

# Windowed SHE-PWM of Interleaved Four-Quadrant Converters for Resonance Suppression in Traction Power Supply Systems

Kejian Song, Georgios Konstantinou, *Member, IEEE*, Wu Mingli, Pablo Acuna, *Member, IEEE*, Ricardo P. Aguilera, *Member, IEEE*, and Vassilios G. Agelidis, *Fellow, IEEE*

**Abstract**—AC electric locomotives that use a number of interleaved four-quadrant converters generate high-frequency switching harmonics which may stimulate certain resonances in traction power supply systems (TPSSs). A windowed selective harmonic elimination pulse-width modulation (SHE-PWM) method is proposed to suppress such resonances. Owing to the windowed design and the precalculated solutions, the proposed method covers the wide potential resonant frequency range and addresses the resonant frequency variation while keeping the low switching frequency of the traction converters. The proposed windowed SHE-PWM is fully tested with a closed-loop controller in a simulation model with the TPSS and the ac electric locomotive. Comparative simulation results show that the windowed SHE-PWM is an effective alternative that overcomes the resonance suppression limitations of the conventional phase-shifted PWM (PS-PWM). The performance of proposed windowed SHE-PWM on an experimental equivalent resonant circuit is further evaluated and compared with PS-PWM. Both simulation and experimental results verify the effectiveness and feasibility of the proposed method.

**Index Terms**—AC electric locomotives, power electronics converters, resonance, selective harmonic elimination PWM, traction power supply system (TPSS).

## I. INTRODUCTION

WITH the development of high-power semiconductor devices and advanced control techniques for power electronics converters, ac-drives have become the most popular

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Kejian Song and Wu Mingli are with the School of Electrical Engineering, Beijing Jiaotong University, Beijing 100044, China (e-mail: 12117360@bjtu.edu.cn; mlwu@bjtu.edu.cn).

G. Konstantinou and P. Acuna are with the School of Electrical Engineering and Telecommunications, The University of New South Wales, Sydney, NSW 2052, Australia (e-mail: g.konstantinou@unsw.edu.au; pablo.acuna@unsw.edu.au).

R. P. Aguilera is with the School of Electrical, Mechanical and Mechatronic Systems, University of Technology Sydney, Sydney, NSW 2007, Australia (e-mail: raguilera@ieee.org).

V. G. Agelidis is with the Department of Electrical Engineering, Technical University of Denmark 2800 Kgs. Lyngby, Denmark (e-mail: vasagel@elektro.dtu.dk).

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TABLE I  
RESONANCE CASES ON CHINESE RAILWAYS

Vehicle type	Frequency (Hz)	Occurrence time	Location
CRH2	1050–1250	Aug. 2008	Wuqing - Yongle
HX <sub>D</sub> 3	850–1050	Mar. 2010	Macheng - Wuhan
CRH380A	2250–2750	Jan. 2011	Guangzhouan Station
HX <sub>D</sub> 3B	1150–1450	Dec. 2011	Shanhaiguan Station
HX <sub>D</sub> 1B	2650–2750	Dec. 2013	Jiujiangxi - Mahuiling
HX <sub>D</sub> 21000	2050–2450	Nov. 2014	Wulipu Station

choice in traction applications globally [1]–[5]. In China, most freight service railways adopt the HX<sub>D</sub> series ac electric locomotives, while all high-speed railways (HSRs) use the CRH series electric multiple units (EMUs). Both of the above locomotives and EMUs use a number of interleaved four-quadrant converters (4QCs) as front-end rectifiers to either draw power from the supply network or inject power back into the supply network during regenerative braking [6]–[9].

### A. Resonance in Traction Power Supply Systems (TPSSs)

Compared with the diode and/or thyristor rectifiers of traditional dc electric locomotives [5], the 4QCs ensure unity power factor and a nearly purely sinusoidal current on the network side. However, the interleaved 4QCs, operating under phase-shifted pulse-width modulation (PS-PWM), still generate a fixed spectrum containing a relatively high amount of sideband harmonics located around the multiples of the carrier frequency. If some of the injected current harmonics, generated by the PWM converters, coincide with the resonant frequency of the TPSS, a resonance will be prone to be stimulated [10], [11]. When a resonance occurs, amplified resonant voltage and current appear in the TPSS, resulting in supply voltage distortion, interference with adjacent communication lines, erroneous operation of protective devices, or even damaging in some high-voltage devices [12], [13]. Typical resonance cases on Chinese railways, occurred in recent years, are summarized in Table I.

The resonance phenomenon has been analyzed through traveling wave theory [14], and a method for online identification of the resonance frequency was proposed in [15]. Two different approaches to deal with this issue were provided in [16] and [17]. However, the German railways that were studied in [14]–[17] have their own TPSS features which are far from the

counterparts in many other countries. Moreover, the 4QC and associated control techniques have seen a great deal of development during the past two decades. Recently, more researchers reported their studies on the TPSS resonance, e.g., [11]–[13], [18]–[21]. Most studies focus on the mechanism of the resonance, and try to illustrate the factors that influence the resonance such as the length of supply section, the position of the vehicle, and the distribution of the resonant harmonics in the TPSS through deriving the impedance-frequency characteristic of the TPSS [19]–[21].

### B. Resonance Suppression Approaches

A number of approaches can be adopted for the resonance suppression in TPSSs. Some older types of ac locomotives and EMUs were equipped with high-pass passive filters (e.g.,  $RC$  branch) to eliminate the high-frequency harmonics [14]. Considering requirements for light weight and reliability, this method is abandoned in many modern ac-drive railway vehicles. An alternative is installing high-pass passive filters in electrical substations (ESSs) or section posts (SPs) [13], [22], [23]. The passive filters can filter out most of the high-frequency harmonics on the supply network, but also move the resonant frequency of the TPSS without any extra circuits on board. However, the bulky ground passive filter equipment increases both cost and space requirements. Active power filters (APFs), with their advantages compared to passive filters, can be used on board the train or installed on the ground to suppress the harmonic propagation on the supply network as documented in the literature [17], [24], [25]. In practice, APFs are currently mature for eliminating lower order harmonics compared to the sideband harmonics, while the extra cost and reliability can be the potential problems for APFs in traction applications.

On the other hand, a proper modulation method that does not generate the resonant frequency harmonics can avoid the resonance potential without any extra drawbacks of the aforementioned approaches [16]. With the additional advantage of tight spectrum control, the selective harmonic elimination PWM (SHE-PWM) can be redefined to address the TPSS resonance problem. In [26], SHE-PWM was initially introduced for two interleaved EMU 4QCs. Although the desired SHE-PWM spectrum performance was obtained, the method did not consider the resonance issue. A resonant harmonic elimination PWM (RHEPWM) method for four interleaved EMU 4QCs was presented in [18]. Essentially, the RHEPWM is a SHE-PWM used for resonant harmonic elimination. This modulation scheme provided a fixed SHE-PWM pattern for a specific resonant frequency but fail to consider the resonant frequency variation [11], [14], [19], [20]. In general, the resonant frequency changes since the train travels across different supply sections. Moreover, the SHE-PWM patterns of the four 4QCs, proposed in [18], have different numbers of commutation angles.

Most of the recent resonance studies, e.g., [11], [13], [18]–[21], focus on EMUs operating on HSRs especially the Chinese cases. The fact is that most of Chinese EMUs are equipped with eight to fourteen 4QCs, and, nevertheless, the ac electric locomotives are equipped with only four, six, or eight

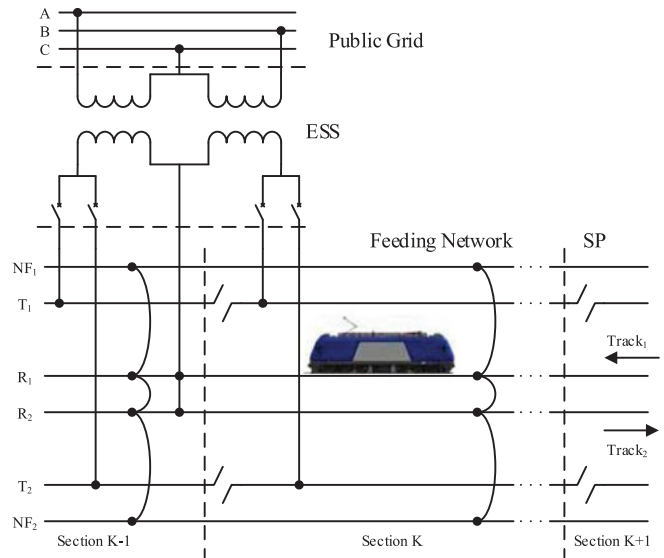


Fig. 1. Configuration of a double-track T-R+NF TPSS. Track<sub>1</sub>: uplink, Track<sub>2</sub>: downlink.

4QCs. Therefore, when PS-PWM schemes are well designed, the sideband harmonic frequencies of EMUs will be very high easy to avoid the resonance. On the contrary, the sidebands of ac electric locomotives, with relatively low frequencies, will be easier to stimulate TPSS resonances. Therefore, more attention should be paid to the ac electric locomotives which are widely running on conventional Chinese railways.

This paper is aimed to propose a windowed SHE-PWM technique to suppress TPSS resonances, considering a typical ac electric locomotive with four interleaved 4QCs. To address this issue, five harmonic free frequency windows are precalculated to account for the potential resonant frequency range and to deal with the resonant frequency variation that depends on the particular TPSS section that the train is running. The rest of this paper is organized as follows. Section II briefly analyzes the mechanism of the TPSS resonance. In Section III, the general formulation of SHE-PWM for interleaved converters is described and then a windowed SHE-PWM technique for four interleaved 4QCs is proposed. Section IV describes the implementation of the proposed method. Section V provides simulation and experimental results to validate the windowed SHE-PWM. Conclusions of this paper are summarized in Section VI. Descriptions and parameters of a typical TPSS studied in this work are presented in Appendixes A and B.

## II. RESONANCE MECHANISM IN TPSSS

The overall structure of a double-track direct feeding system with return wire (T-R+NF) TPSS, which is widely used in conventional Chinese railways, is presented in Fig. 1. This minimum TPSS consists of an ESS, a feeding network section, and a SP. An ac electric locomotive acts as a nonlinear load injecting harmonics into the TPSS. In the ESS, a  $V_v$  connection transformer is commonly used to draw power from three-phase public grid (110 or 220 kV) supplying two sections. The SP located at the end of a section electrically divides the feeding network.

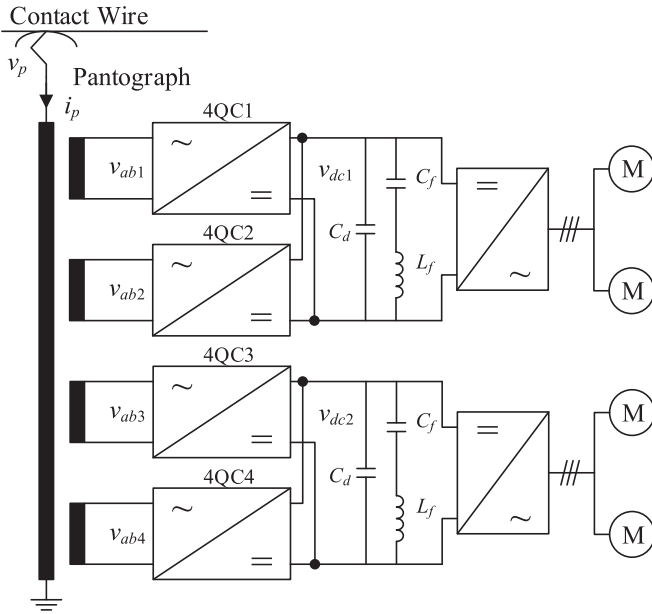


Fig. 2. Configuration of a typical ac electric locomotive drive system.

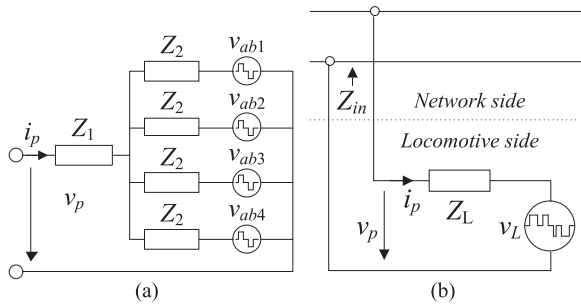


Fig. 3. Network-side model of ac locomotive. (a) Equivalent circuit. (b) Thévenin model coupling with the TPSS.

Treating the locomotive as a constant harmonic current source is not explicit to illustrate the coupling relationship between the TPSS and the locomotive for the purpose of studying the resonance. A detailed model of an ac locomotive should be built according to the electrical structure of its ac-drive system. A typical configuration of the ac locomotive drive system is given in Fig. 2. Four 4QCs, with the same topology of single-phase H-bridge converter, are interleaved via an on-board step-down transformer to draw power from the feeding network through a pantograph. Here,  $v_{abi}$  ( $i = 1, 2, \dots, 4$ ) denotes the 4QC ac-side voltage, while  $v_p$  and  $i_p$  represent the voltage and current at the pantograph. Two of the 4QCs share a common dc-link providing constant voltage for a three-phase inverter driving the induction motors. Additionally,  $v_{dc1}$  and  $v_{dc2}$  stand for the two dc-link voltages,  $C_d$  is the support capacitor,  $C_f$  and  $L_f$  behave as a second harmonic filter branch in a dc link.

Since the four secondary windings of the transformer are considered independent and decoupled, the locomotive network-side model can be represented by using an equivalent circuit as shown in Fig. 3(a). To simplify the analysis, the transformer turn ratio is assumed 1:1 hereinafter.  $Z_1$  and  $Z_2$  represent the leakage

impedances of the transformer primary and secondary windings, respectively. The circuit can be simplified to a Thévenin model with an equivalent voltage source and impedance, respectively

$$v_L = \frac{v_{ab}}{4} = \frac{\sum_{i=1}^4 v_{abi}}{4} \quad (1)$$

$$Z_L(j\omega) = Z_1(j\omega) + \frac{Z_2(j\omega)}{4} \quad (2)$$

where  $v_{ab}$  is the combined ac-side voltage of the four interleaved 4QCs. Consequently, the coupling relationship between the ac locomotive and the TPSS is depicted in Fig. 3(b) where  $Z_{in}$  stands for the input impedance of the TPSS seen from the pantograph. Neglecting the background harmonics, a  $k$ th harmonic  $v_{Lk}$  of the equivalent voltage generates a harmonic voltage at the pantograph

$$v_{pk} = \frac{Z_{in}(jk\omega_1)}{Z_{in}(jk\omega_1) + Z_L(jk\omega_1)} v_{Lk} \quad (3)$$

where  $\omega_1$  stands for the fundamental angular frequency. According to the analysis above, the following remarks can be obtained.

*Remark 1:* Both the equivalent impedances of the TPSS and the locomotive,  $Z_{in}$  and  $Z_L$ , create a coupling impedance system with one or more resonant frequencies.<sup>1</sup> The composite voltage  $v_{ab}$  contains higher order harmonics which may coincide with the resonant frequency stimulating very high harmonic voltage at the pantograph  $v_{pk}$  causing a series detrimental effects, which is collectively referred to as TPSS resonance.

*Remark 2:* The equivalent impedance  $Z_{in}$  of TPSS refers to the impedance-frequency characteristics of the ESS and the feeding network. The SP provides no impedance, but defines the length of a TPSS that affects  $Z_{in}$  as well as the resonant frequency. Modeling the complex TPSS in frequency domain is another attractive aspect of the resonance research which is significant to get a comprehensive understanding of the resonance. Brief descriptions and parameters of the ESS and the feeding network studied in this paper are given in Appendixes A and B, respectively.

### III. PROPOSED WINDOWED SELECTIVE HARMONIC ELIMINATION PWM

#### A. General Formulation of SHE-PWM for Multiple Interleaved Converters

SHE-PWM provides a tight control of the harmonic spectrum of a given PWM voltage waveform [27]. The acquisition, continuity, and range of the available solutions depend on the formulation of the SHE-PWM problem for a particular application and converter. Interested readers are referred to [28] for a detailed mathematical analysis of multilevel SHE-PWM. In the case of  $k$  interleaved three-level H-bridge converters, the problem is

<sup>1</sup>Typically, there are more than one resonant frequencies in a TPSS [14], [20]. The lowest resonant frequency is the one that is easily within the range of the PWM harmonics of lower sideband groups (see Table I for such examples). This can have detrimental effects on the operation of the system and is the main concern of this paper. The impact of other resonant frequencies to the system is negligible and is not linked to the PWM.

formulated individually for the fundamental frequency component of each converter, while higher order harmonic elimination is achieved for the combined multilevel waveform. Assuming quarter-wave (QW) symmetry with  $N$  transitions (switching angles) per quarter-period, per-bridge, the fundamental frequency components can be written as

$$\begin{aligned} & \left( \sum_{i=1}^N (-1)^i \cos \alpha_i - M_1 \right)^2 + \left( \sum_{i=N+1}^{2N} (-1)^{i+1} \cos \alpha_i - M_2 \right)^2 \\ & + \dots + \left( \sum_{i=(k-1)N+1}^{kN} (-1)^i \cos \alpha_i - M_k \right)^2 = 0 \end{aligned} \quad (4)$$

where  $M_k$  is the modulation index corresponding to the  $k$ th converter and the higher order harmonics as

$$b_n = \left[ \sum_{i=1}^N (-1)^i \cos n\alpha_i + \sum_{i=N+1}^{2N} (-1)^{i+1} \cos n\alpha_i + \dots + \sum_{i=(k-1)N+1}^{kN} (-1)^i \cos n\alpha_i \right]^2 \quad (5)$$

Typically, the system operates with equal modulation indices in all the bridges so that  $M_1 = M_2 = \dots = M_k = M$ . For a single-phase output voltage,  $M$  is generally governed by

$$M = \frac{\pi}{4V_{dc}} \hat{V}_1 \quad (6)$$

where  $\hat{V}_1$  and  $V_{dc}$  are the target fundamental component and dc voltage, respectively. The restrictions for the angles, in order to derive a feasible three-level waveform, are independently applied for each bridge so that

$$\begin{aligned} & 0 < \alpha_1 < \alpha_2 < \dots < \alpha_N < \pi/2, \\ & 0 < \alpha_{N+1} < \alpha_{N+2} < \dots < \alpha_{2N} < \pi/2, \\ & \dots \\ & 0 < \alpha_{(k-1)N+1} < \alpha_{(k-1)N+2} < \dots < \alpha_{kN} < \pi/2. \end{aligned} \quad (7)$$

A total of  $kN$  angles are available for the control of the fundamental frequency and the elimination of the higher order harmonics. A number of  $k$  harmonics are required to control the fundamental frequency of each converter, while maximum  $k(N-1)$  additional high-order harmonics can be eliminated. The solutions to the SHE-PWM problem can be found through an iterative minimization/optimization process of the total harmonic spectrum so that (4) and (5) are simultaneously equal to zero, following the set of restrictions of (7) [28]. A typical issue with SHE-PWM for multiple interleaved and multilevel converters is that the range and continuity of solutions are quite limited [29]. To improve both of these aspects, the number of harmonics that are eliminated can be reduced from the maximum number of  $k(N-1)$  harmonics by one or two, effectively relaxing the requirements of the SHE-PWM problem.

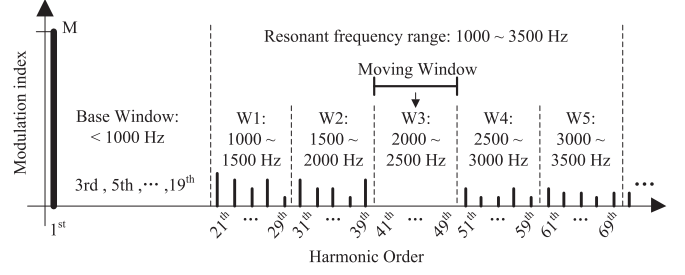


Fig. 4. Concept of windowed SHE-PWM utilizing W3, eliminating resonant harmonics between 2000 and 2500 Hz.

## B. Windowed SHE-PWM

In order to address the resonance issue that may potentially appear in the coupling system of the TPSS and the locomotive, the SHE-PWM problem is reformulated so that both low-order harmonics as well as harmonics around the resonant frequency are eliminated. However, the resonant frequency is not constant but depends on the TPSS section the locomotive is located. Thus, a fixed SHE-PWM cannot tackle the resonant frequency variation. To address all the problems described above, a windowed SHE-PWM method featuring a base window plus a moving window is proposed in this paper as shown in Fig. 4.

For the windowed SHE-PWM, two distinct windows of eliminated harmonics are defined. *The base window* is fixed at low frequency range. Inside this window, the fundamental frequency components are controlled to  $M$  and all the odd harmonics are eliminated. *The moving window* addresses the resonance for a particular TPSS section and moves accordingly. The frequency range of the resonances is split into several subregions; each of them with a width equal to the moving window. When the resonant frequency is in a subregion, all harmonics within the window are eliminated.

As discussed earlier, the design of the windowed SHE-PWM depends on the number of commutation angles that can be used to control harmonics. Considering a typical locomotive, as described previously, with four interleaved single-phase H-bridge converters conventionally operating with carrier frequencies between 250 and 450 Hz. Accordingly,  $k = 4$  and  $N = 5$  are considered in this study so that a total of 20 angles can be used to formulate the SHE-PWM problem. Out of the 20 angles, 4 angles are required to handle the fundamental frequency components of the four bridges, 2 angles are discarded for relaxing the problem restrictions [29], and 14 angles are used to eliminate harmonics including nine low-order harmonics (from the 3rd to the 19th) in the base window and 5 harmonics in the moving window.

According to the previous angle arrangements, the proposed SHE-PWM is defined as shown in Fig. 4. The base window frequency range is up to 1000 Hz. The moving window has a width of 500 Hz and is selected based on the potential resonant frequency range (from 1000 to 3500 Hz). Hence, a total of five subregions (W1, W2, ..., W5) are required. For instance, in Fig. 4, when the resonant frequency is within window W3, the five angles of the moving window are used to eliminate the odd harmonics between 2000 and 2500 Hz. In order to avoid the

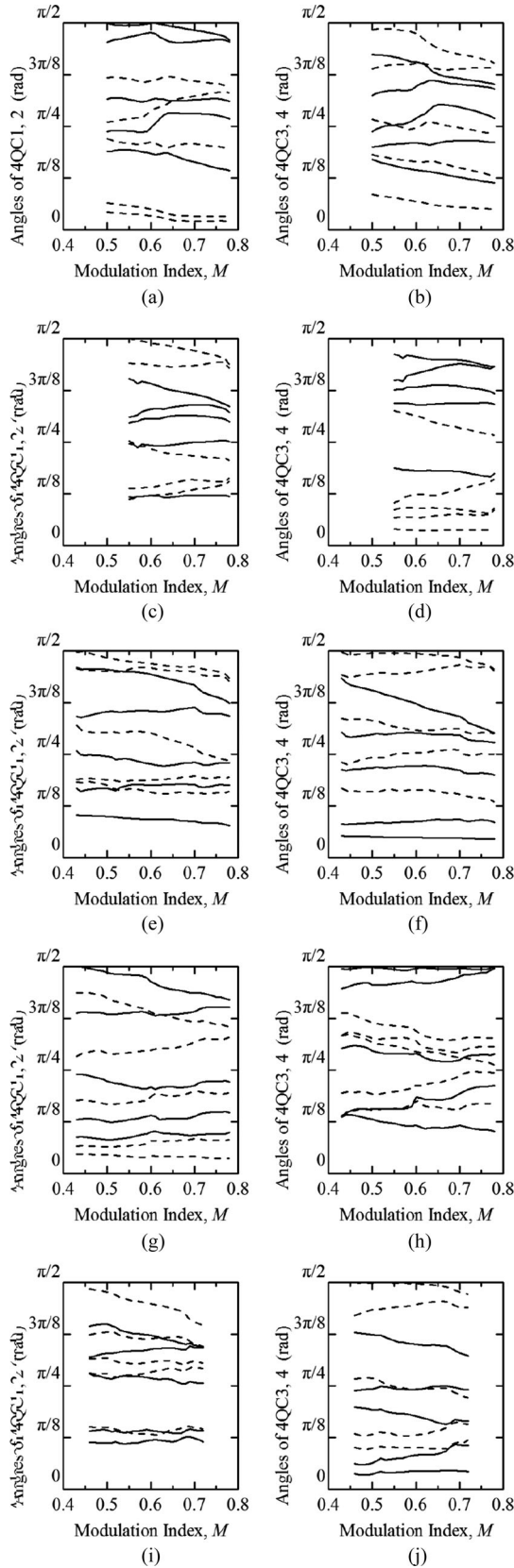


Fig. 5. Windowed SHE-PWM solutions. (a) and (b): W1, (c) and (d): W2, (e) and (f): W3, (g) and (h): W4, (i) and (j): W5. Solid line: angles of 4QC1 and 4QC3, Dashed line: angles of 4QC2 and 4QC4.

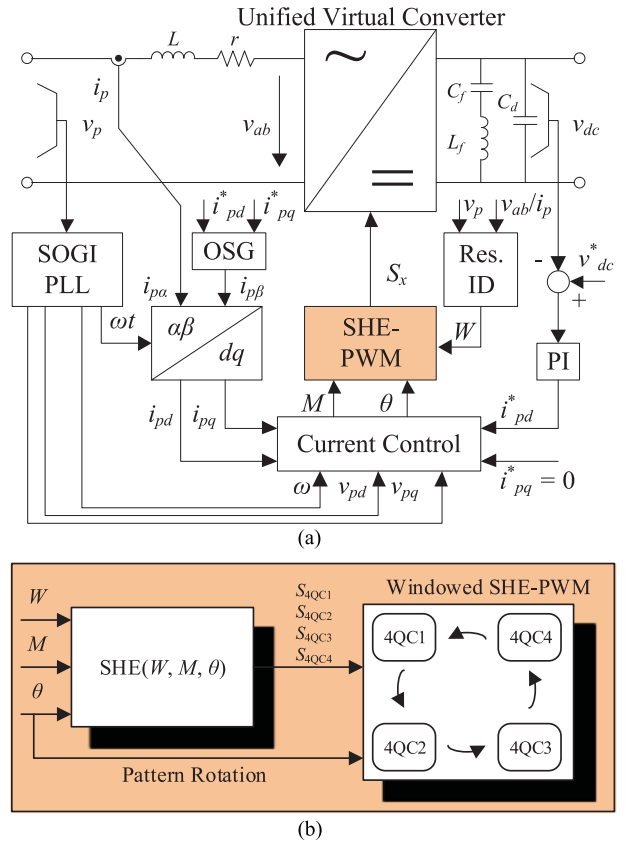


Fig. 6. Full implementation: (a) Unified virtual converter and its master controller. (b) Windowed SHE-PWM.

impact of large noneliminated harmonics that may be excited by resonant frequencies, an overlap between the two windows can also be considered. Alternatively, the multiple solutions of the windowed SHE-PWM problem can be evaluated and those with relatively high noneliminated harmonics near the windows can be penalized/discarded.

The windowed SHE-PWM problem is transcendental in nature and exhibits multiple solutions. Considering the base and moving windows of Section III-B and Fig. 4, the problem is formulated and a unique set of solutions for the switching patterns of the four H-bridges that covers all five of the windows is shown in Fig. 5. The reduction by two in the number of eliminated high-order harmonics facilitates the acquisition and the continuity of the acquired solutions at the cost of harmonic performance for SHE-PWM technique.

#### IV. IMPLEMENTATION

Closed-loop implementation of a SHE-PWM technique is not a trivial issue, and in this section, a full implementation of the proposed windowed SHE-PWM method is developed in the  $dq$  frame.

The proposed SHE-PWM pattern is calculated to steer the composite voltage  $v_{ab}$  rather than any single 4QC ac-side voltage  $v_{abi}$ . Therefore, a unified virtual converter, representing the equivalent behavior of the four interleaved 4QCs, is defined as

TABLE II  
ELECTRICAL PARAMETERS OF THE LOCOMOTIVE MODEL

Parameter	Description	Value
$P_N$	Rated output power	4800 kW
$N_T$	Transformer turns ratio	25000 V : 970 V
$L$	AC filter inductance	1.75 mH
$r$	AC filter resistance	0.05 $\Omega$
$V_{dc}^*$	DC-link voltage reference	1800 V
$C_d$	DC-link support capacitance	12 mF
$C_f$	Capacitance of second harmonic filter	9.85 mF
$L_f$	Inductance of second harmonic filter	0.257 mH

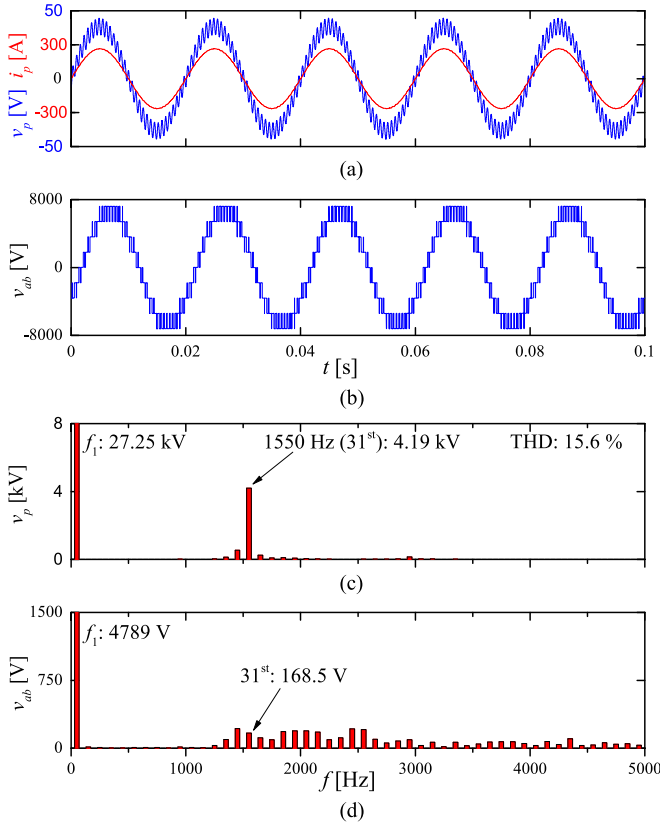


Fig. 7. Simulation result of PS-PWM, (a) waveforms of  $v_p$  and  $i_p$ , (b) waveform of  $v_{ab}$ , (c) spectrum of  $v_p$ , (d) spectrum of  $v_{ab}$ .

the control objective for a master controller [see Fig. 6(a)]. Here,  $L$  and  $r$  stand for the leakage inductance and resistance of the transformer, as seen from one of the secondary windings. The voltage  $v_{dc}$  is the artificial total dc-link voltage. Note that the unified virtual converter is based on assumptions: the four interleaved 4QCs have identical circuits and generally the 4QCs equally share the traction load so that assuming  $v_{dc} = v_{dc1} = v_{dc2}$ , similar to  $M_1 = M_2 = \dots = M_k = M$  mentioned before. The master controller handles the line current of the locomotive  $i_p$ , while synchronizing it with  $v_p$  through regulating the composite voltage  $v_{ab}$  as a SHE-PWM pattern. A standard second-order generalized integrator phase-locked loop (SOGI-PLL) is used to synchronize with the supply voltage  $v_p$ . A standard PI controller is used to regulate  $v_{dc}$  generating the reference

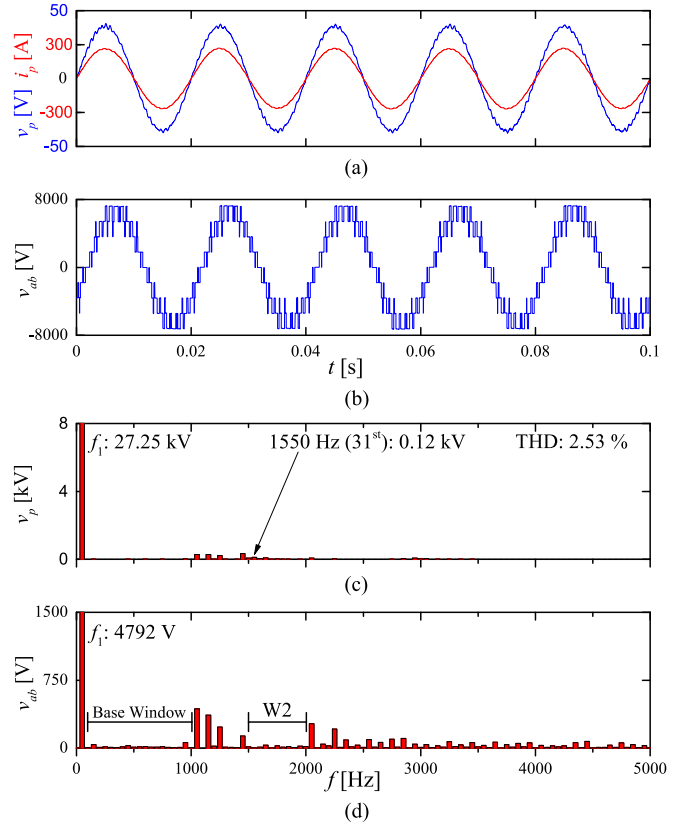


Fig. 8. Simulation result of windowed SHE-PWM: (a) waveforms of  $v_p$  and  $i_p$ , (b) waveform of  $v_{ab}$ , (c) spectrum of  $v_p$ , (d) spectrum of  $v_{ab}$ .

current  $i_{pd}^*$ . A  $dq$ -based single-phase current controller, that uses an improved orthogonal signal generation (OSG) method adopted from [30], synthesizes the modulation index  $M$  and phase angle  $\theta$  of the target composite voltage in order to generate the SHE pattern [28], [31].

The implementation of the windowed SHE-PWM is presented in Fig. 6(b). The proposed SHE pattern is defined as a function with three parameters:  $SHE(W, M, \theta)$ . Conventionally,  $M$  and  $\theta$  are used to read the SHE look-up table that generates the switching signals for the 4QCs [28]. An additional parameter  $W \in (1, 2, \dots, 5)$ , for resonance identification (Res. ID), is introduced to address the resonant frequency variation. When the resonant frequency is identified in the range of  $Wj$  ( $j \in (1, 2, \dots, 5)$ ),  $W$  is set to  $j$  so that  $Wj$  is selected as the moving window.<sup>2</sup> According to operational data and measurement experience in field the TPSSs, the resonant frequency remains constant when the locomotive runs inside a same supply section so that the window changes infrequently. Another issue that should be noted is that when using the SHE-PWM, the four 4QCs have different switching patterns during a fundamental period. To avoid the potentially unbalanced thermal

<sup>2</sup>The extremum value of the ratio  $\frac{v_p(j\omega)}{v_{ab}(j\omega)}$  or  $\frac{v_p(j\omega)}{i_p(j\omega)}$  can be used to identify the resonant frequency, since these values reflect the harmonic amplification. An on-line resonance identification method was documented in detail in [15]. Such methods are out of the scope of this work.

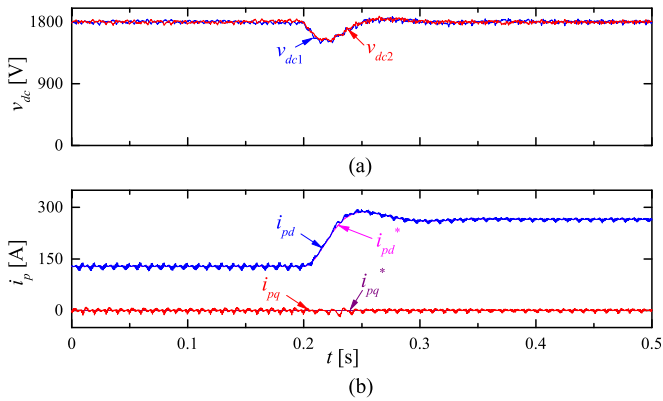


Fig. 9. Step change of the output power from half to full of the rated one: (a) waveforms of dc-link voltages, (b) waveforms of ac-side current.

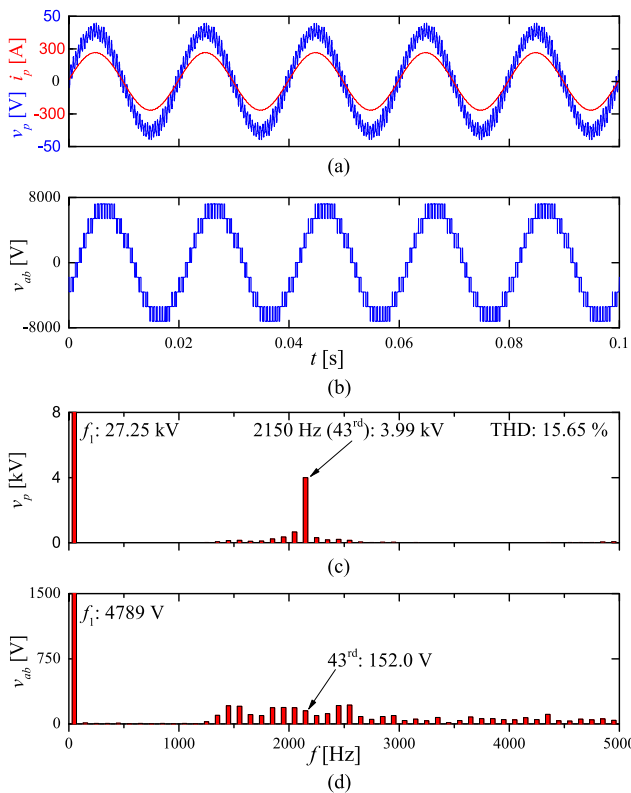


Fig. 10. Simulation result of PS-PWM, (a) waveforms of  $v_p$  and  $i_p$ , (b) waveform of  $v_{ab}$ , (c) spectrum of  $v_p$ , (d) spectrum of  $v_{ab}$ .

distribution, the order of the 4QCs is rotated every fundamental period along with  $\theta$ .

## V. RESULTS

In this section, simulation and experimental results, necessary to validate the effectiveness and the feasibility of the windowed SHE-PWM of interleaved 4QCs for resonance suppression, are presented.

### A. Comparative Simulation Study

The coupling system of the TPSS and the locomotive is modeled through MATLAB/Simulink. The locomotive model,

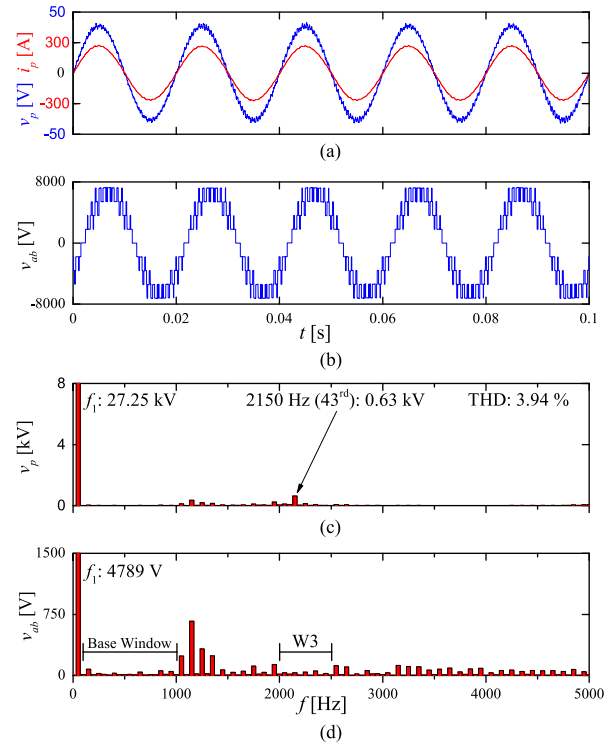


Fig. 11. Simulation result of windowed SHE-PWM: (a) waveforms of  $v_p$  and  $i_p$ , (b) waveform of  $v_{ab}$ , (c) spectrum of  $v_p$ , (d) spectrum of  $v_{ab}$ .

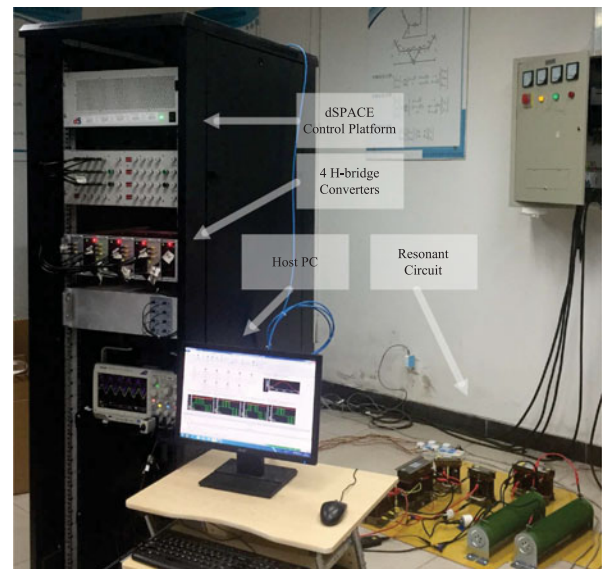


Fig. 12. Laboratory prototype: (a) photo of the overall prototype, (b) equivalent circuit diagram of the resonant circuit.

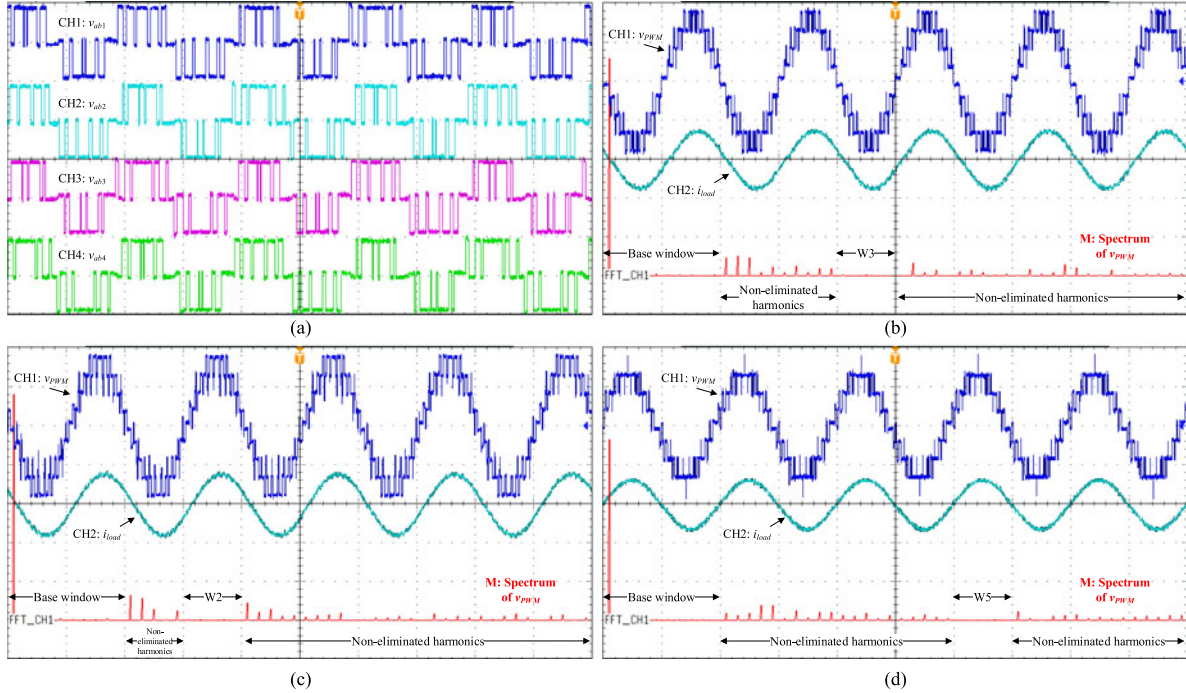


Fig. 13. Experimental result of windowed SHE-PWM: (a)–(b)  $W3$ ,  $M = 0.71$ , SHE patterns of the four H-bridge voltages,  $v_{abi}$ , waveform and spectrum of the combined voltage,  $v_{PWM}$  and waveform of the load current,  $i_{load}$ , (c)–(d) waveforms and spectra for  $W2$ ,  $M = 0.74$  and  $W5$ ,  $M = 0.6$ . 50 V/div for  $v_{abi}$ , 100 V/div for  $v_{PWM}$ , 10 A/div for  $i_{load}$  and 20 V/div-y, 500 Hz/div-x for spectrum.

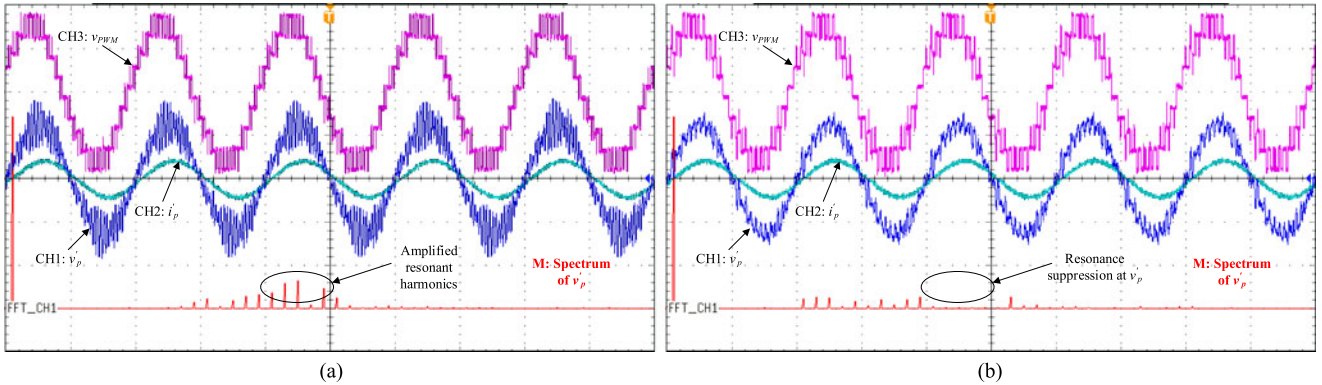


Fig. 14. Experimental result on the resonant circuit: (a) PS-PWM with 250 Hz carrier frequency, (b) windowed SHE-PWM with  $W3$ ,  $M = 0.71$ . CH1:  $v_p$ , 100 V/div, CH2:  $i_p$ , 20 A/div, CH3:  $v_{PWM}$ , 100 V/div, M: FFT for CH3, 20 V/div-y, 500 Hz/div-x.

including the on-board transformer and four interleaved 4QCs, is based on the configuration of Fig. 2 and its electrical parameters are listed in Table II. The inverters and motors are seen as resistive loads governed by the dc-link voltage and output power. The double-track T-R+NF TPSS model is developed according to the ESS and the feeding network parameters of Appendixes A and B. Simulation results of the windowed SHE-PWM are presented and compared with those of PS-PWM (250 Hz carrier frequency).

1) *Test1 24 km Section, W2*: A first test is executed on a 24-km-long TPSS section model. Steady-state simulation results of PS-PWM and windowed SHE-PWM are given in Figs. 7 and 8, respectively, when the locomotive model operated at rated power.

Using the conventional PS-PWM, a resonance occurs and the pantograph voltage  $v_p$  is distorted seriously, as shown in Fig. 7(a). According to Fig. 7(b) and (d), the combined pulse voltage  $v_{ab}$  contains a sideband harmonic of 1550 Hz (31st), 168.5 V (3.5% of fundamental) which coincides with the resonant frequency stimulating the TPSS resonance. Consequently, as shown in Fig. 7(c), the 31st harmonic is amplified to 4.19 kV in  $v_p$  and the total harmonic distortion (THD) of this supply voltage increases to 15.6%. Furthermore, harmonics near the 31st are amplified as well because of the relatively high impedance values of the frequencies close to the resonant frequency.

The resonance is suppressed by adopting the windowed SHE-PWM with the moving window on  $W2$ . As shown in Fig. 8(a),  $v_p$  is significantly less distorted than that of PS-PWM. Fig. 8(b)

TABLE III  
SPECTRUM ANALYSIS OF  $v_p'$  FOR PS-PWM AND WINDOWED SHE-PWM

$f$ (Hz)	50	1750	1850	1950	2050	2150	2250	2350	2450	2550	2650	2750	THD
$\S v_p'$ (V, rms)	88.24	3.69	5.71	6.16	<b>7.53</b>	<b>11.50</b>	<b>12.56</b>	<b>1.72</b>	<b>9.24</b>	4.74	1.12	0.41	27.18 %
$\dagger v_p'$ (V, rms)	88.49	1.53	4.11	5.03	<b>0.75</b>	<b>0.32</b>	<b>0.35</b>	<b>0.43</b>	<b>0.25</b>	0.41	5.08	1.2	15.05 %

$\S$ : PS-PWM,  $\dagger$ : Windowed SHE-PWM

and (d) provides the waveform and spectrum of  $v_{ab}$  in which the harmonics of both base window (up to 1000 Hz) and moving window (from 1500 to 2000 Hz) are nearly completely eliminated. Although some harmonics out of those ranges are generated, they are at uncritical frequencies and, thus, the spectrum of Fig. 8(c) contains few harmonics out of the base and moving windows. The THD of  $v_p$  decreases to only 2.53%.

Additionally, the pantograph current  $i_p$  waveforms of both Figs. 7(a) and 8(a) are sinusoidal and in phase with  $v_p$ . Using the proposed SHE-PWM with W2, a step change in the output power from half to full of the rated one is shown in Fig. 9. The dc-link voltages [see Fig. 9(a)] and ac-side current [see Fig. 9(b)] take about 125 ms to reach their new equilibrium points, so that both steady state and dynamic performances of the controller are verified.

2) *Test2 14 km Section, W3*: A second test is executed on a 14-km-long TPSS section model. Similarly, steady-state simulation results of PS-PWM and windowed SHE-PWM with the moving window on W3 are given in Figs. 10 and 11, respectively, when the locomotive model operated at rated power.

A higher frequency (2150 Hz, 43rd) resonance occurs in the shorter TPSS section, when using the PS-PWM. Fig. 10(a) and (c) shows that  $v_p$  is severely distorted and rich in 43rd harmonic (3.99 kV). The THD of  $v_p$  reaches 15.65%. The waveform and spectrum of  $v_{ab}$ , given in Fig. 10(b) and (d), are similar to those of the former test since the fixed PWM. In this case, another sideband (152.0 V, 43rd) of  $v_{ab}$  stimulates the resonance.

The application of the windowed SHE-PWM suppresses the resonance. In this case, the moving window is on W3 performing different switching pattern as shown in Fig. 11(b) and (d). As a result,  $v_p$  is again less distorted, contains few harmonics and has a largely decreased THD of 3.94%, see Fig. 11(a) and (c).

In this test, although the resonant harmonic is eliminated effectively through the proposed SHE-PWM, there exists a certain amount of resonant harmonic in  $v_p$  [see Fig. 11(c)]. This is mainly due to the extremely high impedance at the resonant frequency. In practice, the system parameters are affected by some nonlinear factors, especially the skin effect of the resistance of the transmission lines. For time-domain simulation purposes, fundamental frequency parameters are provided in Tables V and VI. Thus, the real damping of the system in high-frequency range (including the resonant frequency) will be higher than that of the simulation model and a better harmonic performance of the proposed SHE-PWM can be expected.

It should be noted that the closed-loop implementation of SHE-PWM introduces some small low-order harmonics due to the current tracking oscillations of the controller. These are

affected by the time-constant of the closed-loop control and achieving complete elimination has detrimental effects to the dynamic response of the controller. Even with the presence of such harmonics, the THD of the voltage remains low and the harmonics within the two windows are eliminated effectively for the purpose of resonance suppression.

### B. Experimental Verification of the Windowed SHE-PWM

The windowed SHE-PWM method has been further validated on an experimental prototype, consisting of four H-bridge converters and a resonant circuit, as shown in Fig. 12(a), controlled with a dSPACE1007 platform. First, solutions of the windowed SHE-PWM are tested by four H-bridge converters with a normal RL load, then, the resonance suppression performance of the proposed method is evaluated by applying the SHE voltage on a resonant circuit and comparing with PS-PWM.

1) *Verification of the Solutions of Windowed SHE-PWM*: Using W3,  $M = 0.71$ , the SHE patterns of the four H-bridges are presented in Fig. 13(a), and the waveform and spectrum of the combined voltage  $v_{PWM}$  are given in Fig. 13(b). It should be noted that  $v_{PWM}$  is generated by connecting the four outputs of the H-bridges in series as a five-winding transformer is not readily in our laboratories. Harmonics in the base window (up to 1000 Hz) and the moving window (W3, from 2000 to 2500 Hz) are completely eliminated. The three-level voltages of the H-bridges have five transitions per QW and the patterns are rotated among the bridges along the fundamental period. Similar experimental results of other windows with different modulation indexes are given in Fig. 13(c) and (d). The experimental results show that the proposed method tightly control the harmonics in the windows providing potentially a capability to avoid some resonant frequencies.

2) *Resonance Suppression Performance of the Windowed SHE-PWM*: To validate the resonance suppression capability of the proposed method, a simplified model of the distributed locomotive-TPSS coupling impedance system is constructed using an RLC resonant circuit, as shown in Fig. 12(b). On the network side,  $Z_s$ ,  $Z_l$ , and  $G_l$  are two 5.5 mH reactors and 0.67  $\mu$ F capacitor (with their parasitic parameters), standing for the equivalent impedance in the ESS, the line impedance and line to ground admittance of the feeding lines, respectively. A 14.3- $\Omega$  power resistor  $r_o$  is connected in the circuit to consume the power and then protect all the elements. On the locomotive side,  $Z'_L$  is a 21 mH reactor (with parasitic resistance) that represents the impedance of the transformer on-board the train.

TABLE IV  
ELECTRICAL PARAMETERS OF ESS

(a) Grid		
Parameter	Description	Value
$S_N$	Rated capacity	1500 MVA
$V_N$	Rated line-to-line voltage	110 kV
$X/R$	Ratio between reactance and resistance	7
(b) Transformer		
Parameter	Description	Value
$S_N$	Rated capacity	31.5 MVA
$N$	Turns ratio	110 kV : 27.5 kV
$V_{SC}$	Short-circuit voltage	10.5%
$P_{cu}$	Rated loss	75 kW

The combined PWM voltage  $v_{PWM}$  is applied to the circuit as a harmonic stimulation; and the voltage on the terminal between the two sides  $v'_p$  is measured as an analog of the response on the pantograph.

When PS-PWM is applied, as shown in Fig. 14(a), the waveform of  $v'_p$  is distorted severely. Harmonics between 2000 and 2500 Hz in  $v'_p$  are amplified apparently, as the sidebands in this frequency range of  $v_{PWM}$  coincide with the resonant frequency of the circuit. Although the fundamental of  $v'_p$  is just 88 V, rms, the amplified resonant harmonics raise up the peak of  $v'_p$  to 180 V. Alternatively, as shown in Fig. 14(b), adopting the windowed SHE-PWM with W3, the waveform of  $v'_p$  is much less distorted than that of PS-PWM case. The resonant harmonics with large amplitudes in  $v'_p$  disappeared, since the selected window covers the resonant frequency range so that  $v_{PWM}$  does not provide the harmonic stimulation within this range. Consequently, the peak of  $v'_p$  decreases to only 140 V (22% reduction to PS-PWM). A comparative analysis of  $v'_p$  spectra of Fig. 14(a) and (b) is summarized in Table III. Using PS-PWM, harmonics in the range from 2000 to 2500 Hz (except the 2350 Hz) are more than 7.5 V, rms, particularly, the harmonic of 2250 Hz goes to 12.65 V, rms, 14.2% of the fundamental; using windowed SHE-PWM, on the contrary, harmonics in that range are no more than 0.75 V, rms, the THD decreases by 12.13%. Some noneliminated harmonics of the windowed SHE-PWM close to the resonant frequency range exist, but their amplitudes are relatively small, generally lower than the counterparts of PS-PWM.

It should be noted that the equivalent circuit consisting of lumped elements is a simplified model for the real distributed system. The frequency response of the circuit is affected by the accuracy, nonlinearity, frequency variation of the parameters of the  $RLC$  elements. Comparing with the simulation as well as the measurements in real applications, the harmonic amplification of the experimental equivalent circuit is not extremely high at the resonant frequency range and it attenuates slow. However, the experimental equivalent circuit provided a resonant point for testing and the results show that when some sidebands of PS-PWM coincide with the resonant frequency stimulating the

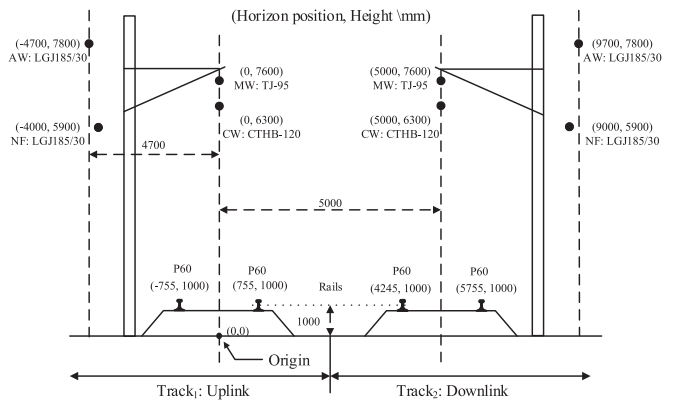


Fig. 15. Typical cross section of a double track T-R+NF feeding network. CW: contact wire, MW: messenger wire, NF: negative feeder, AW: auxiliary wire.

resonance, the windowed SHE-PWM can be an alternative to effectively suppress the resonance.

## VI. CONCLUSION

A windowed SHE-PWM method is proposed in this paper for the purpose of TPSS resonance suppression. The proposed modulation scheme covers a low-frequency range as well as a window within the range of the potential resonant frequency in a TPSS section, while keeping a desired low switching frequency of the traction converters. Thanks to the proper selection of the windows and the relaxations in the formulation of the SHE-PWM problem, a wide range of continuous solutions, necessary for the closed-loop control, can be calculated and used to address the resonant frequency variation. A simulation comparison between the windowed SHE-PWM and the conventional PS-PWM proves that the windowed SHE-PWM is an effective alternative to the PS-PWM for the purpose of resonance suppression. The solutions of the proposed windowed SHE-PWM are verified experimentally with the resonance suppression performance of the proposed method evaluated on an equivalent resonant circuit and compared with PS-PWM. Both simulations and experiments validate the effectiveness and feasibility of the proposed method.

The windowed SHE-PWM can be readily expanded for other locomotive topologies. For instance, one can design a  $k = 6$  and  $N = 7$  windowed SHE-PWM problem for a locomotive with six interleaved H-bridge 4QCs with 350-Hz carrier frequency. A similar approach can also be used in locomotives with different 4QC topologies, for example, reformulating (4) and (5) as five-level waveforms for single-phase three-level NPC 4QCs. Despite the large computational requirements of the windowed SHE-PWM, all the formulations of the problem will be precalculated offline. Therefore, the proposed method is flexible and easy-to-implement.

## APPENDIX A MODELING OF THE ESS

The core of the ESS is the Vv transformer which commonly consists of two single-phase transformers. Besides, the

TABLE V  
SELF- AND MUTUAL-IMPEDANCE MATRIX OF THE TRANSMISSION LINES,  $\Omega/\text{KM}$

	T1	R1	NF1	T2	R2	NF2
T1	0.1057 + j0.4874	0.0497 + j0.3086	0.0488 + j0.3567	0.0491 + j0.2992	0.0495 + j0.2903	0.0480 + j0.2838
R1	0.0497 + j0.3086	0.1068 + j0.5409	0.0490 + j0.3140	0.0495 + j0.2903	0.0498 + j0.3284	0.0485 + j0.2850
NF1	0.0488 + j0.3567	0.0490 + j0.3140	0.2066 + j0.7320	0.0480 + j0.2838	0.0485 + j0.2850	0.0473 + j0.2726
T2	0.0491 + j0.2992	0.0495 + j0.2903	0.0480 + j0.2838	0.1057 + j0.4874	0.0497 + j0.3086	0.0488 + j0.3567
R2	0.0495 + j0.2903	0.0498 + j0.3284	0.0485 + j0.2850	0.0497 + j0.3086	0.1068 + j0.5408	0.0490 + j0.3140
NF2	0.0480 + j0.2838	0.0485 + j0.2850	0.0473 + j0.2726	0.0488 + j0.3567	0.0490 + j0.3140	0.2066 + j0.7320

TABLE VI  
SELF- AND MUTUAL-ADMITTANCE MATRIX OF THE TRANSMISSION LINES,  $10^{-5} \text{ S/KM}$

	T1	R1	NF1	T2	R2	NF2
T1	0.0000 + j0.5643	0.0000 - j0.0567	0.0000 - j0.1057	0.0000 - j0.0940	0.0000 - j0.0256	0.0000 - j0.0135
R1	0.0000 - j0.0567	1000.0 + j1.0403	0.0000 - j0.0209	0.0000 - j0.0256	0.0000 - j0.0393	0.0000 - j0.0043
NF1	0.0000 - j0.1057	0.0000 - j0.0209	0.0000 + j0.2706	0.0000 - j0.0135	0.0000 - j0.0043	0.0000 - j0.0022
T2	0.0000 - j0.0940	0.0000 - j0.0256	0.0000 - j0.0135	0.0000 + j0.5643	0.0000 - j0.0567	0.0000 - j0.1057
R2	0.0000 - j0.0256	0.0000 - j0.0393	0.0000 - j0.0043	0.0000 - j0.0567	1000.0 + j1.0403	0.0000 - j0.0209
NF2	0.0000 - j0.0135	0.0000 - j0.0043	0.0000 - j0.0022	0.0000 - j0.1057	0.0000 - j0.0209	0.0000 + j0.2706

external three-phase grid should be modeled in the ESS referring to three-phase Thévenin theorem. In this study, 110-kV grid and 31.5-MVA single-phase transformer are chosen for modeling the ESS, as shown in Table IV(a) and (b), respectively.

#### APPENDIX B

##### MODELING OF THE FEEDING NETWORK

Fig. 15 shows the cross section of the double-track T-R+NF feeding network studied in this paper. The feeding network is a paralleled multiconductor transmission line structure with distributed parameters of the conductors. It is generally modeled as a chain circuit model described by impedance and admittance matrices of the conductors per length unit, as documented in available technical literature, e.g., [19], [21], [32], [33]. To get a simplified model, some conductors should be combined electrically by using Carson equation resulting in a six-line structure. For each track, there are three lines: T (including CW, MW and AW), R (including two running rails) and NF as shown in Fig. 1. According to the geometrical positions and types of the paralleled conductors of Fig. 15, the  $6 \times 6$  impedance and admittance matrices are calculated in Tables V and VI, respectively.

#### REFERENCES

- [1] K. Sato, M. Yoshizawa, and T. Fukushima, "Traction systems using power electronics for Shinkansen high-speed electric multiple units," in *Proc. Int. Power Electron. Conf.*, Jun. 2010, pp. 2859–2866.
- [2] T. Uzuka, "Faster than a speeding bullet: An overview of Japanese high-speed rail technology and electrification," *IEEE Electrific. Mag.*, vol. 1, no. 1, pp. 11–20, Sep. 2013.
- [3] X. Huang, L. Zhang, M. He, X. You, and Q. Zheng, "Power electronics used in Chinese electric locomotives," in *Proc. IEEE Int. Power Electron. Motion Control Conf.*, May 2009, pp. 1196–1200.
- [4] H.-S. Song, R. Keil, P. Mutschler, J. van der Weem, and K. Nam, "Advanced control scheme for a single-phase PWM rectifier in traction applications," in *Proc. Annu. Meeting, Ind. Appl. Conf.*, vol. 3, Oct. 2003, pp. 1558–1565.
- [5] G. G. Balazs, M. Horvath, I. Schmidt, and P. Kiss, "Examination of new current control methods for modern PWM controlled AC electric locomotives," in *Proc. IET Int. Conf. Power Electron., Mach. Drives*, Mar. 2012, pp. 1–5.
- [6] S. Gazafzudi, A. Tabakhpour Langerudy, E. Fuchs, and K. Al-Haddad, "Power quality issues in railway electrification: A comprehensive perspective," *IEEE Trans. Ind. Electron.*, vol. 62, no. 5, pp. 3081–3090, May 2015.
- [7] W. Song, J. Ma, L. Zhou, and X. Feng, "Deadbeat predictive power control of single-phase three-level neutral-point-clamped converters using space-vector modulation for electric railway traction," *IEEE Trans. Power Electron.*, vol. 31, no. 1, pp. 721–732, Feb. 2015.
- [8] L. He, J. Xiong, H. Ouyang, P. Zhang, and K. Zhang, "High-performance indirect current control scheme for railway traction four-quadrant converters," *IEEE Trans. Ind. Electron.*, vol. 61, no. 12, pp. 6645–6654, Dec. 2014.
- [9] A. Steimel, "Electric railway traction in Europe," *IEEE Ind. Appl. Mag.*, vol. 2, no. 6, pp. 6–17, Nov. 1996.
- [10] S. Kejian, W. Mingli, V. Agelidis, and W. Hui, "Line current harmonics of three-level neutral-point-clamped electric multiple unit rectifiers: Analysis, simulation and testing," *IET Power Electron.*, vol. 7, no. 7, pp. 1850–1858, Jul. 2014.
- [11] X. Chu, F. Lin, and Z. Yang, "The analysis of time-varying resonances in the power supply line of high speed trains," in *Proc. Int. Power Electron. Conf.*, May 2014, pp. 1322–1327.
- [12] Y. Xiong, Y. Zhang, and D. Tong, "Analysis on harmonic current of electrified railway traction network based on multi-port reduced-order model," in *Proc. China Int. Conf. Elect. Distrib.*, Sep. 2012, pp. 1–6.
- [13] H. Hu, Z. He, and S. Gao, "Passive filter design for China high-speed railway with considering harmonic resonance and characteristic harmonics," *IEEE Trans. Power Del.*, vol. 30, no. 1, pp. 505–514, Feb. 2015.
- [14] J. Holtz and H. J. Keli, "The propagation of harmonic currents generated by inverter-fed locomotives in the distributed overhead supply system," *IEEE Trans. Power Electron.*, vol. 4, no. 2, pp. 168–174, Apr. 1989.
- [15] J. Holtz and J. O. Krah, "On-line identification of the resonance conditions in the overhead supply line of electric railways," *Archiv Fr Elektrotechnik*, vol. 74, no. 1, pp. 99–106, 1990.
- [16] J. Holtz and J. O. Krah, "Adaptive optimal pulse-width modulation for the line-side converter of electric locomotives," *IEEE Trans. Power Electron.*, vol. 7, no. 1, pp. 205–211, Jan. 1992.

- [17] J. O. Krah and J. Holtz, "Total compensation of line-side switching harmonics in converter-fed ac locomotives," *IEEE Trans. Ind. Appl.*, vol. 31, no. 6, pp. 1264–1273, Nov. 1995.
- [18] H. Cui, W. Song, H. Fang, X. Ge, and X. Feng, "Resonant harmonic elimination pulse width modulation-based high-frequency resonance suppression of high-speed railways," *IET Power Electron.*, vol. 8, no. 5, pp. 735–742, May 2015.
- [19] H. Lee, C. Lee, G. Jang, and S. Hyuk Kwon, "Harmonic analysis of the Korean high-speed railway using the eight-port representation model," *IEEE Trans. Power Del.*, vol. 21, no. 2, pp. 979–986, Apr. 2006.
- [20] A. Dolar, M. Gualdoni, and S. Leva, "Impact of high-voltage primary supply lines in the  $2 \times 25$  kv—50 Hz railway system on the equivalent impedance at pantograph terminals," *IEEE Trans. Power Del.*, vol. 27, no. 1, pp. 164–175, Jan. 2012.
- [21] Z. He, H. Hu, Y. Zhang, and S. Gao, "Harmonic resonance assessment to traction power-supply system considering train model in china high-speed railway," *IEEE Trans. Power Del.*, vol. 29, no. 4, pp. 1735–1743, Aug. 2014.
- [22] H. Lee, G. Kim, S. Oh, and C. Lee, "Optimal design for power quality of electric railway," in *Proc. Int. Joint Conf. SICE-ICASE*, Oct. 2006, pp. 3864–3869.
- [23] W. Mingli, Z. Huang, S. Yang, Z. Chu, and M. Liu, "Suppression device for higher-order harmonic resonance and transient over-voltage in traction network," CHN Patent: ZL 2007 1 0120620.9, Sep. 2007.
- [24] T. Maeda, T. Watanabe, A. Mechi, T. Shiota, and K. Iida, "A hybrid single-phase power active filter for high order harmonics compensation in converter-fed high speed trains," in *Proc. Conf. Power Convers.*, Aug. 1997, vol. 2, pp. 711–717.
- [25] A. Bueno, J. M. Aller, J. A. Restrepo, R. Harley, and T. G. Habetler, "Harmonic and unbalance compensation based on direct power control for electric railway systems," *IEEE Trans. Power Electron.*, vol. 28, no. 12, pp. 5823–5831, Dec. 2013.
- [26] G. Konstantinou, V. G. Agelidis, and J. Pou, "Interleaved selective harmonic elimination pwm for single-phase rectifiers in traction applications," in *Proc. IEEE Annu. Conf. Ind. Electron. Soc.*, Nov. 2013, pp. 930–935.
- [27] H. S. Patel and R. G. Hoft, "Generalized techniques of harmonic elimination and voltage control in thyristor inverters: Part I—Harmonic elimination," *IEEE Trans. Ind. Appl.*, vol. IA-9, no. 3, pp. 310–317, May 1973.
- [28] M. S. A. Dahidah, G. Konstantinou, and V. G. Agelidis, "A review of multilevel selective harmonic elimination PWM: Formulations, solving algorithms, implementation and applications," *IEEE Trans. Power Electron.*, vol. 30, no. 8, pp. 4091–4106, Aug. 2015.
- [29] G. Konstantinou, V. G. Agelidis, and J. Pou, "Theoretical considerations for single-phase interleaved converters operated with SHE-PWM," *IEEE Power Electron. Lett.*, vol. 29, no. 10, pp. 5124–5128, Oct. 2014.
- [30] M. Ebrahimi, S. A. Khajehoddin, and M. Karimi-Ghartemani, "Fast and robust single-phase DQ current controller for smart inverter applications," *IEEE Trans. Power Electron.*, vol. 31, no. 5, pp. 3968–3976, May 2016.
- [31] U. A. Miranda, L. G. B. Rolim, and M. Aredes, "A DQ synchronous reference frame current control for single-phase converters," in *Proc. IEEE Power Electron. Spec. Conf.*, Jun. 2005, pp. 1377–1381.
- [32] W. Mingli, C. Roberts, and S. Hillmans, "Modelling of ac feeding systems of electric railways based on a uniform multi-conductor chain circuit topology," in *Proc. IET Conf. Railway Traction Syst.*, Apr. 2010, pp. 1–5.
- [33] A. Mariscotti, P. Pozzobon, and M. Vanti, "Distribution of the traction return current in at electric railway systems," *IEEE Trans. Power Del.*, vol. 20, no. 3, pp. 2119–2128, Jul. 2005.



**Kejian Song** was born in Hunan province, China, on January 8, 1988. He received the B.Sc. degree in electrical engineering from Shaoyang University, Shaoyang, China, in 2010 and the M.Sc. degree in electrical engineering from Beijing Jiaotong University (BJTU), Beijing, China in 2012, where he is currently working toward the Ph.D. degree in electrical engineering. From December 2014 to December 2015, he was with the Australia Energy Research Institute, UNSW Australia, Sydney, as an exchanged Ph.D. student sponsored by China Scholarship

Council.

His research interests include modulation methods and control strategies for traction converters and electric power quality of traction power supply systems.



**Georgios Konstantinou** (S'08–M'11) received the B.Eng. degree in electrical and computer engineering from the Aristotle University of Thessaloniki, Thessaloniki, Greece, in 2007, and the Ph.D. degree in electrical engineering from UNSW Australia, Sydney, in 2012.

From 2012 to 2015, he was a Research Associate at UNSW Australia where he is currently a Lecturer with the School of Electrical Engineering and Telecommunications. His main research interests include hybrid and modular multilevel converters, power electronics for HVDC and energy storage applications, pulse width modulation, and selective harmonic elimination techniques for power electronics.



**Wu Mingli** was born in Hebei province, China, on November 11, 1971. He received the B.Sc. and M.Sc. degrees in electrical engineering from Southwest Jiaotong University, Chengdu, China, in 1993 and 1996, respectively, and the Ph.D. degree in electrical engineering from Beijing Jiaotong University (BJTU), Beijing, China, in 2006.

Since 2008, he has been a Professor in the School of Electrical Engineering, BJTU. His research interests include power supply for electric railways, digital simulation of power systems, and electric power

quality.



**Pablo Acuna** (M'12) received the B.S. degree in electronics engineering, the electronics engineering professional degree, and the Ph.D. degree in electrical engineering from the University of Concepción, Chile, in 2004, 2007, and 2013 respectively.

He is currently a Research Associate at the School of Electrical Engineering and Telecommunications, University of New South Wales, Sydney, Australia. His research interests include electrical power conversion systems and its applications to industry, transportation and utility.



**Ricardo P. Aguilera** (S'01–M'12) received the B.Sc. degree in electrical engineering from the Universidad de Antofagasta, Chile, in 2003, the M.Sc. degree in electronics engineering from the Universidad Tecnica Federico Santa Maria, Chile, in 2007, and the Ph.D. degree in electrical engineering from The University of Newcastle, Australia, in 2012.

From 2012 to 2013, he was a Research Academic at UoN, where he was part of the Centre for Complex Dynamic Systems and Control. From 2014 to 2016, he was a Senior Research Associate at The University of New South Wales (UNSW), Australia, where he was part of the Australian Energy Research Institute. Since September 2016, he has been with the School of Electrical, Mechanical and Mechatronic Systems, University of Technology Sydney, Australia, where he currently holds a Lecturer position. His main research interests include power electronics, renewable energy, and theoretical and practical aspects on model predictive control.



**Vassilios G. Agelidis** (S'89–M'91–SM'00–F'16) was born in Serres, Greece. He received the B.Eng. degree in electrical engineering from the Democritus University of Thrace, Thrace, Greece, in 1988, the M.S. degree in applied science from Concordia University, Montreal, QC, Canada, in 1992, and the Ph.D. degree in electrical engineering from Curtin University, Perth, Australia, in 1997.

He has worked at Curtin University (1993–1999), University of Glasgow, U.K. (2000–2004), Murdoch University, Perth, Australia (2005–2006), the University of Sydney, Australia (2007–2010), and the University of New South Wales (UNSW), Sydney, Australia (2010–2016). He is currently a Professor in the Department of Electrical Engineering, Technical University of Denmark. He received the Advanced Research Fellowship from the U.K.'s Engineering and Physical Sciences Research Council in 2004.

Dr. Agelidis was the Vice-President Operations within the IEEE Power Electronics Society from 2006 to 2007. He was an AdCom Member of the IEEE Power Electronics Society from 2007 to 2009 and the Technical Chair of the 39th IEEE Power Electronics Specialists Conference, Rhodes, Greece, 2008.