left(\frac{1}{2} - \frac{D_1}{2}\right) \leq 0 \leq \left(\frac{1}{2} - \frac{D_1}{2}\right) \leq \frac{\phi_b}{\pi}$		

are the common working modes in both forward and reverse power flow. Only forward power flow will be analyzed in this paper. The same conclusion can be drawn for the reverse power flow by using the same method. As seen,  $v_{CF}$  and  $v_{DE}$  are voltages across the two LC networks, which are larger than zero. The capacitances of  $C_{s1}$  and  $C_{s2}$  are large enough to filter out the dc voltage offset, which guarantees that the average currents in  $L_{s1}$  and  $L_{s2}$  are equal to zero. The voltages across  $C_{s1}$  and  $C_{s2}$  are  $V_o/2$ . The phase shift angle  $\Delta\varphi$  can control the current in the auxiliary LC networks.  $\Delta\varphi$  is the small value. Otherwise, there is large current in the LC networks, which degrades the efficiency. Therefore,  $D_1$  can only be regulated in a wide range to meet the voltage-second balance across the both side of the transformers. In this case, the converter can be modulated by EPS. In order to meet voltage-second balance across the both side of the transformer, the converter should meet  $nV_{bat}D_1 = \frac{V_o}{2}(1 - \frac{\Delta\varphi}{\pi}) \approx \frac{V_o}{2}$ . Therefore, the effective voltage gain meets the condition:  $M = V_o/nV_{bat} = 2D_1 \leq 2$ . The turns ratio of the transformer should be designed in consideration with the minimum battery voltage. The turns ratio of the transformer can be designed as  $n = V_o/2V_{bat\_min}$ , where  $V_{bat\_min}$  is the minimum battery voltage. Assuming  $L_{s1} = L_{s2} = L_s$ ,  $C_{s1} = C_{s2} = C_s$ , and  $i_{s1} = i_{s2} = i_s$ , and defining  $X_r = 2\pi L_r/T_s$  and  $X_s = 2\pi L_s/T_s$ , the currents in converter meet the following conditions:

$$\begin{cases} i_2 = i_5 = \frac{i_1}{2n} - i_s \\ i_3 = i_4 = \frac{i_1}{2n} + i_s \end{cases} \quad (1)$$

Ignoring the dead time of the gate signals, there are four working stages for each working mode in half of the switching period. To explain, the working stages in Mode 1a are shown in Fig. 5.

**Stage 1** ( $[t_0, t_1]$ ) [see Fig. 5(a)]: Prior to  $t_0$ ,  $Q_1, Q_3, Q_6, Q_7, Q_9$ , and  $Q_{12}$  are ON, and  $Q_2, Q_4, Q_5, Q_8, Q_{10}$ , and  $Q_{11}$  are OFF. At  $t_0$ ,  $Q_3$  is switched OFF and  $i_1$  is negative. The junction capacitor of  $Q_4$  is discharged, and  $Q_4$  is turned ON with ZVS.  $i_1$  is increased, and  $i_{s1}$  and  $i_{s2}$  are positive. The

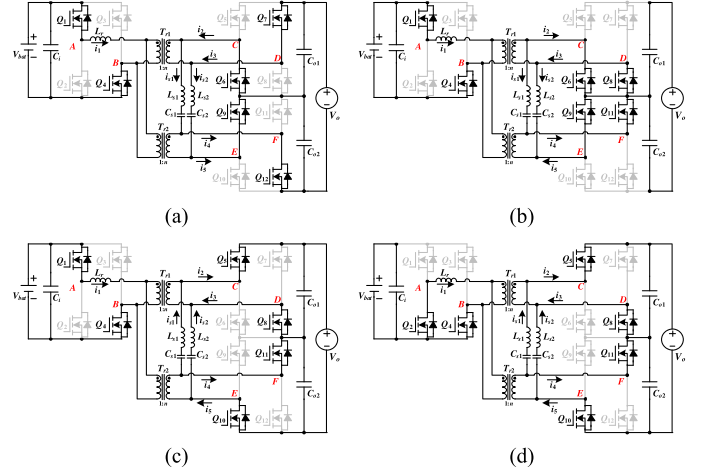


Fig. 5. Topological stages with half switching period in Mode 1a. (a)  $[t_0, t_1]$ . (b)  $[t_1, t_2]$ . (c)  $[t_2, t_3]$ . (d)  $[t_3, t_4]$ .

currents in this stage are expressed as follows:

$$\begin{cases} i_1(t) = i_1(t_0) + \frac{V_{bat} + V_o/(2n)}{L_r}(t - t_0) \\ i_s(t) = i_s(t_0). \end{cases} \quad (2)$$

**Stage 2** ( $[t_1, t_2]$ ) [see Fig. 5(b)]: At  $t_1$ ,  $Q_7$  and  $Q_{12}$  are turned OFF. Because  $i_3$  and  $i_4$  are positive at this time, the junction capacitors of  $Q_8$  and  $Q_{11}$  start to be discharged. Until the voltage across  $Q_8$  and  $Q_{11}$  reaches zero,  $Q_8$  and  $Q_{11}$  are turned ON with ZVS.  $i_1$  is still increased, while  $i_{s1}$  and  $i_{s2}$  start to decrease. The currents in this stage are expressed as follows:

$$\begin{cases} i_1(t) = i_1(t_1) + \frac{V_{bat}}{L_r}(t - t_1) \\ i_s(t) = i_s(t_1) - \frac{V_o}{2L_s}(t - t_1). \end{cases} \quad (3)$$

**Stage 3** ( $[t_2, t_3]$ ) [see Fig. 5(c)]: At  $t_2$ ,  $Q_6$  and  $Q_9$  are turned OFF.  $i_2$  and  $i_5$  are positive and large enough, so the junction capacitors of  $Q_5$  and  $Q_{10}$  are discharged. Until the voltage across  $Q_5$  and  $Q_{10}$  reaches zero,  $Q_5$  and  $Q_{10}$  are turned ON with ZVS. In this stage, the energy starts to transmit from the battery side to the output side. The currents in this stage are expressed as follows:

$$\begin{cases} i_1(t) = i_1(t_1) + \frac{V_{bat} - V_o/(2n)}{L_r}(t - t_2) \\ i_s(t) = i_s(t_2). \end{cases} \quad (4)$$

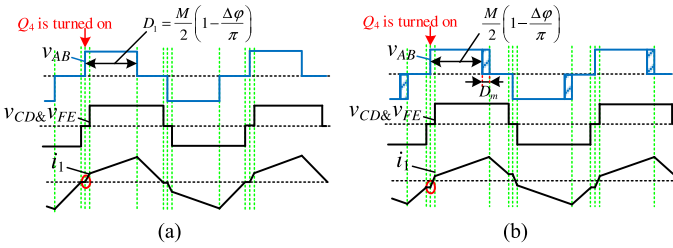
**Stage 4** ( $[t_3, t_4]$ ) [see Fig. 5(d)]: At  $t_4$ ,  $Q_1$  is turned OFF. The current in the primary side of the transformer will charge and discharge the junction capacitors of  $Q_1$  and  $Q_2$ . When the voltage across  $Q_1$  reaches zero and the voltage across  $Q_2$  reaches  $V_{bat}$ ,  $Q_2$  is turned ON with ZVS. The currents in this stage are expressed as follows:

$$\begin{cases} i_1(t) = i_1(t_1) - \frac{V_o/(2n)}{L_r}(t - t_3) \\ i_s(t) = i_s(t_3). \end{cases} \quad (5)$$

According to (1)–(5), currents  $i_1, i_2, i_3, i_4, i_5$  at the time of  $t_0, t_1, t_2$ , and  $t_3$  can be derived. The working stages in Mode 2a, Mode 3, and Mode 4 can be analyzed in the same method. The key feature of the working modes will be analyzed in accordance with these currents.

TABLE II  
 ZVS CONDITIONS FOR  $Q_1$  AND  $Q_4$ 

	Mode 1a	Mode 2a
ZVS for $Q_1$	$-i_1(t_3) = -I_{base} \left[ \frac{1}{8} \left( \frac{\varphi_a}{\pi} + \frac{\varphi_b}{\pi} - D_1 \right) + \frac{D_1}{4M} \right] \leq -I_{ZVS1}$	$-i_1(t_3) = -I_{base} \left[ \frac{D_1}{4M} + \frac{1}{8} \left( D_1 - \frac{\varphi_a}{\pi} - \frac{\varphi_b}{\pi} \right) \right] \leq -I_{ZVS1}$
ZVS for $Q_4$	$i_1(t_0) = I_{base} \left[ \frac{1}{8} \left( 2 - \frac{\varphi_a}{\pi} - \frac{\varphi_b}{\pi} - D_1 \right) - \frac{D_1}{4M} \right] \leq -I_{ZVS1}$	$i_1(t_1) = I_{base} \left[ \frac{1}{8} \left( 1 + \frac{\varphi_a}{\pi} - \frac{\varphi_b}{\pi} \right) - \frac{D_1}{4M} \right] \leq -I_{ZVS1}$
	Mode 3	Mode 4
ZVS for $Q_1$	$-i_1(t_3) = -I_{base} \left[ \frac{D_1}{4M} - \frac{1}{8} \left( D_1 - \frac{\varphi_a}{\pi} - \frac{\varphi_b}{\pi} \right) \right] \leq -I_{ZVS1}$	$i_1(t_1) = I_{base} \left[ \frac{1}{8} \left( 1 + \frac{\varphi_a}{\pi} - \frac{\varphi_b}{\pi} \right) - \frac{D_1}{4M} \right] \leq -I_{ZVS1}$
ZVS for $Q_4$	$i_1(t_2) = I_{base} \left[ \frac{1}{8} \left( D_1 + \frac{\varphi_b}{\pi} + \frac{\varphi_a}{\pi} \right) - \frac{D_1}{4M} \right] \leq -I_{ZVS1}$	$i_1(t_2) = I_{base} \left[ \frac{1}{8} \left( 1 + \frac{\varphi_a}{\pi} - \frac{\varphi_b}{\pi} \right) - \frac{D_1}{4M} \right] \leq -I_{ZVS1}$


 Fig. 6. Key waveforms of Mode 2a with specific duty cycle. (a)  $D_1 = \frac{M}{2} \left( 1 - \frac{\Delta\varphi}{\pi} \right)$ . (b)  $D_1 = \frac{M}{2} \left( 1 - \frac{\Delta\varphi}{\pi} \right) + D_m$ .

### III. KEY FEATURE AND MODULATION SCHEME OF THE CONVERTER

#### A. ZVS Analyses for $Q_1 - Q_4$

Because of the symmetry in two halves of the switching period, the ZVS conditions for  $Q_1$  and  $Q_2$  are the same, and the ZVS conditions for  $Q_3$  and  $Q_4$  are the same. Therefore, ZVS performance of  $Q_1$  and  $Q_4$  will be analyzed, and  $Q_3$  and  $Q_2$  work in the same condition. In order to achieve ZVS for  $Q_1$  and  $Q_4$ ,  $i_1$  should be negative and large enough, i.e.,  $i_1 \leq -I_{ZVS1}$ , where  $I_{ZVS1}$  is the minimum current to charge or discharge the junction capacitors during the dead time for ZVS of  $Q_1 - Q_4$ .  $I_{ZVS1}$  is associated with  $C_{oss}$  (output capacitance) of the switches. The proximate evaluation of  $I_{ZVS1}$  can be expressed as  $V_{bat} C_{oss(Q1-Q4)} / t_{dead}$ , where  $t_{dead}$  is the dead time of the switches.

According to  $i_1$  at the commutation time, the ZVS boundaries of  $Q_1$  and  $Q_4$  in different working modes are shown in Table II.  $I_{base}$  is defined as the normalized current, where  $I_{base} = \frac{V_o T_s}{n L_r}$ . Taking Mode 2a for example, if  $D_1$  is equal to  $\frac{V_o}{2nV_{bat}} \left( 1 - \frac{\Delta\varphi}{\pi} \right) = \frac{M}{2} \left( 1 - \frac{\Delta\varphi}{\pi} \right)$ , the key waveform of  $i_1$  is shown in Fig. 6(a). When  $Q_4$  is turned ON,  $i_1$  is equal to zero. Therefore,  $Q_4$  works in hard switching. If  $D_1$  is set to be larger than  $\frac{M}{2} \left( 1 - \frac{\Delta\varphi}{\pi} \right)$ , i.e.,  $D_1 = \frac{M}{2} \left( 1 - \frac{\Delta\varphi}{\pi} \right) + D_m$ , the key waveform of  $i_1$  is shown in Fig. 6(b). When  $Q_4$  is turned ON,  $i_1$  is less than zero. Therefore,  $Q_4$  has the potential to achieve ZVS. Substituting  $D_1 = \frac{M}{2} \left( 1 - \frac{\Delta\varphi}{\pi} \right) + D_m$  into Table II, the ZVS

conditions for  $Q_1$  and  $Q_4$  are shown in Table III. The ZVS conditions for  $Q_1$  and  $Q_4$  in different modes can be synthesized to the same. As long as  $\frac{I_{base} D_m}{4M} \geq I_{ZVS1}$ , i.e.,  $D_m \geq \frac{4L_r I_{ZVS1}}{V_{bat} T_s}$ ,  $Q_1$  and  $Q_4$  can guarantee ZVS in all the working modes.  $D_m$  is designed as  $\frac{4L_r I_{ZVS1}}{V_{bat} T_s}$  in the following analyses and converter design.

#### B. ZVS Analyses for $Q_5 - Q_{12}$

Because of the symmetry in two halves of the switching period, the ZVS conditions for  $Q_5, Q_6, Q_9,$  and  $Q_{10}$  are the same, and the ZVS conditions for  $Q_7, Q_8, Q_{11},$  and  $Q_{12}$  are the same. Therefore, the ZVS conditions for  $Q_5$  &  $Q_{10}$  and  $Q_8$  &  $Q_{11}$  will be analyzed in half of the switching period. The commutations during the dead time for  $Q_5$  &  $Q_{10}$  and  $Q_8$  &  $Q_{11}$  are shown in Fig. 7. To achieve ZVS of  $Q_5$  &  $Q_{10}$  and  $Q_8$  &  $Q_{11}$ ,  $i_2, i_5, i_3,$  and  $i_4$  should be positive and large enough, i.e.,  $i_2 = i_5 \geq I_{ZVS2}$  and  $i_3 = i_4 \geq I_{ZVS2}$ , where  $I_{ZVS2}$  is the minimum current to charge and discharge the junction capacitor for ZVS of  $Q_5 - Q_{12}$  during the dead time. The proximate evaluation of  $I_{ZVS2}$  can be expressed as  $V_o C_{oss(Q5-Q12)} / 2t_{dead}$ . The ZVS constraints on  $Q_5$  &  $Q_{10}$  and  $Q_8$  &  $Q_{11}$  are shown in Table IV.

To achieve ZVS of  $Q_5$  &  $Q_{10}$  and  $Q_8$  &  $Q_{11}$  in all the working modes, the following conditions should be satisfied.

- 1) As seen in Table IV of Mode 1a, the ZVS boundary of  $Q_5$  &  $Q_{10}$  is rewritten as follows:

$$\Delta\varphi \geq \frac{1}{\frac{M}{4X_s} - \frac{M-2}{8n^2 X_r}} \left[ \frac{I_{ZVS2}}{nV_{bat}} - \frac{(M-2)\pi}{8n^2 X_r} - \frac{\varphi}{2n^2 X_r} \right] = \Delta\varphi_d. \quad (6)$$

- 2) In Mode 1a, the ZVS boundary of  $Q_8$  &  $Q_{11}$  is rearranged as follows:

$$\Delta\varphi \geq \frac{1}{\frac{M}{4X_s} - \frac{M+2}{8n^2 X_r}} \left[ \frac{I_{ZVS2}}{nV_{bat}} - \frac{(M-2)\pi}{8n^2 X_r} - \frac{\varphi}{2n^2 X_r} \right] = \Delta\varphi_e. \quad (7)$$

TABLE III  
DERIVED ZVS CONDITIONS FOR  $Q_1$  AND  $Q_4$

	Mode 1a	Mode 2a
ZVS for $Q_1$	$-i_1(t_3) = -I_{base} \left[ \frac{1}{8} \left( \frac{2\varphi_a}{\pi} + 1 - D_1 \right) + \frac{D_m}{4M} \right] \leq -\frac{I_{base} D_m}{4M} \leq -I_{ZVS1}$	$-i_1(t_3) = -I_{base} \left[ \frac{1}{8} \left( \frac{2\varphi_a}{\pi} + 1 - D_1 \right) + \frac{D_m}{4M} \right] \leq -\frac{I_{base} D_m}{4M} \leq -I_{ZVS1}$
ZVS for $Q_4$	$i_1(t_0) = I_{base} \left[ \frac{1}{8} \left( 1 - D_1 - \frac{2\varphi_a}{\pi} \right) - \frac{D_m}{4M} \right] \leq -\frac{I_{base} D_m}{4M} \leq -I_{ZVS1}$	$i_1(t_1) = -\frac{I_{base} D_m}{4M} \leq -I_{ZVS1}$
	Mode 3	Mode 4
ZVS for $Q_1$	$-i_1(t_3) = -I_{base} \left[ \frac{1}{8} \left( \frac{2\varphi_a}{\pi} + 1 - D_1 \right) - \frac{D_m}{4M} \right] \leq -\frac{I_{base} D_m}{4M} \leq -I_{ZVS1}$	$i_1(t_1) = -\frac{I_{base} D_m}{4M} \leq -I_{ZVS1}$
ZVS for $Q_4$	$i_1(t_2) = -I_{base} \left[ \frac{1}{8} \left( 1 - D_1 - \frac{2\varphi_b}{\pi} \right) + \frac{D_m}{4M} \right] \leq -\frac{I_{base} D_m}{4M} \leq -I_{ZVS1}$	$i_1(t_1) = -\frac{I_{base} D_m}{4M} \leq -I_{ZVS1}$

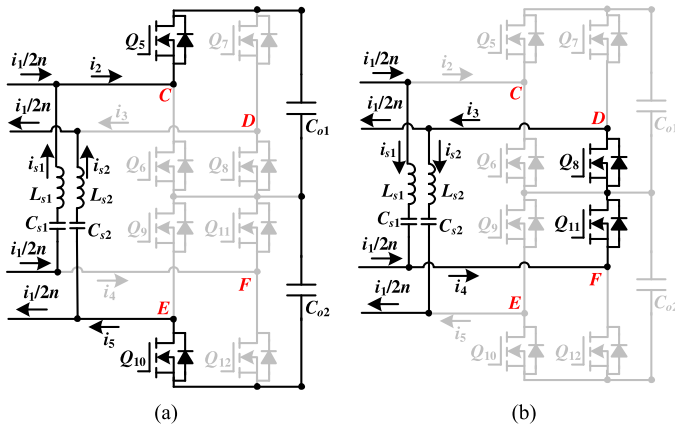


Fig. 7. Commutations during the dead time for  $Q_5$  &  $Q_{10}$  and  $Q_8$  &  $Q_{11}$ . (a)  $Q_5$  &  $Q_{10}$ . (b)  $Q_8$  &  $Q_{11}$ .

Comparing (6) with (7),  $\Delta\varphi_e$  is greater than  $\Delta\varphi_d$ . Therefore, as long as (7) is satisfied, (6) must be satisfied.

- As seen in Table IV, the ZVS boundary of  $Q_5$  &  $Q_{10}$  in Mode 2a is the same as that in Mode 1a, which is expressed as (6).
- The ZVS boundary of  $Q_8$  &  $Q_{11}$  in Mode 2a is rewritten as follows:

$$\Delta\varphi \geq \frac{4X_s}{V_o} \left( I_{ZVS2} + \frac{D_m \pi}{8n^2 X_r} \right). \quad (8)$$

It is independent of  $\varphi$ .

- The ZVS constraints on  $Q_5 - Q_{12}$  in Mode 3 are the same as  $Q_8$  &  $Q_{11}$  in Mode 2a, which is expressed as (8).
- The ZVS boundary of  $Q_5$  &  $Q_{10}$  in Mode 4 is the same as that in Mode 1a.
- The ZVS boundary of  $Q_8$  &  $Q_{11}$  in Mode 4 is rearranged as follows:

$$\Delta\varphi \geq \frac{1}{\frac{MT_s}{4X_s} - \frac{M-2}{8n^2 X_r}} \left[ \frac{I_{ZVS2}}{nV_{bat}} - \frac{(M-2)\pi}{8n^2 X_r} + \frac{\varphi}{2n^2 X_r} \right]. \quad (9)$$

As long as (9) is true, (6) must be satisfied.

Above all, the ZVS boundary of  $Q_5 - Q_{12}$  can be synthesized to (7) in Mode 1a, (6) and (8) in Mode 2a, (8) in Mode 3, and (9) in Mode 4.

### C. Modulation Trajectory

In terms of the analyses of the ZVS boundaries of  $Q_5 - Q_{12}$ , the ZVS range can be calculated with specific parameters. Fig. 8 shows the three-dimensional surface of the ZVS boundary versus  $V_{bat}$  and  $\varphi$ , where  $L_r = 24 \mu\text{H}$ ,  $T_s = 12.5 \mu\text{s}$ ,  $L_s = 22 \mu\text{H}$ ,  $n = 1.5$ ,  $I_{ZVS1} = 2 \text{ A}$ ,  $I_{ZVS2} = 2 \text{ A}$ , and  $V_o = 600 \text{ V}$ . The vertical axis is  $\Delta\varphi$ . The space above the surface is the ZVS area, and the space below the surface is hard switching area. Fig. 9 shows the ZVS range of  $Q_5 - Q_{12}$  with different battery voltages. Fig. 9 is the vertical section of Fig. 8. The shaded area in Fig. 9 is the ZVS range for  $Q_5 - Q_{12}$ . As seen, with the increase of the battery voltage, the converter becomes more difficult to achieve ZVS. By using the currents in the auxiliary LC networks, i.e.,  $\Delta\varphi$  is large enough, the converter can guarantee ZVS of  $Q_5 - Q_{12}$ . However, it will cause more conduction loss with large  $\Delta\varphi$ . In order to achieve ZVS with low conduction loss, the modulation trajectory should be designed according to the boundary conditions analyzed in Section III-C. The designed modulation trajectory is the red solid line shown in Fig. 9.

In (7), setting  $\Delta\varphi_e = 0$ ,  $\varphi$  is calculated as follows:

$$\varphi = \frac{2nI_{ZVS} X_r}{V_{bat}} - \frac{\pi}{4} (M - 2) = \varphi_n. \quad (10)$$

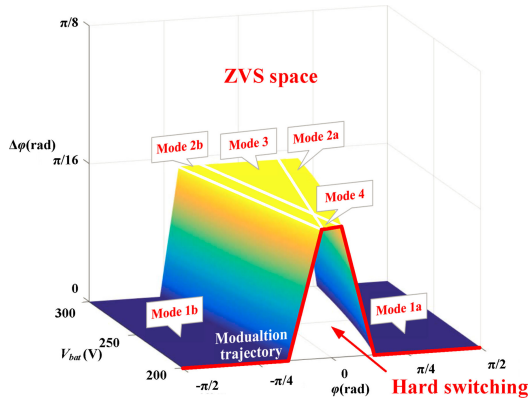
The coordinate of the point  $N$  in Fig. 9 is expressed as  $(\varphi_n, 0)$ , which varies with the battery and output voltages. The point  $M$  is on the boundary condition between Mode 1a and Mode 2a, which is expressed as follows:

$$\Delta\varphi = \frac{1}{1 + M/2} \left[ 2\varphi + \left( \frac{M}{2} + D_m - 1 \right) \pi \right]. \quad (11)$$

Then, in terms of (7) and (11), the coordinate of the point  $M$  in Fig. 9 is expressed as  $(\varphi_m, \Delta\varphi_m)$ , where eq.(12) shown at the bottom of the next page.

TABLE IV  
 ZVS CONDITIONS FOR  $Q_5$  &  $Q_{10}$  AND  $Q_8$  &  $Q_{11}$ 

	Mode 1a	Mode 2a
<b>ZVS for <math>Q_5</math>&amp;<math>Q_{10}</math></b>	$i_2(t_2) = i_5(t_2)$ $= I_{base} \left[ \left(1 - \frac{\Delta\varphi}{\pi}\right) \frac{1}{16n} + \left(\frac{2\varphi}{\pi} + \frac{\Delta\varphi}{\pi} - 1\right) \frac{1}{8nM} + \frac{nL_r \Delta\varphi}{8L_s \pi} \right]$ $= I_{base} \left[ \frac{1}{16n} \left(1 - \frac{2}{M}\right) + \frac{1}{4nM} \frac{\varphi}{\pi} + \left(\frac{nL_r}{8L_s} - \frac{1}{16n} + \frac{1}{8nM}\right) \frac{\Delta\varphi}{\pi} \right] \geq I_{ZVS2}$	$i_2(t_2) = i_5(t_2)$ $= I_{base} \left[ \left(1 - \frac{\Delta\varphi}{\pi}\right) \frac{1}{16n} - \left(1 - \frac{2\varphi}{\pi} - \frac{\Delta\varphi}{\pi}\right) \frac{1}{8nM} + \frac{nL_r \Delta\varphi}{8L_s \pi} \right]$ $= I_{base} \left[ \frac{1}{16n} \left(1 - \frac{2}{M}\right) + \frac{1}{4nM} \frac{\varphi}{\pi} + \left(\frac{nL_r}{8L_s} - \frac{1}{16n} + \frac{1}{8nM}\right) \frac{\Delta\varphi}{\pi} \right] \geq I_{ZVS2}$
<b>ZVS for <math>Q_8</math>&amp;<math>Q_{11}</math></b>	$i_3(t_1) = i_4(t_1)$ $= I_{base} \left[ \left(1 - \frac{\Delta\varphi}{\pi}\right) \frac{1}{16n} + \left(\frac{2\varphi}{\pi} - \frac{\Delta\varphi}{\pi} - 1\right) \frac{1}{8nM} + \frac{nL_r \Delta\varphi}{8L_s \pi} \right]$ $= I_{base} \left[ \frac{1}{16n} \left(1 - \frac{2}{M}\right) + \frac{1}{4nM} \frac{\varphi}{\pi} + \left(\frac{nL_r}{8L_s} - \frac{1}{16n} - \frac{1}{8nM}\right) \frac{\Delta\varphi}{\pi} \right] \geq I_{ZVS2}$	$i_3(t_0) = i_4(t_0) = I_{base} \left[ \left(1 - \frac{\Delta\varphi}{\pi}\right) \frac{1}{16n} - \frac{D_1}{8nM} + \frac{nL_r \Delta\varphi}{8L_s \pi} \right]$ $= I_{base} \left( -\frac{D_m}{8nM} + \frac{nL_r \Delta\varphi}{8L_s \pi} \right) \geq I_{ZVS2}$
	Mode 3	Mode 4
<b>ZVS for <math>Q_5</math>&amp;<math>Q_{10}</math></b>	$i_2(t_1) = i_5(t_1) = I_{base} \left[ \left(1 - \frac{\Delta\varphi}{\pi}\right) \frac{1}{16n} - \frac{D_1}{8nM} + \frac{nL_r \Delta\varphi}{8L_s \pi} \right]$ $= I_{base} \left( -\frac{D_m}{8nM} + \frac{nL_r \Delta\varphi}{8L_s \pi} \right) \geq I_{ZVS2}$	$i_2(t_3) = i_5(t_3)$ $= I_{base} \left[ \left(1 - \frac{\Delta\varphi}{\pi}\right) \frac{1}{16n} + \left(\frac{2\varphi}{\pi} + \frac{\Delta\varphi}{\pi} - 1\right) \frac{1}{8nM} + \frac{nL_r \Delta\varphi}{8L_s \pi} \right]$ $= I_{base} \left[ \frac{1}{16n} \left(1 - \frac{2}{M}\right) + \frac{1}{4nM} \frac{\varphi}{\pi} + \left(\frac{nL_r}{8L_s} - \frac{1}{16n} + \frac{1}{8nM}\right) \frac{\Delta\varphi}{\pi} \right] \geq I_{ZVS2}$
<b>ZVS for <math>Q_8</math>&amp;<math>Q_{11}</math></b>	$i_3(t_0) = i_4(t_0) = I_{base} \left[ \left(1 - \frac{\Delta\varphi}{\pi}\right) \frac{1}{16n} - \frac{D_1}{8nM} + \frac{nL_r \Delta\varphi}{8L_s \pi} \right]$ $= I_{base} \left( -\frac{D_m}{8nM} + \frac{nL_r \Delta\varphi}{8L_s \pi} \right) \geq I_{ZVS2}$	$i_3(t_0) = i_4(t_0)$ $= I_{base} \left[ \left(1 - \frac{\Delta\varphi}{\pi}\right) \frac{1}{16n} - \left(1 + \frac{2\varphi}{\pi} - \frac{\Delta\varphi}{\pi}\right) \frac{1}{8nM} + \frac{nL_r \Delta\varphi}{8L_s \pi} \right]$ $= I_{base} \left[ \left(1 - \frac{2}{M}\right) \frac{1}{16n} - \frac{1}{4nM} \frac{\varphi}{\pi} + \left(\frac{nL_r}{8L_s} - \frac{1}{16n} + \frac{1}{8nM}\right) \frac{\Delta\varphi}{\pi} \right] \geq I_{ZVS2}$


 Fig. 8. Three-dimensional (3-D) surface of the ZVS boundary versus  $V_{bat}$  and  $\varphi$ .

Point  $M$  also varies with the battery and output voltages. Therefore, the line  $MN$  in Fig. 9 is expressed as follows:

$$\Delta\varphi = \frac{\Delta\varphi_m}{\varphi_m - \varphi_n} (\varphi - \varphi_n). \quad (13)$$

The modulation trajectory can be illustrated as a flowchart shown in Fig. 10. The control diagram is shown in Fig. 11. As seen in Fig. 11, the output voltage is controlled by a proportional-integral (PI) controller. The output of the PI controller is the phase shift angle  $\varphi$ . As seen in the flowchart as shown in Fig. 10,  $\Delta\varphi$  is calculated in accordance with  $\varphi$ . Then, the gate signals of  $Q_1 - Q_{12}$  are generated in terms of  $D_1$ ,  $\varphi$ ,  $\Delta\varphi$ . As seen in (10) and (12) shown at the bottom of this page, the turning points of the modulation trajectory are associated with  $L_r$  and  $L_s$ . Due to the manufacture and nonlinearity of the inductor,  $L_r$  and  $L_s$  may not be equal to their nominal values, which may make the points  $M$  and  $N$  deviate away from their set points. However, point  $M$  is still located on the boundary condition between Mode 1a and Mode 2a, and point  $N$  is still located on the horizontal axis. As long as points  $M$  and  $N$  are located in the shadowed area of Fig. 9, the modulation scheme for ZVS is still effective and not very sensitive to the parameter of  $L_r$  and  $L_s$ .

According to the modulation trajectory and closed-loop control diagram,  $D_1$  versus phase shift angle and battery voltage

$$\begin{cases} \varphi_m = X_s \left( \frac{M+2}{M} \right) \left[ \frac{I_{ZVS}}{nV_{bat}} - \frac{M-2}{8n^2 X_r} - \left( \frac{0.5\pi M}{X_s(M+2)} - \frac{0.25\pi}{n^2 X_r} \right) (M + D_m - 1) \right] \\ \Delta\varphi_m = 4X_s \left[ \frac{I_{ZVS}}{V_o} - \frac{(1-2/M)\pi}{8n^2 X_r} + \frac{\pi}{4n^2 X_r M} (M + D_m - 1) \right] \end{cases} \quad (12)$$

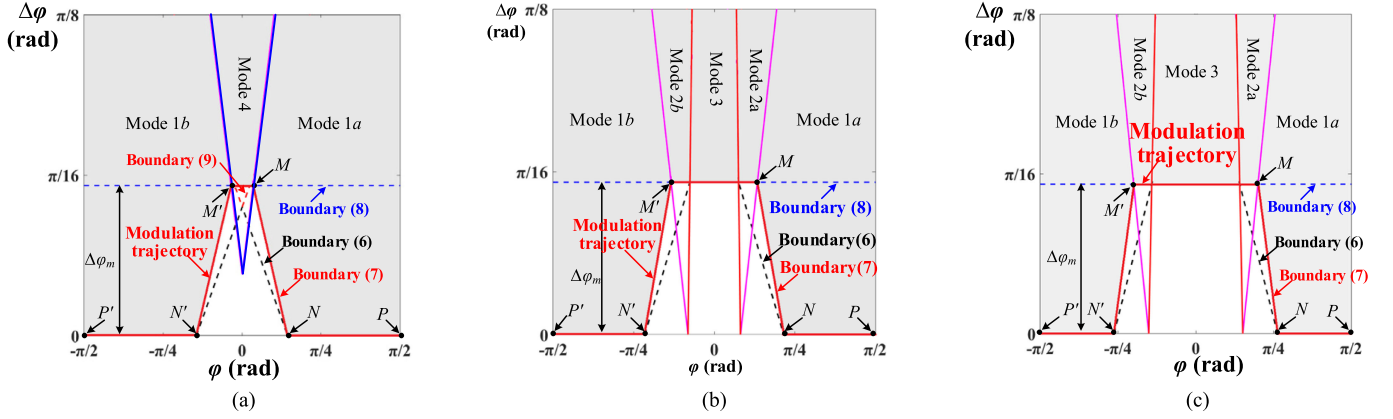


Fig. 9. ZVS range and modulation trajectory for different battery voltages. (a)  $V_{bat} = 200$  V. (b)  $V_{bat} = 250$  V. (c)  $V_{bat} = 300$  V.

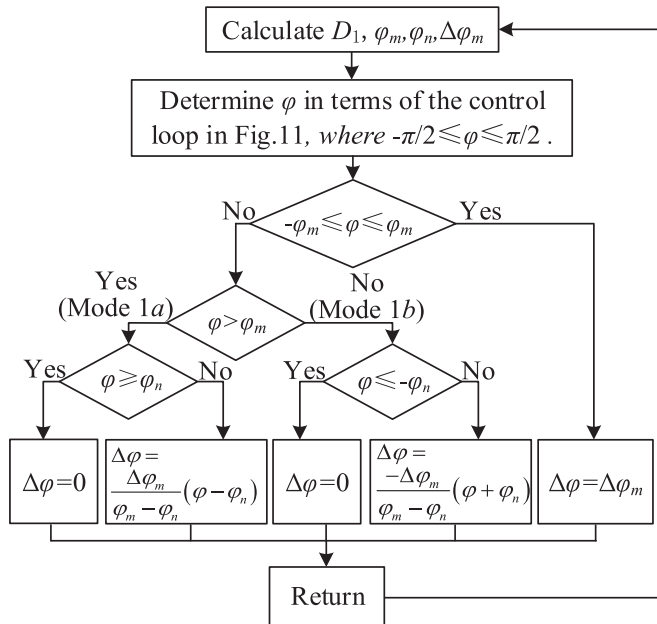


Fig. 10. Flowchart of the modulation trajectory.

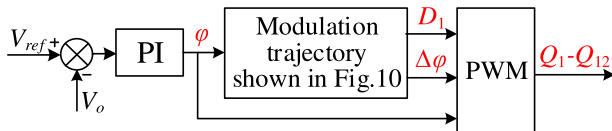


Fig. 11. Closed-loop control diagram.

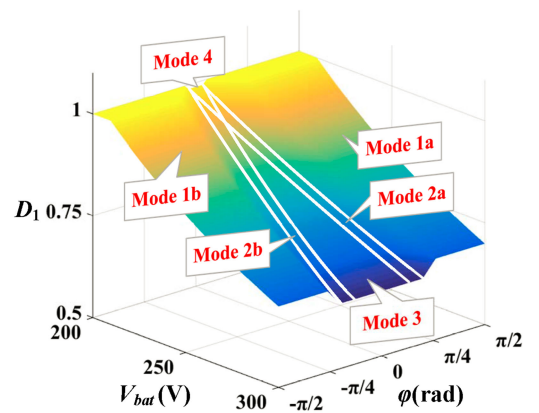


Fig. 12.  $D_1$  versus phase shift angle  $\varphi$  and battery voltage  $V_{bat}$ .

TABLE V  
OUTPUT POWER EXPRESSIONS IN DIFFERENT WORKING MODES

Working mode	Output power
Mode 1a	$P_o = \frac{MV_{bat}^2}{8X_r} \left( 2\varphi_a + 2\varphi_b + 2D_1\pi - D_1^2\pi - \frac{2\varphi_a^2}{\pi} - \frac{2\varphi_b^2}{\pi} - \pi \right)$
Mode 2a	$P_o = \frac{MV_{bat}^2}{8X_r} \left( 4\varphi_a D_1 + 4\varphi_b + 2D_1\pi - D_1^2\pi - \frac{4\varphi_b^2}{\pi} - \pi \right)$
Mode 3	$P_o = \frac{MV_{bat}^2}{4X_r} (\varphi_a + \varphi_b) D_1$
Mode 4	$P_o = \frac{MV_{bat}^2}{4X_r} \left( \varphi_a + \varphi_b + \frac{\varphi_a^2}{\pi} - \frac{\varphi_b^2}{\pi} \right)$

is shown in Fig. 12. As depicted in Fig. 12,  $D_1$  can seamlessly transit between the adjacent working modes.

The output power expressions in different working modes are shown in Table V. The output power in different working modes is not associated with the parameters of the  $LC$  networks, which demonstrates that the  $LC$  networks have no impact on the output performance.

The output power versus the phase shift angle and battery voltage in per unit (p.u.) is shown in Fig. 13, where

$L_r = 24 \mu\text{H}$ ,  $T_s = 12.5 \mu\text{s}$ ,  $L_s = 22 \mu\text{H}$ ,  $n = 1.5$ ,  $I_{zvs1} = 2$  A,  $I_{zvs2} = 2$  A, and  $V_o = 600$  V. Fig. 13(a) shows the relationship among output power, battery voltage, and phase shift in three dimensions. Fig. 13(b) is the right lateral view of Fig. 13(a). In the range of  $\varphi$  from  $-\pi/2$  to  $\pi/2$ , the output power is monotonically increasing. Fig. 13(c) shows the curves of the output power versus the phase shift angle. It illustrates that the converter can achieve seamless transition between the adjacent working modes, which demonstrates that the

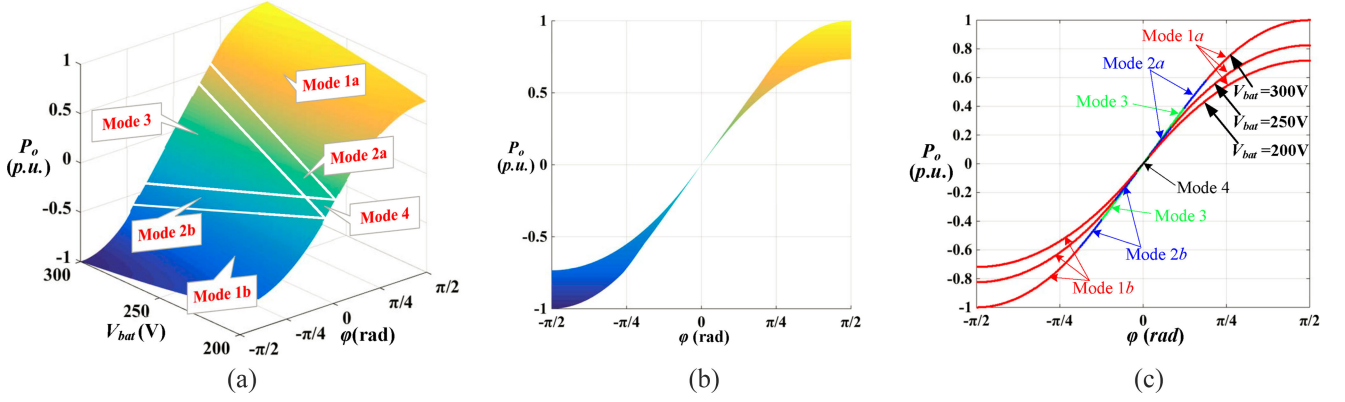


Fig. 13. Output power versus phase shift angle  $\varphi$  and battery voltage  $V_{bat}$ . (a) Three-dimensional surface. (b) Right lateral view of Fig. 13(a). (c) Two-dimensional curves of the output power versus  $\varphi$ .

bidirectional power flow can be controlled by the phase shift angle.

#### D. Design of the Auxiliary Inductor $L_s$

As seen in Fig. 9, the slope of the  $MN$  should be lower than zero. Otherwise, the modulation trajectory cannot be implemented in seamless transition. Therefore, according to (7), the following condition should be satisfied:

$$L_s < \frac{L_r}{\frac{1}{2n^2} + \frac{1}{n^2 M}}. \quad (14)$$

In terms of Fig. 13,  $L_r$  should be first selected to meet the load requirement in different voltages. Then,  $L_s$  can be designed in terms of (14).  $L_{s1}$  and  $L_{s2}$  may not be equal to the set values in the circuit, which may cause the difference of currents in  $L_{s1}$  and  $L_{s2}$ . If the current in the auxiliary is large enough, the modulation scheme is still effective for wide ZVS.

#### E. Switch Conduction Loss Comparison

The RMS of  $i_1$ ,  $i_2$ ,  $i_3$ ,  $i_4$ , and  $i_5$  can be evaluated to investigate the conduction loss. The RMS of  $i_1$  reflect the conduction loss of  $Q_1 - Q_4$ ; the RMS of  $i_2$  and  $i_5$  reflect the conduction loss of  $Q_5, Q_6, Q_9$ , and  $Q_{10}$ ; the RMS of  $i_3$  and  $i_4$  reflect the conduction loss of  $Q_7, Q_8, Q_{11}$ , and  $Q_{12}$ . The RMS current in the converter can be defined as follows: eq.(15) shown at the bottom of this page.

The RMS currents versus the output power with different voltage gain are illustrated in Fig. 14. The solid lines are the RMS currents of the proposed converter, and the dashed lines are the RMS currents of the conventional OSDAB converter (shown in Fig. 2). The series inductance and turns ratio of the transformers in both converters are the same. The OSDAB is also operated in duty ratio control on the battery side. As seen in Fig. 14, the RMS current in the conventional OSDAB converter

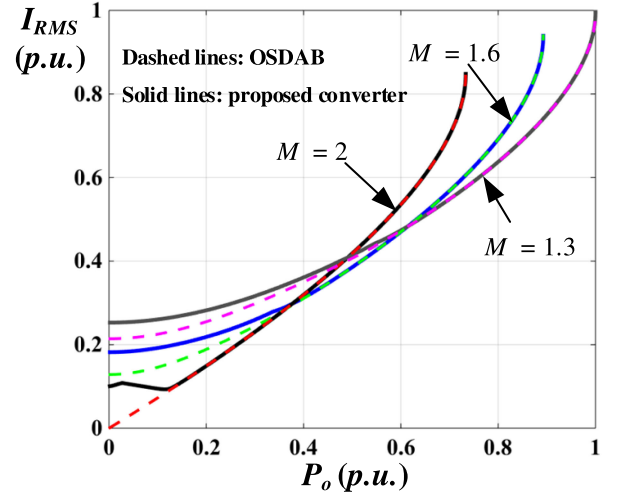


Fig. 14. RMS currents in p.u. in the converter versus the output power (dashed lines: conventional OSDAB converter without  $LC$  networks; solid lines: proposed converter).

is lower than that in the proposed converter under light loads, but ZVS in the proposed converter can be achieved. Furthermore, the RMS current in the converter is very low under light loads, so the conduction loss does not affect the total loss too much. With the increase of the battery voltage, the conventional OSDAB converter will work in hard switching in wide load range, which lowers the efficiency. All the switches in the proposed converter can achieve ZVS even in no load case. The switching loss can be dramatically reduced, and the efficiency can be improved. In heavy loads, the current in the transformer can maintain all the switches in ZVS, so the RMS current curves of the two converters coincide in heavy loads. In this case, the proposed converter actually works in the same mode as the conventional OSDAB converter. Therefore, the currents in dual  $LC$

$$I_{RMS} = \frac{2}{n} \sqrt{\frac{1}{T_s} \int_0^{T_s} i_1^2(t) dt} + \sqrt{\frac{1}{T_s} \int_0^{T_s} i_2^2(t) dt} + \sqrt{\frac{1}{T_s} \int_0^{T_s} i_3^2(t) dt} + \sqrt{\frac{1}{T_s} \int_0^{T_s} i_4^2(t) dt} + \sqrt{\frac{1}{T_s} \int_0^{T_s} i_5^2(t) dt} \quad (15)$$

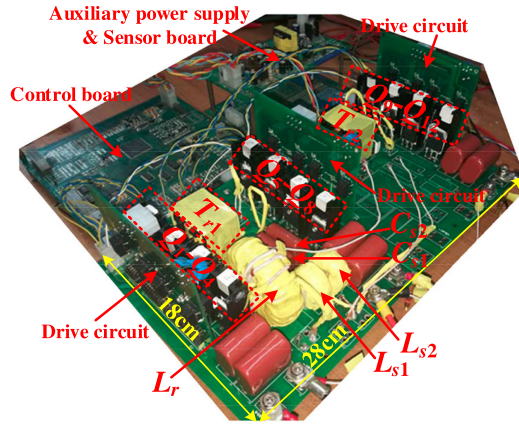


Fig. 15. 1.3 kW experimental prototype for test.

TABLE VI  
DETAILED SPECIFICATIONS

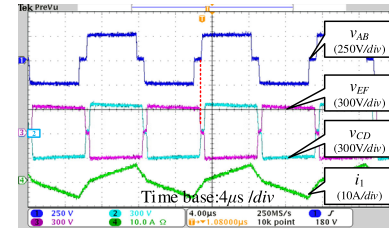
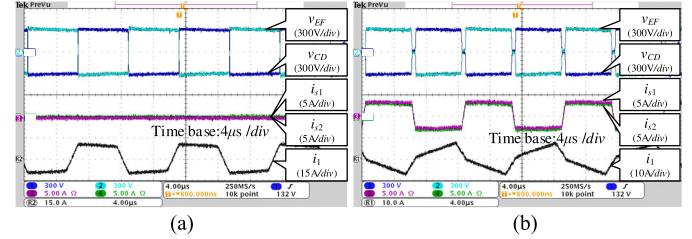
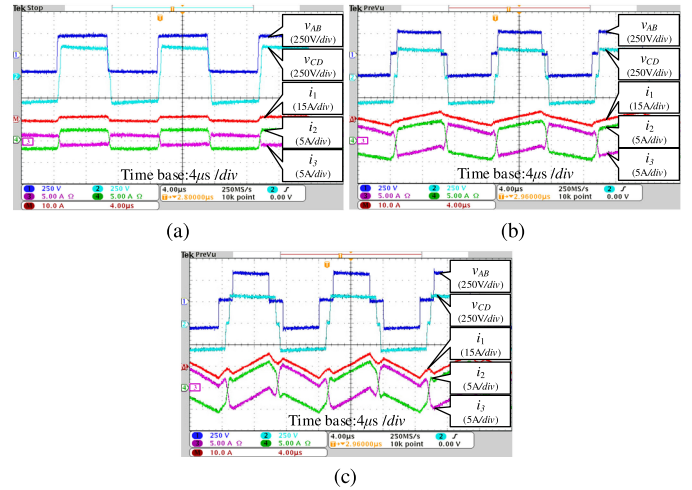
Items	Symbol	Parameter
Battery voltage	$V_{bat}$	200 V~300 V
Output voltage	$V_o$	600 V
Turns ratio of the transformers	$n$	1.5
Switching frequency (period)	$f_s (T_s)$	80 kHz (12.5 $\mu$ s)
Switches	$Q_{1-12}$	FQA28N50
Series inductor	$L_r$	24 $\mu$ H
Auxiliary inductor $L_{s1}$	$L_{s1}$	22 $\mu$ H
Auxiliary inductor $L_{s2}$	$L_{s2}$	22 $\mu$ H
Auxiliary capacitor $C_{s1}$	$C_{s1}$	4.7 $\mu$ F
Auxiliary capacitor $C_{s1}$	$C_{s2}$	4.7 $\mu$ F
Output filter capacitance	$C_{o1}, C_{o2}$	20 $\mu$ F
Dead time	$t_{dead}$	400ns

networks are equal to zero, and the loss caused by LC networks is reduced to zero.

#### IV. EXPERIMENTAL VERIFICATIONS

To verify the proposed output-series DAB converter with dual auxiliary LC networks, a 1.3 kW experimental prototype is built. In energy storage system, the output can be linked to a dc bus to compensate the mismatch of the power supply and load demands. Therefore, the output voltage is set as a constant value of 600 V, and the battery voltage is 200–300 V. Fig. 15 shows the prototype of the test. The series inductor is selected as 25  $\mu$ H to meet the load requirement. According to (14),  $L_s$  should be less than 54  $\mu$ H. In the experimental prototype  $L_s$  is selected as 22  $\mu$ H. The detailed specifications are shown in Table VI. As seen, the volume of  $L_{s1}$ ,  $L_{s2}$ ,  $C_{s1}$ , and  $C_{s2}$  is very small, so they do not affect the power density and do not cost too much.  $I_{ZVS1}$  and  $I_{ZVS2}$  are evaluated as 2 A.

Fig. 16 shows the key waveforms of  $v_{AB}$ ,  $v_{CD}$ , and  $v_{EF}$ , when  $V_{bat} = 250$  V and  $P_o = 650$  W.  $v_{CD}$  and  $v_{EF}$  are symmetrical with the horizontal axis, the currents in the dual auxiliary LC networks are determined by  $v_{CF}$  and  $v_{DE}$ . As seen in the figure,

Fig. 16. Measured key waveforms of  $v_{AB}$ ,  $v_{CD}$ , and  $v_{EF}$  when  $V_{bat} = 250$  V,  $P_o = 650$  W.Fig. 17. Currents in the auxiliary LC networks. (a)  $V_{bat} = 200$  V and  $P_o = 650$  W. (b)  $V_{bat} = 250$  V and  $P_o = 650$  W.Fig. 18. Measured key waveforms for the forward power flow in light loads. (a)  $V_{bat} = 200$  V,  $P_o = 300$  W. (b)  $V_{bat} = 250$  V,  $P_o = 300$  W. (c)  $V_{bat} = 300$  V,  $P_o = 300$  W.

the converter works in Mode 2a. The voltage amplitudes of  $v_{CD}$  and  $v_{EF}$  are almost same, which reflects the voltage balance of the output capacitors.

Fig. 17 shows the waveforms of  $v_{CD}$ ,  $v_{EF}$ , and currents in the auxiliary LC networks. As seen in Fig. 17(a), when  $V_{bat} = 200$  V and  $P_o = 650$  W, the converter can achieve ZVS even without the LC networks. Therefore,  $i_{s1}$  and  $i_{s2}$  are controlled to zero. As seen in Fig. 17(b), when  $V_{bat} = 250$  V and  $P_o = 650$  W,  $i_{s1}$  and  $i_{s2}$  are adjusted to be large enough for ZVS. In all these cases,  $i_{s1}$  and  $i_{s2}$  are the same.

Fig. 18 shows the forward power flow when the converter works in light loads. Fig. 18(a) shows experimental results when the battery voltage is 200 V. In this case, the converter works in Mode 4. The phase shift angle  $\Delta\varphi$  causes current difference

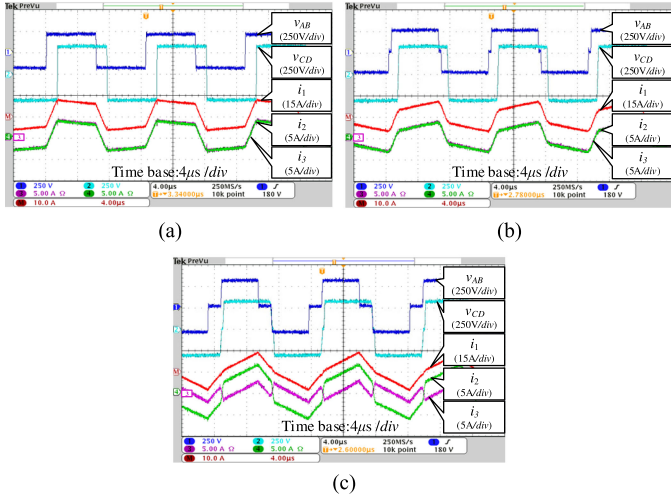


Fig. 19. Measured key waveforms for the forward power flow in heavy loads. (a)  $V_{bat} = 200$  V,  $P_o = 1300$  W. (b)  $V_{bat} = 250$  V,  $P_o = 1300$  W. (c)  $V_{bat} = 300$  V,  $P_o = 1300$  W.

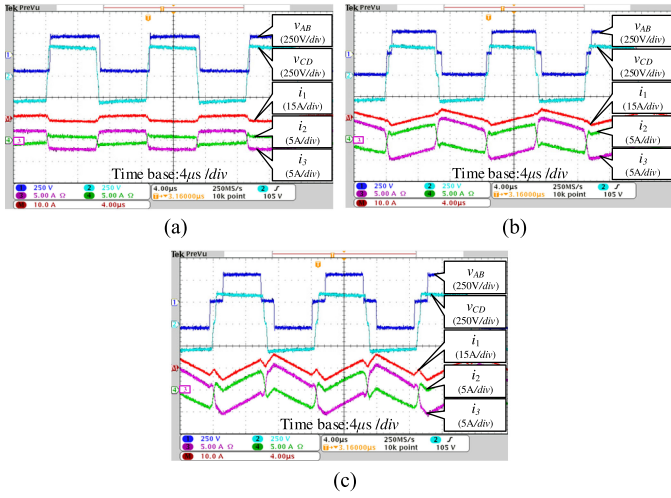


Fig. 20. Measured key waveforms for the reverse power flow in light loads. (a)  $V_{bat} = 200$  V,  $P_o = -328$  W. (b)  $V_{bat} = 240$  V,  $P_o = -313$  W. (c)  $V_{bat} = 280$  V,  $P_o = -300$  W.

between  $i_2$  and  $i_3$ , so the converter can achieve ZVS of all the switches in this case. Fig. 18(b) and (c) show the forward experimental results in light loads when the battery voltages are 250 and 300 V, respectively. With the increase of the battery voltage,  $\Delta\varphi$  is adaptively regulated to keep the converter work in ZVS over the wide battery range.

Fig. 19 shows the key waveforms for the forward power flow in heavy loads. Fig. 19(a) and (b) show the experimental results when the battery voltages are 200 and 250 V, respectively. In these two cases, the converter works in Mode 1a. The converter can achieve ZVS of all the switches even if  $\Delta\varphi$  is equal to zero. In Fig. 19(c), when the battery voltage is 300 V,  $\Delta\varphi$  is regulated to be greater than zero for ZVS. The conventional OSDAB converter will lose ZVS.

Fig. 20 shows the key waveforms for the reverse power flow with light loads. In Fig. 20(a), the converter works in Mode 4.

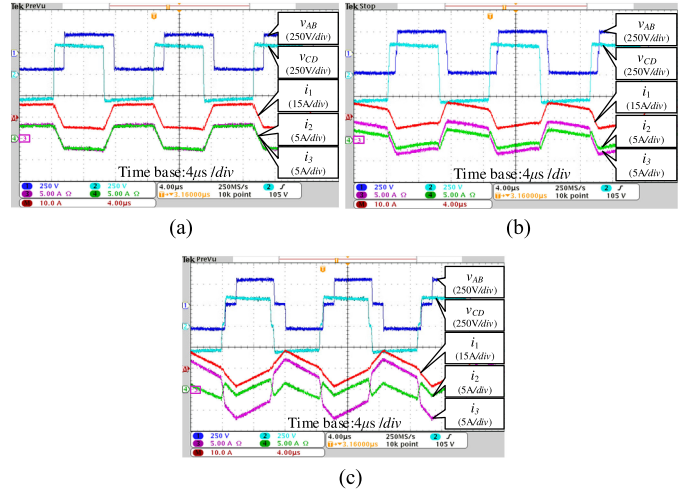


Fig. 21. Measured key waveforms for the reverse power flow in heavy loads. (a)  $V_{bat} = 200$  V,  $P_o = -1200$  W. (b)  $V_{bat} = 240$  V,  $P_o = -1250$  W. (c)  $V_{bat} = 280$  V,  $P_o = -1268$  W.

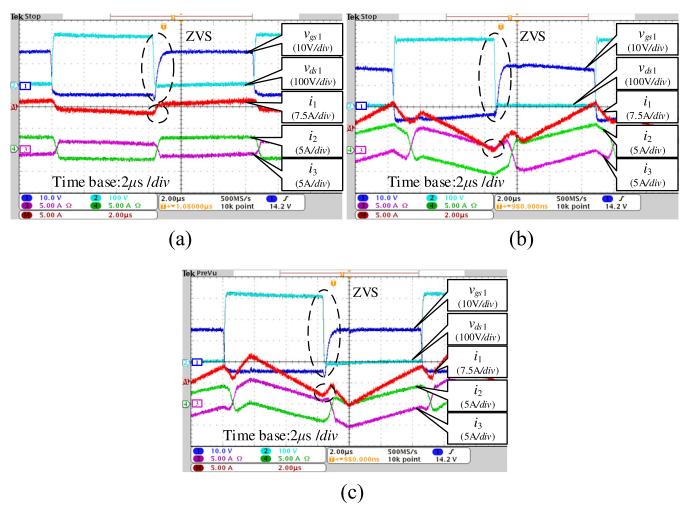


Fig. 22. Gate signal and drain-source voltage of switch  $Q_1$ . (a)  $V_{bat} = 200$  V,  $P_o = 300$  W. (b)  $V_{bat} = 300$  V,  $P_o = 300$  W. (c)  $V_{bat} = 300$  V,  $P_o = -300$  W.

In Fig. 20(b), the converter works in Mode 2b. In Fig. 20(c), the converter works in Mode 3. In these cases,  $\Delta\varphi$  is greater than zero for the ZVS of  $Q_5 - Q_8$ . The working modes in Fig. 20 are nearly symmetrical with those in Fig. 18.

Fig. 21 shows the key waveforms for the reverse power flow with heavy loads. As shown in Fig. 21(a) and (b), when the battery voltages are 200 and 240 V and the load power is  $-1200$  W, the converter works in Mode 1b. In Fig. 21(b), the converter works in Mode 1b, and  $\Delta\varphi$  is a little greater than zero. As illustrated in Fig. 21(c), with the increase of the battery voltage, the phase shift angle is decreased and the converter switches to Mode 2b.

Fig. 22 shows the gate signal and drain-source voltage of switch  $Q_1$ . In all different working modes,  $i_1$  is less than zero during the commutation interval. The energy storage in the junction capacitor is discharged by  $i_1$ , illustrating that  $Q_1$  works in

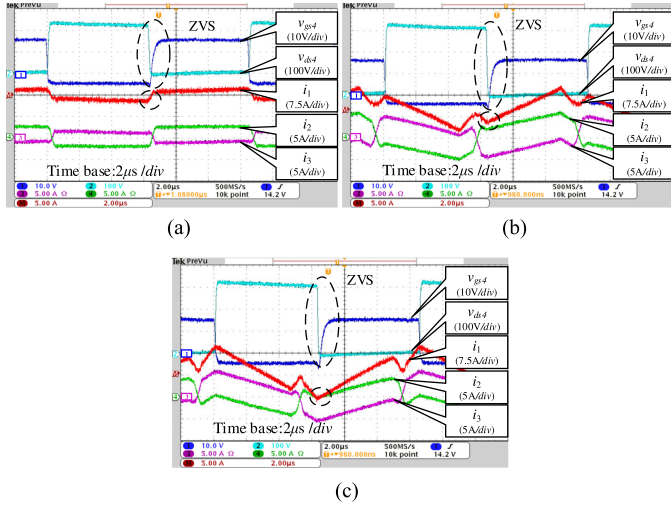


Fig. 23. Gate signal and drain–source voltage of switch  $Q_4$ . (a)  $V_{bat} = 200$  V,  $P_o = 300$  W. (b)  $V_{bat} = 300$  V,  $P_o = 300$  W. (c)  $V_{bat} = 300$  V,  $P_o = -300$  W.

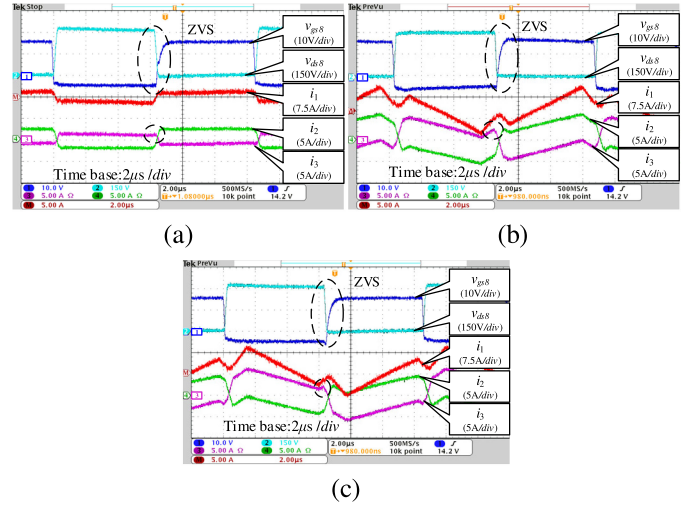


Fig. 25. Gate signal and drain–source voltage of switch  $Q_8$ . (a)  $V_{bat} = 200$  V,  $P_o = 300$  W. (b)  $V_{bat} = 300$  V,  $P_o = 300$  W. (c)  $V_{bat} = 300$  V,  $P_o = -300$  W.

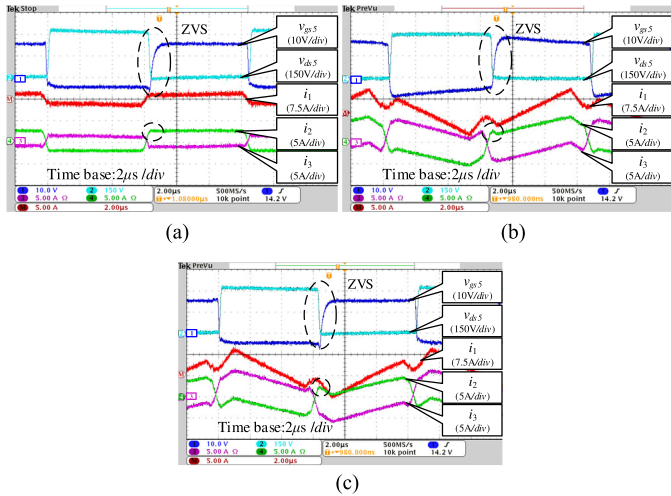


Fig. 24. Gate signal and drain–source voltage of switch  $Q_5$ . (a)  $V_{bat} = 200$  V,  $P_o = 300$  W. (b)  $V_{bat} = 300$  V,  $P_o = 300$  W. (c)  $V_{bat} = 300$  V,  $P_o = -300$  W.

ZVS for both forward and reversed power flow.  $Q_2$  works in the same mode with  $Q_1$ , so it can also achieve ZVS.

Fig. 23 shows the gate signal and drain–source voltage of switch  $Q_4$ .  $i_1$  is still less than zero during the commutation interval of  $Q_4$ . It also illustrates that  $Q_4$  can achieve ZVS.  $Q_3$  works in the same modes with  $Q_4$ , which demonstrates that  $Q_3$  can also achieve ZVS.

Fig. 24 shows the gate signal and drain–source voltage of switch  $Q_5$ . As seen in different working modes, before  $Q_5$  is turned ON,  $i_2$  is large enough to charge and discharge the junction capacitors of  $Q_6$  and  $Q_5$ .  $Q_5$  can work in ZVS in both forward and reverse power flow.  $Q_6$ ,  $Q_9$ , and  $Q_{10}$  operate in the same ZVS constraint as  $Q_5$ , so they are also easy to achieve ZVS.

Fig. 25 shows the gate signal and drain–source voltage of switch  $Q_8$ . As seen during the dead time interval of  $Q_8$ ,  $i_3$  is large enough to charge and discharge the junction capacitors of  $Q_7$  and  $Q_8$ . It validates the ZVS performance for  $Q_8$  in both

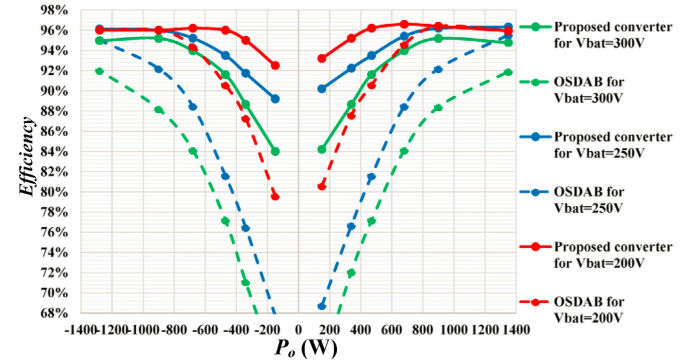


Fig. 26. Efficiency curves for the proposed converter and OSDAB.

forward and reverse power flow.  $Q_7$ ,  $Q_{11}$ , and  $Q_{12}$  operate in the same working mode as  $Q_8$ , so they can also achieve ZVS.

The measured efficiency curves for the proposed converter and OSDAB converter (shown in Fig. 2) are shown in Fig. 26. When the battery voltage is 200 V, the OSDAB can achieve ZVS in heavy load even without auxiliary LC networks. Therefore, at 200 V battery voltage, the efficiency curves of the proposed converter and OSDAB converter coincide in heavy load. In all the working modes, the proposed converter can achieve ZVS, so the efficiency of the proposed converter is greatly improved compared with the OSDAB converter. Especially at the 300 V battery voltage and a 1350 W load, an efficiency improvement of more than 2% is achieved.

The calculated loss distribution in 1.3 kW output power is shown in Fig. 27. In 200 V battery voltage, the current amplitude is lower than 250 and 300 V battery voltage, so series inductor core loss is lower than that in 250 and 300 V battery voltage. The calculated RMS in the series inductor versus the battery voltage in the rated load is shown in Fig. 28. The RMS current in 250 V battery voltage is lower than that in 200 and 300 V battery voltages, so the copper loss in the series inductor and transformer is lower than that in 200 and 300 V battery voltage.

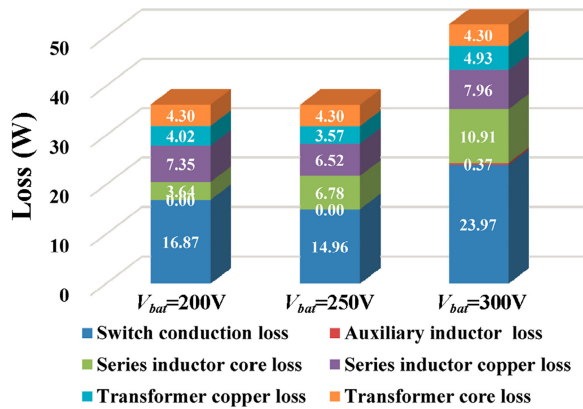


Fig. 27. Loss breakdown in 1.3 kW output power.

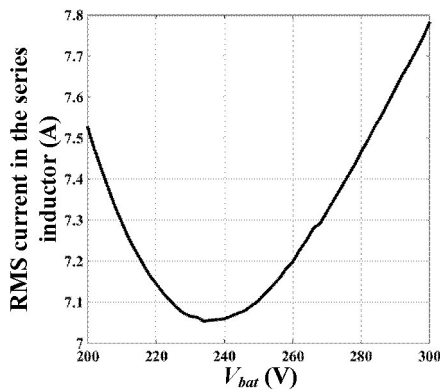


Fig. 28. RMS current in the series inductor versus the battery voltage in 1.3 kW.

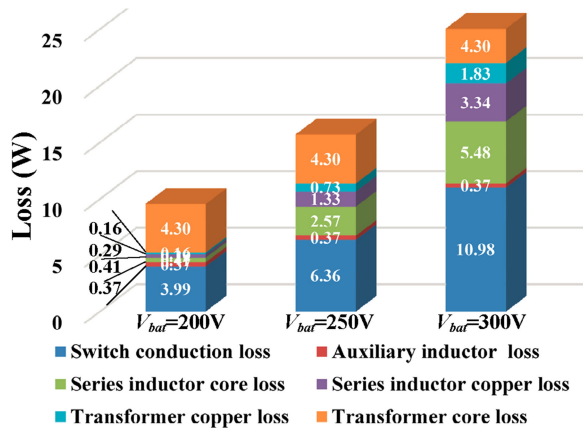


Fig. 29. Loss breakdown in 200 W output power.

In 200 and 250 V, the converter can achieve ZVS for all the switches even without *LC* networks. Therefore, the loss caused by *LC* networks is almost zero. In 300 V battery voltage, all the switches can achieve ZVS with *LC* networks. The loss caused by *LC* networks is very low. Because of the ZVS of all the switching, the switching loss can be ignored, and the efficiency is dramatically improved.

Fig. 29 shows the calculated loss distribution in 300 W output power. When the battery voltage is 200 V, the peak current and

RMS current in the transformers are very low. Therefore, the conduction loss and core loss are very low. With the increase of the battery voltage, the peak current and RMS current in the transformers are increased. The conduction loss and core loss are increased simultaneously.

### V. CONCLUSION

This paper presents an output-series dual active bridge converter with dual auxiliary *LC* networks. This converter can meet the high output dc-link voltage requirement. The two auxiliary *LC* networks are connected with the bridge legs of the two output full bridges. With the aid of the dual auxiliary *LC* networks, the converter can achieve ZVS performance of the output full bridges over full load range and wide battery voltage range. The ZVS boundaries of all the switches have been analyzed, and the modulation trajectory is designed according to the ZVS boundaries. The flowchart of the modulation trajectory can guarantee seamless transition between the adjacent working modes. Therefore, the converter can achieve ZVS with low conduction loss. Although the conduction loss in the proposed converter is a little bit greater than the conventional OSDAB converter, the proposed converter has a good tradeoff between the ZVS performance and the conduction loss in auxiliary circuit. Finally, the experimental results validate the ZVS performance in the proposed converter. The efficiency curves demonstrate the efficiency improvement in the OSDAB with dual *LC* networks.

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