

# Wide-Range Adaptive IPT Using Dipole-Coils With a Reflector by Variable Switched Capacitance

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**Abstract**—A dipole-coil-based inductive power transfer (IPT) with a reflector, which first adopts the variable switched capacitance for load power regulation under very wide-range distance variation between transmitter (Tx) and receiver (Rx) coils, is newly proposed. The resonant frequency of the LC tank of the proposed IPT can be appropriately modulated by the variable switched capacitance with reliable zero-voltage-switching (ZVS) operations. Therefore, even though the distance changes very widely, load power can be regulated solely by the variable switched capacitance in the Rx circuit without complicated communication links between the Tx and Rx coils. A detailed static analysis based on a recent imaginary gyrator model and design procedure for the proposed IPT are presented to build a simplified LC resonant tank of the proposed IPT and ZVS condition and to identify applicable distance variation range for constant load power. A prototype of the Tx and Rx coils for 100 W of load power, considering average power consumptions of home appliances, was fabricated and verified by simulations and experiments, which showed that load power was completely regulated to 100 W for 23–70 cm of very wide-range distance variation at a fixed switching frequency of 140 kHz.

**Index Terms**—Dipole coil resonance system (DCRS), inductive power transfer (IPT), load power regulation, reflector, variable switched capacitance, wide-range distance variation between Tx and Rx coils, zero voltage switching (ZVS).

## I. INTRODUCTION

WIRELESS power transfer (WPT) has been widely used in many technologies such as electric vehicles, mobile devices, Internet of things, medical devices, and home appliances by virtue of providing electric power without cumbersome cables, creating clean and uncluttered-looking electronic devices and an inherent way to avoid electrical accidents. Contact- and non-contact-type of WPT systems with less than 5 cm

distance between the transmitter (Tx) and receiver (Rx) are prominent in markets for mobile devices and home appliances. However, as customers require the freedom of using WPT, these conventional types of short-distance WPT are no longer a viable solution to fulfill the requirements of the customers. Thus, numerous WPT technologies have been introduced to transfer a high load power at long distance [1]–[28]. One such candidate, coupled magnetic resonance systems have been developed since their introduction in 2007 [1]–[7]. This system, however, adopts four large resonant coils and operates at several MHz for a very high quality factor ( $\sim 2,000$ ); hence, the system has inherent demerits, which are large voltage stress of resonant capacitors in each coil, inherent bulky and volumetric structures, and hypersensitivity to the surrounding conditions such as temperature, humidity, and human proximity. Radio frequency (RF) and infrared (IR) types of WPT systems may be a solution due to their characteristic straightness from the Tx to the Rx [8]–[13]. However, the RF-type WPT has inherent EMF/EMI problems, low power efficiency, low power density ( $\text{kW/m}^3$ ), and cannot penetrate metal objects [8]–[10]. The IR-type WPT is also incapable of penetrating obstacles, has low power efficiency and density, and requires very precise control to align the Tx and Rx through a straight beam [11]–[13]. On the other hand, inductive power transfer (IPT) systems are known to be suitable for long distance WPT applications; 209 W at 5 m and 11 W at 7 m of long distance wireless power delivery have been achieved by the dipole coil resonance system (DCRS) [14]–[15]. The DCRS adopts long slim-size dipole coils operating at a relatively low switching frequency (several tens of kHz) with a low quality factor ( $\sim 100$ ), which is beneficial to adopt various practical applications with a simple structure and less sensitive characteristic. It was proven that a Tx reflector, which is a metal plate and placed behind the Tx coil, is effective to increase the power efficiency while delivering the same load power [23]. Therefore, IPT based on the DCRS with the Tx reflector is highly applicable to long distance WPT applications with high power transfer capability.

In spite of merits of IPT due to its low quality factor, load characteristics of IPT such as load voltage, load power, and power efficiency inevitably change when the distance  $d$  between Tx and Rx coils varies, i.e., the variation of the coupling factor  $k$ , as shown in Figs. 1 and 2. The tuning methods based on saturable reactors in a Class E inverter were adopted to regulate the load power under  $k$  changes [24]–[25]. However, the dc current of saturable reactors, switching frequency, and duty cycle should

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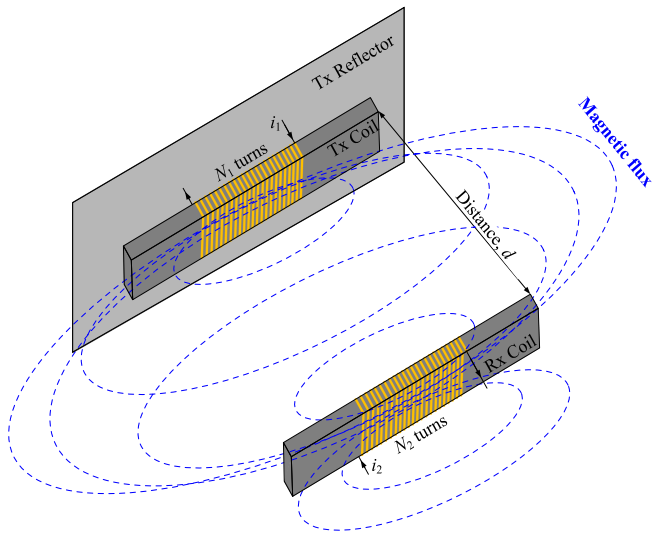


Fig. 1. Overall Tx and Rx coil configuration of the proposed IPT with the Tx reflector.

be precisely controlled not only to regulate load power but also to guarantee zero voltage switching (ZVS) and zero-voltage derivative switching operations of the Class E inverter. In addition, due to high sensitive characteristics of load resistance and distance variations for reliable operation of the Class E inverter, it may not be suitable for practical applications. Additional circuits such as dc–dc converters in Tx and Rx coils, isolation-type feedback control circuits between Tx and Rx coils, and wireless communication links are required to regulate load power, which increases cost and complexity of the whole WPT system [26]–[28].

In this paper, an adaptively controlled variable switched capacitance is first applied to a dipole-coil-based loosely-coupled IPT system with a Tx reflector, which can regulate load power under very wide-range distance variation, as shown in Fig. 3. The equivalent circuit of the proposed IPT can be represented as an LC parallel resonant circuit, as shown in Fig. 5. The equivalent capacitance of the variable switched capacitance can be appropriately modulated, which controls the resonant frequency of the LC tank in the Rx circuit and finally regulates load power. Contrary to the conventional variable switched capacitance circuits [35]–[38], the proposed IPT simply uses two main switches  $S_1$  and  $S_2$  in the Rx rectifier circuit for adaptive control of the variable switched capacitance and one comparator with sensing resistors for ZVS operations of  $S_1$  and  $S_2$ ; hence, the proposed IPT is applicable to the home appliances due to its simple structure and the low cost of the whole system. The validity of the proposed IPT is verified by simulations and experiments, showing a complete load power regulation over the wide-range distance variation.

## II. THEORETICAL CONSIDERATION OF THE VARIABLE SWITCHED CAPACITANCE

It is important to modulate the switching frequency or resonant frequency of the LC tank so that the load characteristics

are appropriately controlled. Switching frequency can be modulated to control the load power when the other parameters are fixed [29]–[31]. However, it may not be easy to satisfy the design goals with the ZVS operation of Tx inverter due to two fixed resonant frequencies of the Tx and Rx coils, which require complicated algorithms and control circuits. In particular, the cumbersome communication links between the Tx and Rx are essential to sense the load voltage and to give Tx control circuit. One of the methods to modulate the resonant frequency of the LC tank is to simply add or remove the capacitors, which are electrically connected or disconnected by the switches, the microcontroller unit (MCU), and additional control circuits [32]–[34]. However, this method has no precise control capability due to its quantized values of each capacitor. Although binary weighted capacitors controlled by MCU may be adopted to control the specific capacitance, it requires a number of additional capacitors and complicated control circuits [34]. On the other hand, the variable switched capacitance becomes a promising solution to modulate the equivalent capacitance and has been widely applied to WPT applications due to its compact size with the high voltage rating of the capacitors, desirable soft-switching operation of main switches, easy applicability to high switching frequency operation [35]–[38]. This variable switched capacitance can be modulated by the switching duty cycle of controlled main switches  $D$ , which results in adaptive change of equivalent capacitance by considering the fundamental components of the voltages and currents, as shown in Fig. 4, where  $v_c$  is the voltage in the parallel capacitor  $C_p$  in Fig. 3,  $v_{c1}$  is the fundamental components of  $v_c$ , and  $v_L$  is the load voltage. Recently, the variable switched capacitance was first applied to LED drivers, which adopt bidirectional switching circuits with ZVS operations of main switches compatible with wide range of switching frequencies [38]. In Fig. 4, equivalent capacitance of the variable switched capacitance with bidirectional switches was theoretically derived by switching duty cycle  $D$  determined by  $v_{gs1}$  and  $v_{gs2}$  as follows [38]:

$$C_v \equiv \frac{C_p}{1 - 2D - \frac{1}{\pi} \sin 2\pi D} \text{ for } 0 \leq D < 0.5. \quad (1)$$

As shown in Fig. 4, the switching waveform of  $v_c$  is determined by  $C_p$ , assuming the other parameters such as  $C_L$ ,  $R_L$ , and  $f_s$  are fixed. From (1), equivalent capacitance  $C_v$  by switching duty cycle  $D$  is derived when the load effect of the diode rectifier is neglected and  $v_c$  is a complete sinusoidal waveform, which corresponds to Fig. 4(c); the peak voltage of  $v_c$  is always less than  $V_L$ , and the diode rectifier operates in discontinuous conduction mode (DCM) [42]–[46]. Contrary to this, the diode rectifier almost operates in continuous conduction mode (CCM) if a very small value of  $C_p$  is used, as shown in Fig. 4(a). The peak voltage of  $v_c$  is abruptly clamped to  $V_L$ , and the waveform of  $v_c$  is nearly rectangular; the equivalent capacitance of Fig. 4(a) no longer matches the theoretical analysis of (1) due to the nonsinusoidal waveform of  $v_c$ . In this case, the conversion ratio of  $\alpha$ , which is the ratio of  $V_c$  and  $V_L$  considering the fundamental components, is nearly 0.9 [42]–[46]. Because the general switching waveform of  $v_c$  has finite charging times of  $t_{c1}$  and  $t_{c2}$ , as shown in Fig. 4(b),  $\alpha$  depends on  $t_{c1}$  and  $t_{c2}$  as

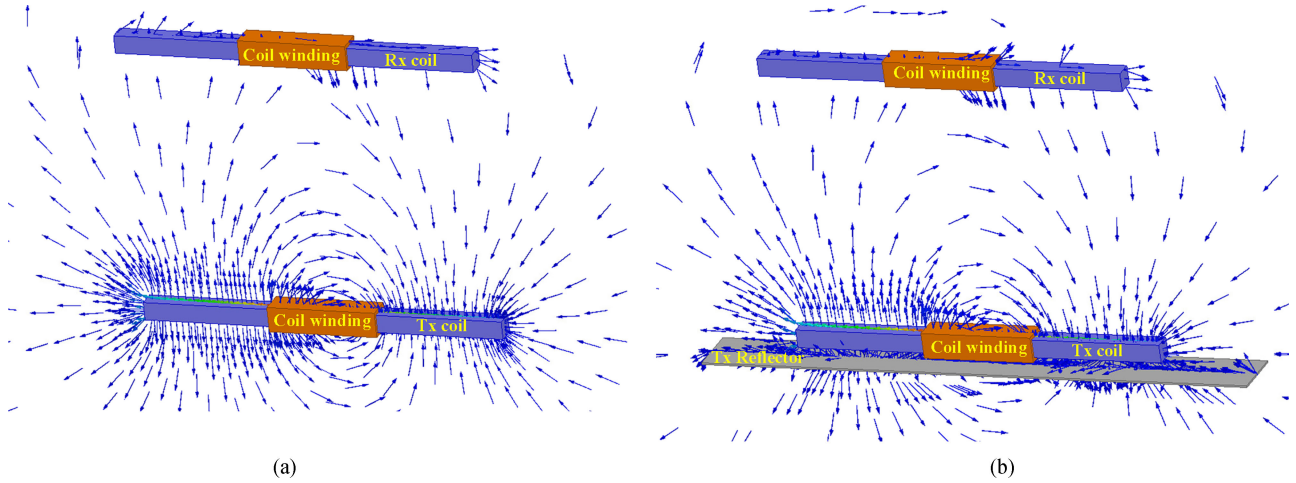


Fig. 2. Simulation results of the magnetic flux vector lines for the proposed IPT performed by 3-D Maxwell simulations, where  $d = 70$  cm,  $I_1 = 10$  A, and  $I_2 = 0$ . (a) Without a Tx reflector. (b) With a Tx reflector.

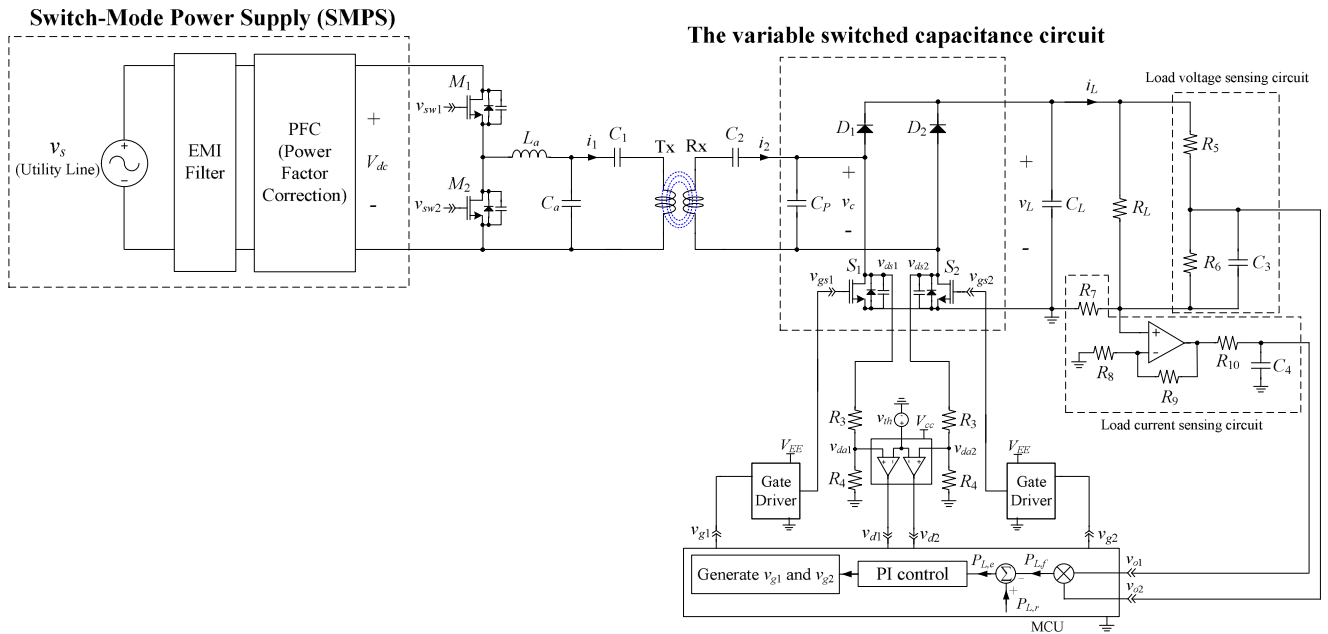


Fig. 3. Overall circuit diagram of the proposed IPT with the switch-mode power supply and the variable switched capacitance.

follows [46]:

$$V_c = \alpha(t_{c1}, t_{c2})V_L, R_e = \alpha^2(t_{c1}, t_{c2})R_L \quad (2)$$

where  $R_e$  is equivalent resistance seen from the diode rectifier.

From (2), it is extremely complicated to find the expression for this highly nonlinear  $\alpha$ , which is the functions of  $t_{c1}$  and  $t_{c2}$  according to analysis; therefore, such an expression can be found only by comparing the experimental results w.r.t. the different cases of  $C_p$ , which will be discussed in detail in Section VI.

### III. STATIC ANALYSIS OF THE PROPOSED IPT

The proposed IPT, as shown in Figs. 1 and 2, is based on conventional slim-size dipole Tx and Rx coils [14]–[15] so that static performance of the variable switched capacitance

for load power regulation is verified. For long distance IPT systems, several Tx and Rx coil structures can be a candidate to be adopted [1]–[22]. Long slim-size dipole coil structures are more preferred than the other coil structures for home appliance applications because dipole coil structures are shaped as line having very small width, which are neither plane nor volumetric structures. Thus, dipole coil structures will be recommended to the home appliances in terms of easily installation under confined spaces. The magnetic field distributions of the proposed IPT for with and without a Tx reflector cases are described in Fig. 2, representing that magnetic flux generated by Tx coil is effectively interlinked to Rx coil. Regarding effect of a reflector, it is not possible to analytically build an explicit modeling of a reflector by quantitative values. Instead, it has been experimentally identified that a Tx reflector adopted behind Tx

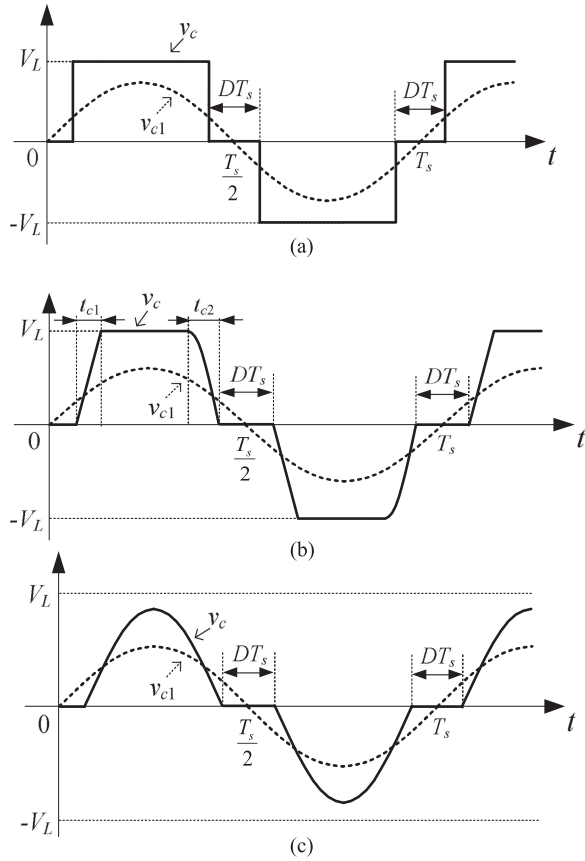


Fig. 4. Switching waveforms of  $v_c$ , depending on the parallel capacitance  $C_p$ . (a) Very small  $C_p$  ( $t_{c1}$  and  $t_{c2} \approx 0$ ), (b) Reasonable  $C_p$ , (c) Very large  $C_p$ .

coil enhances the power efficiency for long distance IPT based on DCRS [23]. As shown in Fig. 2(b), self-inductance of the Tx coil  $L_1$  decreases due to the reduction of leakage magnetic flux behind the Tx coil, i.e., the leakage magnetic flux inside the Tx coil reduces, which is beneficial to reduce core loss of the Tx coil and finally to enhance the power efficiency [23]. As shown in Fig. 3, the switch-mode power supply, which is typically composed of an EMI filter and a power factor correction (PFC), is generally used; hence, an EMI issue caused by high frequency switching operation is no concern, and electric devices connecting to the utility line operate with high power factor (PF) and low total harmonic distortion (THD) to satisfy the international standards [47]–[48]. Input voltage of the asymmetric half-bridge inverter in Fig. 3 is constant dc voltage  $V_{dc}$ , and  $L_a$  and  $C_a$  are adopted to generate a constant source current. Primary-series-secondary-series resonant capacitors  $C_1$  and  $C_2$  are adopted as an example in this paper to nullify the reactance of the Tx and Rx coils, respectively. The other resonant topologies, such as primary-series-secondary-parallel for both voltage and current sources, can be also adopted for the variable switched capacitance, though not shown in this paper [50]. The variable switched capacitance circuit is composed of two main switches  $S_1$  and  $S_2$  and two fast recovery diodes  $D_1$  and  $D_2$  with a lumped parallel capacitor  $C_p$ . Circuit topology of the variable switched capacitance circuit is similar with active

rectifiers [39]–[41]. However, contrary to those conventional active rectifiers [39]–[41], secondary rectifier of the proposed IPT adopts  $C_p$  with an active rectifier circuit so that  $C_p$  is utilized as the variable switched capacitance; hence, the proposed variable switched capacitance circuit requires a small number of components compared to conventional one adopted to versatile LED drivers [38]. Nevertheless, the functionality of the variable switched capacitance is identical to the conventional one, which will be identified in Section IV. To ensure the ZVS operations of  $S_1$  and  $S_2$ , the comparator with sensing resistors is adopted to sense the  $v_{ds1}$  and  $v_{ds2}$ , and to feed  $v_{d1}$  and  $v_{d2}$  to the MCU. The load voltage  $v_L$  and the load current  $i_L$  are sensed by the load voltage and current sensing circuits, and the load capacitor  $C_L$  is connected to the output of the rectifier for smoothing  $v_L$ .

#### A. Load Power $P_L$

The proposed IPT in Fig. 3 can be represented in Fig. 5 by an imaginary gyrator-based circuit modeling, which is a simple and systematic ways to analyze the IPT with graphical procedures [49]. In Fig. 5,  $M$  is mutual inductance, and  $r_1$  and  $r_2$  include the equivalent series resistances (ESRs) of capacitors  $C_1$  and  $C_2$  and core and copper losses of the Tx and Rx coils, respectively. Especially, effect of the Tx reflector causes decrement of  $L_1$  and increment of  $r_1$ , whose variations are adopted throughout this paper [23]. The variable switched capacitance circuit is regarded as  $C_v$  and load resistance  $R_L$  can be represented as equivalent resistance  $R_e$ , as identified from (1) and (2). Assuming that only fundamental components of the voltages and currents are considered and the switching duty cycle of the inverter is 0.5, the output voltage of the asymmetric half-bridge inverter  $V_1$  is determined as follows [42]–[46]:

$$V_1 = \frac{2\sqrt{2}}{\pi} \cdot \frac{V_{dc}}{2} \approx 0.45 V_{dc}. \quad (3)$$

By applying Thevenin's theorem to the left part of the circuit of Fig. 5, an equivalent Thevenin circuit is obtained, as shown in Fig. 6(a), where it is assumed that  $L_1$  and  $C_1$ , and  $L_2$  and  $C_2$  are fully resonated, respectively. Then, the Thevenin voltage source  $V_a$  is derived as follows:

$$V_a = \frac{V_1}{X_a} \quad (4a)$$

$$\because X_a \equiv 1 - \omega_s^2 L_a C_a, f_a \equiv \frac{1}{2\pi\sqrt{L_a C_a}} \quad (4b)$$

$$f_s = f_{r1} = f_{r2} \left( \because f_{r1} \equiv \frac{1}{2\pi\sqrt{L_1 C_1}}, f_{r2} \equiv \frac{1}{2\pi\sqrt{L_2 C_2}} \right) \quad (4c)$$

where  $f_s$  and  $f_a$  are the switching frequency of the inverter and the resonant frequency of  $L_a$  and  $C_a$ , respectively.

According to the gyrator characteristics, the Thevenin voltage source and impedance in Fig. 6(a) can be transformed to the current source  $I_g$  with equivalent inductance  $L_e$  and resistor  $r_{g1}$

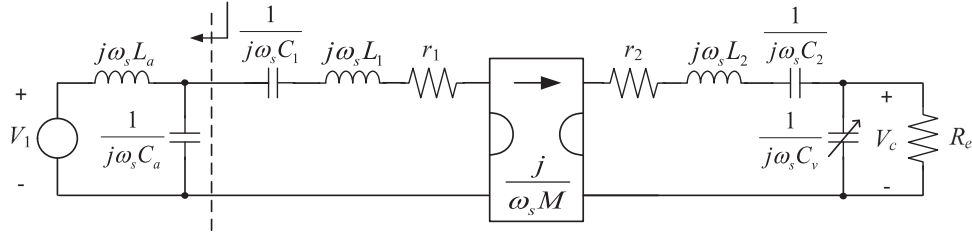


Fig. 5. Simplified equivalent circuit of Fig. 3 with a gyrator, substituting the proposed variable switched capacitance circuit as  $C_v$ .

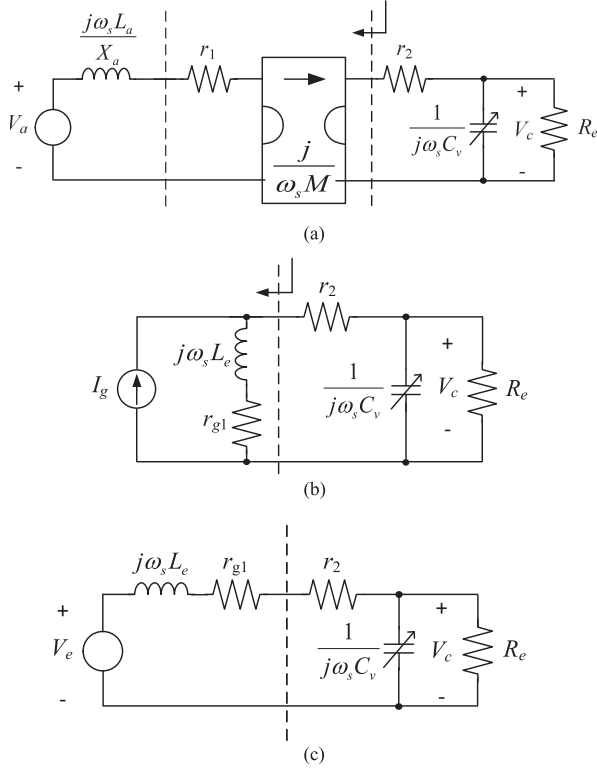


Fig. 6. Simplified final static circuit of the proposed IPT from the load-side viewpoint. (a) Equivalent Thevenin circuit of Fig. 5, assuming that  $L_1$  &  $C_1$  and  $L_2$  &  $C_2$  are fully resonated. (b) Equivalent circuit of (a), eliminating a gyrator. (c) Simplified final static circuit of (b).

Fig. 6(b) as follows [49]:

$$I_g = \frac{jV_a}{X_m} = \frac{jV_1}{X_m X_a} \quad (5a)$$

$$L_e = \frac{-L_a X_m^2 X_a}{r_1^2 X_a^2 + \omega_s^2 L_a^2} > 0 \quad (\because X_a < 0), r_{g1} = \frac{r_1 X_m^2 X_a^2}{r_1^2 X_a^2 + \omega_s^2 L_a^2} \quad (5b)$$

$$\therefore X_m \equiv \omega_s M. \quad (5c)$$

As shown in Fig. 6(c), the simplified final equivalent circuit, which is an LCR parallel resonant circuit, can be obtained, where equivalent source voltage  $V_e$  is as follows:

$$V_e = I_g \cdot (j\omega_s L_e + r_{g1}) = \frac{jX_m V_1}{r_1 X_a + j\omega_s L_a}. \quad (6)$$

As identified from (4b) and (5b), the equivalent inductance  $L_e$  should be positive, i.e.,  $X_a < 0$  ( $\because f_s > f_a$ ), in this paper so that  $L_e$  is regarded as an inductance and the final equivalent circuit is composed of an LCR parallel resonant circuit in Fig. 6(c).

From (5) and (6), the voltage gain  $G_V$  and load power  $P_L$  are finally determined as follows: (7) shown at the bottom of this page.

### B. Source Power $P_S$ and Efficiency $\eta$

The source power  $P_s$  for power efficiency can be calculated from Fig. 7, which shows the equivalent circuit from the source-side viewpoint. By applying the Norton equivalent theorem of Fig. 5 and converting the parallel connection of  $R_e$  and  $C_v$  in Fig. 5 to the series connection, Fig. 5 can be converted to Fig. 7(a), where  $I_s$ ,  $C'_v$  and  $R'_e$  are derived, as follows:

$$I_s = \frac{V_1}{j\omega_s L_a} \quad (8a)$$

$$R'_e = \frac{R_e}{1 + \omega_s^2 C_v^2 R_e^2}, C'_v = \frac{1 + \omega_s^2 C_v^2 R_e^2}{\omega_s^2 C_v R_e^2}. \quad (8b)$$

Similar to Fig. 6(b), by eliminating the gyrator in Fig. 7(a), the simplified final static circuit from the source-side viewpoint can be obtained, as shown in Fig. 7(b), where  $L_g$  and  $r_{g2}$  are defined, as follows:

$$L_g = \frac{C'_v X_m^2}{1 + \omega_s^2 C_v^2 (r_2 + R'_e)^2}, r_{g2} = \frac{\omega_s^2 C_v^2 X_m^2 (r_2 + R'_e)}{1 + \omega_s^2 C_v^2 (r_2 + R'_e)^2}. \quad (9)$$

$$\therefore G_V \equiv \left| \frac{V_c}{V_e} \right| = \frac{R_e}{\sqrt{\{R_e (1 - \omega_s^2 L_e C_v) + r_{g1} + r_2\}^2 + \omega_s^2 \{L_e + C_v R_e (r_{g1} + r_2)\}^2}} \quad (7a)$$

$$P_L \equiv \frac{V_L^2}{R_L} = \frac{|V_c|^2}{R_e} = \frac{R_e |V_e|^2}{\{R_e (1 - \omega_s^2 L_e C_v) + r_{g1} + r_2\}^2 + \omega_s^2 \{L_e + C_v R_e (r_{g1} + r_2)\}^2}. \quad (7b)$$

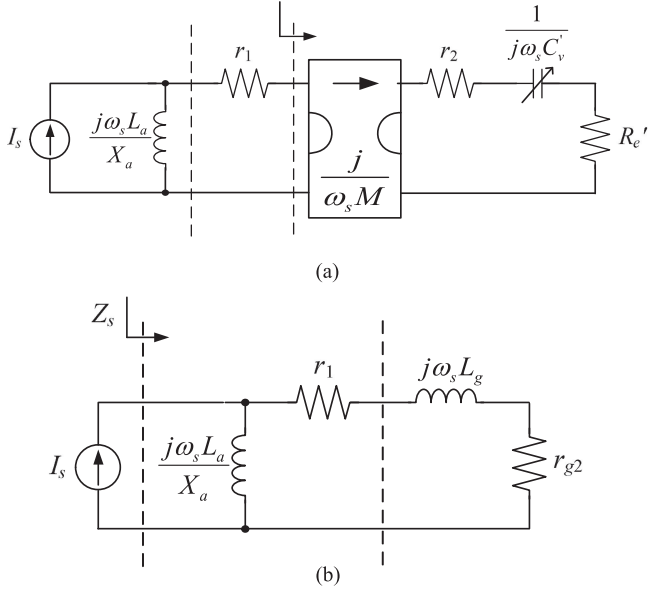


Fig. 7. Simplified final static circuit of the proposed IPT from the source-side viewpoint. (a) Equivalent Norton circuit of Fig. 5. (b) Simplified final static circuit of (a).

Finally, the source power  $P_s$  and the power efficiency  $\eta$  can be determined from (8) and (9) as follows:

$$\therefore P_s = |I_s|^2 \operatorname{Re}\{Z_s\} = \frac{(r_1 + r_{g2}) V_1^2}{\omega_s^2 (L_a + X_a L_g)^2 + X_a^2 (r_1 + r_{g2})^2} \quad (10a)$$

$$\eta = \frac{P_L}{P_s} \quad (10b)$$

$$\begin{aligned} \therefore Z_s &\equiv \frac{j\omega_s L_a}{X_a} // (j\omega_s L_g + r_1 + r_{g2}) \\ &= \frac{j\omega_s L_a (r_1 + r_{g2}) - \omega_s^2 L_a L_g}{j\omega_s (L_a + X_a L_g)^2 + X_a (r_1 + r_{g2})}. \end{aligned} \quad (10c)$$

### C. ZVS Conditions for $M_1$ and $M_2$

Although the distance is widely changed, ZVS conditions of  $M_1$  and  $M_2$  in the half-bridge inverter in Fig. 3 should be guaranteed. Assuming that  $L_1$  and  $C_1$ , and  $L_2$  and  $C_2$  in Fig. 5 are fully resonated, respectively, and the parallel connection of  $R_e$  and  $C_v$  in Fig. 5 is converted to the series connection, then equivalent circuit can be obtained, as shown in Fig. 8(a). Pure imaginary impedances  $j\omega_s L_a$  and  $-j\omega_s L_a$ , which are simply short circuit, are inserted to make another gyrator model [49]. By eliminating a gyrator having  $j/(\omega_s M)$  of forward gain and inserting another gyrator model having  $1/(j\omega_s L_a)$  of forward gain, the simplified static circuit from the source-side viewpoint can be obtained, as shown in Fig. 8(b), where the other circuit transformation process is similar with Fig. 7. Note that capacitive impedance of the gyrator output implies inductive impedance of the gyrator input [49]; hence, the gyrator output impedance should be capacitive, as shown in Fig. 8(b), so that the gyrator input impedance, which corresponds to output of the

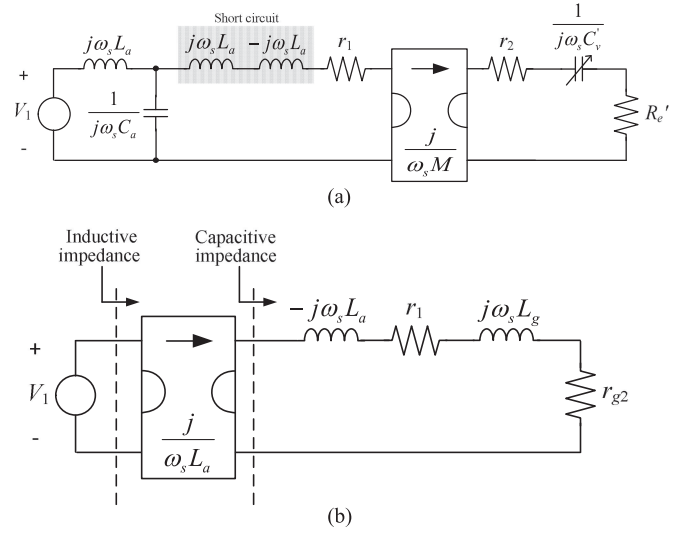


Fig. 8. Simplified static circuit of the proposed IPT from the source-side viewpoint for ZVS conditions of  $M_1$  and  $M_2$ . (a) Equivalent circuit of Fig. 5 by inserting pure imaginary impedances. (b) Simplified static circuit of (a) with ZVS conditions of  $M_1$  and  $M_2$ .

half-bridge inverter, is inductive, as follows:

$$-j\omega_s L_a + j\omega_s L_g < 0 \quad \rightarrow \quad \therefore L_a > L_g. \quad (11)$$

In (11),  $L_g$  can be calculated from (9), whose value depends on the distance  $d$  and switching duty cycle  $D$ . Therefore,  $L_g$  should be always lower than  $L_a$  under load power regulation to satisfy (11), which will be experimentally verified in Section V.

## IV. DESIGN OF THE PROPOSED IPT AND CONTROL CIRCUIT

### A. Design of the Proposed IPT

Throughout this paper, it is assumed that target of load power is set to be 100 W and distance variation range of wireless power delivery is 20–70 cm, considering average power consumptions of home appliances such as television, computer desktops, monitors, and electric rice cookers and typical distance range between home appliances and floor at home. To deliver 100 W of load power at the 70 cm-off maximum distance condition ( $d = d_{\max}$ ), two slim-sized dipole coils are established for Tx and Rx with the Tx reflector, as shown in Fig. 1. The final goal of the proposed design procedure is to regulate the load power when  $d$  severely changes: at least 20–70 cm of distance variation should be managed, considering to account for various types of home appliance WPT, which is the design goal of this paper. Under the given Tx and Rx coil structures,  $L_1$ ,  $L_2$ , and  $M$  in Fig. 5 were experimentally measured when  $d$  decreases from 70 to 20 cm, as listed in Table I, where  $L_1$  includes the effect of the Tx reflector in Figs. 1 and 2. The self-inductance of  $L_1$  and  $L_2$  are slightly increased when  $d$  decreases, whose variation is not so large due to the loosely coupled IPT of the Tx and Rx cores. The physical dimensions and the other parameter selections of the Tx and Rx coils will be discussed in detail in Section V. Throughout this paper, it is assumed that

TABLE I  
MEASURED AND CALCULATED PARAMETERS FOR 100 W PROTOTYPE IPT

$d$ (cm)	$L_1$ ( $\mu\text{H}$ )	$L_2$ (mH)	$M$ ( $\mu\text{H}$ )	$k$	$L_e$ ( $\mu\text{H}$ )	$r_{g1}$ ( $\Omega$ )
70	823	2.270	42	0.031	40	7
60	823	2.271	54	0.039	66	12
50	823	2.273	79	0.058	142	27
40	824	2.275	111	0.081	278	53
30	825	2.279	149	0.108	500	95
20	840	2.312	227	0.163	1,170	222

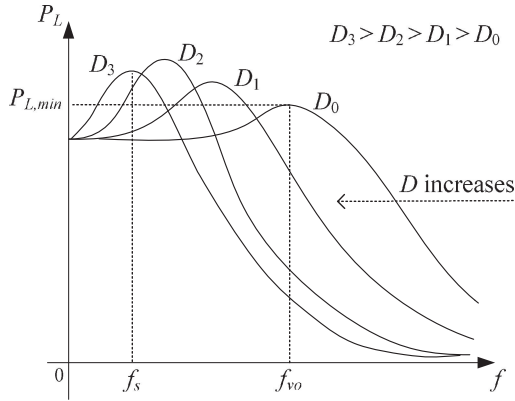


Fig. 9. Characteristic of  $P_L$  w.r.t. frequency  $f$  for various duties at  $d = d_{\max}$ .

the output voltage of the SMPS  $V_{dc}$ , which corresponds to the output voltage of PFC in Fig. 3, is generally 400 V if the utility line voltage is 220 V/60 Hz and the PFC adopts the boost-type converter. The switching frequency is fixed to 140 kHz, considering the international standards of Wireless Power Consortium (WPC), AirFuel Alliance, and EN62233. Instead, the resonant frequency of LC tank  $f_v$  composed of  $L_e$  and  $C_v$  in Fig. 6(c) is modulated by switching duty cycle  $D$  as follows:

$$f_v(D) \equiv \frac{1}{2\pi\sqrt{L_e C_v(D)}}. \quad (12)$$

Therefore, the proposed design focuses on determining the remaining four parameters ( $L_a$ ,  $C_a$ ,  $C_p$ , and  $R_L$ ) for regulating constant nominal load power  $P_{L,\text{nom}}$  with wide-range distance variation ( $d_{\min} \leq d \leq d_{\max}$ ).

To find the appropriate values of those four parameters, the design procedure of the proposed IPT was established to satisfy the three assumptions shown below.

1) At  $d = d_{\max}$ , the initial resonant frequency  $f_{v0}$  when the duty is zero ( $D = D_0$ ) should be larger than the switching frequency  $f_s$  at  $D = D_0$ , as shown in Fig. 9, i.e.,

$$f_{v0} > f_s \quad (\because f_{v0} = \frac{1}{2\pi\sqrt{L_e C_v(D_0)}}, C_v(D_0) = C_p). \quad (13)$$

2) At  $d = d_{\max}$ , because the load power  $P_L$  is just below a nominal load power  $P_{L,\text{nom}}$ , i.e.,  $P_L = P_{L,\text{min}}$  at  $D_0 = 0$  in Fig. 9, the operating point to satisfy  $P_L \geq P_{L,\text{nom}}$  should be reached by modulating  $C_v(D)$ . In other words,  $f_v$  decreases as  $D$

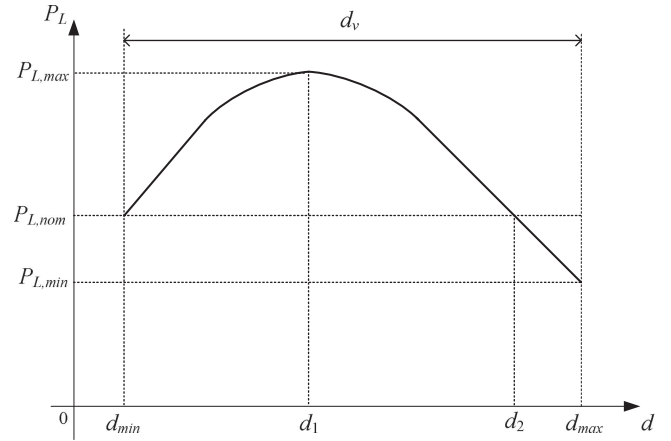


Fig. 10. Characteristic of  $P_L$  w.r.t. distance  $d$  without control of the variable switched capacitance.

increases, and finally  $f_v$  will be equal to  $f_s$  under the condition that  $f_s$  is fixed at  $D = D_3$ , as shown in Fig. 9. To satisfy this condition, the maximum voltage gain  $G_{V,\text{max}}$ , which can be derived from (7a) under  $f_s = f_v$ , should be at least larger than 1 as follows:

$$\begin{aligned} G_{V,\text{max}}|_{d=d_{\max}} &= \frac{R_e}{\sqrt{\{Z_v(D) + R_e(r_{g1} + r_2)/Z_v(D)\}^2 + (r_{g1} + r_2)^2}} \\ &> 1 \quad (\because f_s = f_v) \end{aligned} \quad (14a)$$

$$\because Z_v \equiv \sqrt{\frac{L_e}{C_v}}. \quad (14b)$$

As identified from (14), the maximum point of load power for each switching duty case when  $f_s = f_v$ , which corresponds to the maximum load voltage in (14a), decreases after it increases when the switching duty cycle starts to decrease from  $D_0$ , as shown in Fig. 9.

3) When  $d$  reaches the minimum required distance  $d_{\min}$ ,  $P_L$  should be larger than or equal to  $P_{L,\text{nom}}$  for  $D = 0$ .

As pointed out in the above assumptions, the load power  $P_L$  will vary when the distance  $d$  changes from  $d_{\max}$  to  $d_{\min}$  without the variable switched capacitance, as shown in Fig. 10, where  $d_v$  is applicable distance variation range for constant load power regulation. By the proposed adaptive switching duty modulation to control the variable switched capacitance, the load power can be regulated, i.e., operating points to satisfy  $P_L = P_{L,\text{nom}}$  within  $d_{\min} \leq d \leq d_{\max}$  always exist, as shown in Fig. 11.

To design the baseline of 100 W nominal load power delivery for 20 cm ( $= d_{\min}$ )  $\leq d \leq$  70 cm ( $= d_{\max}$ ) throughout this paper, there are many possible combinations for the selection of those four circuit parameters ( $L_a$ ,  $C_a$ ,  $C_p$ , and  $R_L$ ) based on the design goals with the above assumptions. In other words, it is not possible to analytically determine only one solution of  $L_a$ ,  $C_a$ ,  $C_p$ , and  $R_L$ . Accordingly, one of the possible combinations can be appropriately determined by numerical calculations;  $L_a = 70.0 \mu\text{H}$ ,  $C_a = 36.2 \text{ nF}$ ,  $C_p = 1.0 \text{ nF}$ , and  $R_L = 200 \Omega$  were selected as an example, which is the small

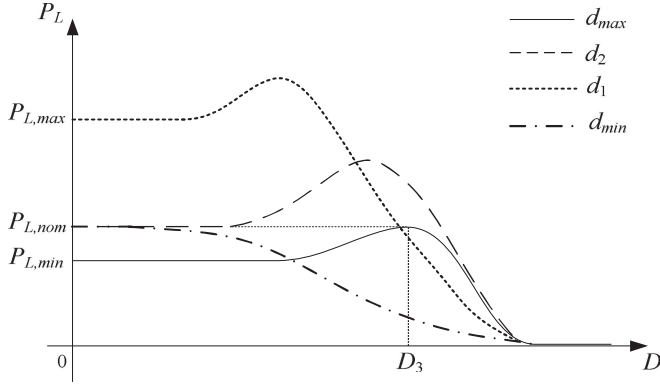


Fig. 11. Characteristic of  $P_L$  w.r.t. duty  $D$  for various distances by the proposed design procedure.

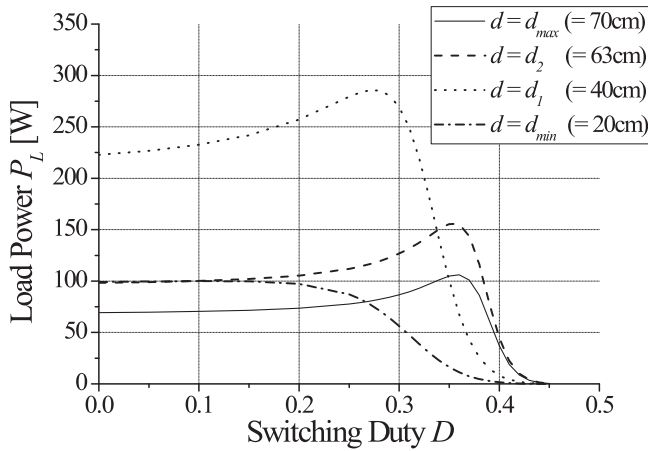


Fig. 12. Calculation results of  $P_L$  w.r.t. duty  $D$  for various distances at  $f_s = 140$  kHz.

$C_p$  case, as identified from Fig. 4(a).  $f_a = 100$  kHz was selected, which satisfies (5b) to make equivalent inductance  $L_e$  at  $f_s = 140$  kHz in Fig. 6(c).

Based on those parameters from the proposed design procedure, the load power was calculated from (7) w.r.t. the switching duty cycle  $D$  and switching frequency  $f_s$ , as shown in Figs. 12 and 13, where  $d_{\max} = 70$  cm,  $d_2 = 63$  cm,  $d_1 = 40$  cm, and  $d_{\min} = 20$  cm were found by calculation results. The conversion ratio  $\alpha$  in (2) is selected as 0.75, whose selection will be discussed in detail in Section VI. The other parameters w.r.t. the distance  $d$  by the proposed static analysis are summarized in Table I. In Figs. 12 and 13(a), the load power is over 100 W of the nominal load power at  $D = 0.35$  for  $d = 70$  cm, and  $D = 0$  for  $d = 20$  cm, as identified from Figs. 10 and 11.  $f_v$  moves from  $f_{v0}$  to  $f_s$  in Fig. 9 as  $D$  increases and load power becomes maximum value when  $f_v = f_s = 140$  kHz, i.e.,  $D = 0.35$ , as shown in Fig. 13(a). For  $d < 20$  cm, there is no satisfaction point for  $P_L = 100$  W by modulating  $D$  in Fig. 12, i.e.,  $d < 20$  cm would not be covered for load power regulation. Nevertheless, applicable distance variation range of  $d_v = 50$  cm in this paper may be enough by this extremely loosely coupled IPT for home appliance applications. Therefore, it is found that the variable switched capacitance can be appropriately modulated by

controlling  $D$  so that load power is regulated for  $d_v = 50$  cm, according to the proposed design procedure.

### B. Operating Principle of the Proposed Control Circuit

To implement the functionality of the variable switched capacitance, it is important to achieve the soft switching operations of  $S_1$  and  $S_2$  for a reliable operation and high power efficiency of the proposed IPT. The proposed control circuit senses the drain-source voltages of both  $S_1$  and  $S_2$  and feeds the gate signals  $v_{gs1}$  and  $v_{gs2}$ ; the signal and sensing grounds are the same, and cumbersome isolation circuits such as optocoupler are not necessarily used in the proposed IPT. Simply by voltage dividers composed of  $R_3$  and  $R_4$ , as shown in Fig. 3, the drain-source voltages of  $S_1$  and  $S_2$  can be sensed as  $v_{da1}$  and  $v_{da2}$ , respectively, and compared to threshold voltage  $v_{th}$ , as shown in Fig. 14. Then, the rising edges of  $v_{d1}$  and  $v_{d2}$  are detected by MCU, and appropriate gate signals  $v_{gs1}$  and  $v_{gs2}$  are finally applied to main switches  $S_1$  and  $S_2$  through the gate drivers.

The detailed operating principle of the proposed control circuit for ZVS operation will be described in the following operating mode analysis, which includes four modes, as shown in Figs. 14 and 15. It is assumed that the equivalent resistances  $r_{g1}$  and  $r_2$  in Fig. 6(c), the drain-source capacitances of two switches  $S_1$  and  $S_2$ , the voltage drop of the all diodes, and the ESRs of all capacitors are neglected in this section for simplicity of analysis. The main switches  $S_1$  and  $S_2$  are the positive and negative polarity operations, respectively. The equivalent voltage  $v_e$  in Fig. 6(c) is represented as a sinusoidal waveform instead of including all of the parameter components for easily explanation. The operating modes begin when the secondary current  $i_2 (= i_{cp} + i_c)$  is just increased.

**Mode 1** [ $t_0, t_1$ ]: At  $t_0$ , the main switches  $S_1$  and  $S_2$  are turned OFF, as shown in Fig. 15(a). Nevertheless, the gate signal  $v_{gs1}$  was already applied even before the zero-crossing point that changes from negative to positive polarities of  $v_c$  for ZVS operation of  $S_1$ . Because  $v_c$  was negatively charged to  $-V_L$  in the previous mode, it goes to zero through the positive current of  $i_{cp}$ , as follows:

$$v_c(t) = -V_L \cos \omega_v(t - t_0) \text{ for } t_0 < t < t_1 \quad (15a)$$

$$i_{cp}(t) = i_2(t) = \frac{V_E \sin \omega_s t_0 + V_L}{\omega_1 L_e} \times \sin \omega_v(t - t_0) \text{ for } t_0 < t < t_1 \quad (15b)$$

$$\therefore \omega_v \equiv \frac{1}{\sqrt{L_e C_p}}, v_e = V_E \sin \omega_s t \quad (15c)$$

This mode ends when  $v_c$  changes from  $-V_L$  to 0, and the time interval  $t_{10}$  is determined as follows:

$$t_{10} \cong \frac{\pi}{2\omega_v}. \quad (16)$$

**Mode 2** [ $t_1, t_2$ ]: At  $t_1$ , the switch  $S_1$  and the body diode of switch  $S_2$  are just turned ON, as shown in Fig. 15(b). In this case, because  $v_{ds1}$  was previously zero at the polarity transition point of  $t = t_1$  and  $v_{gs1}$  was already applied, the ZVS operation of  $S_1$

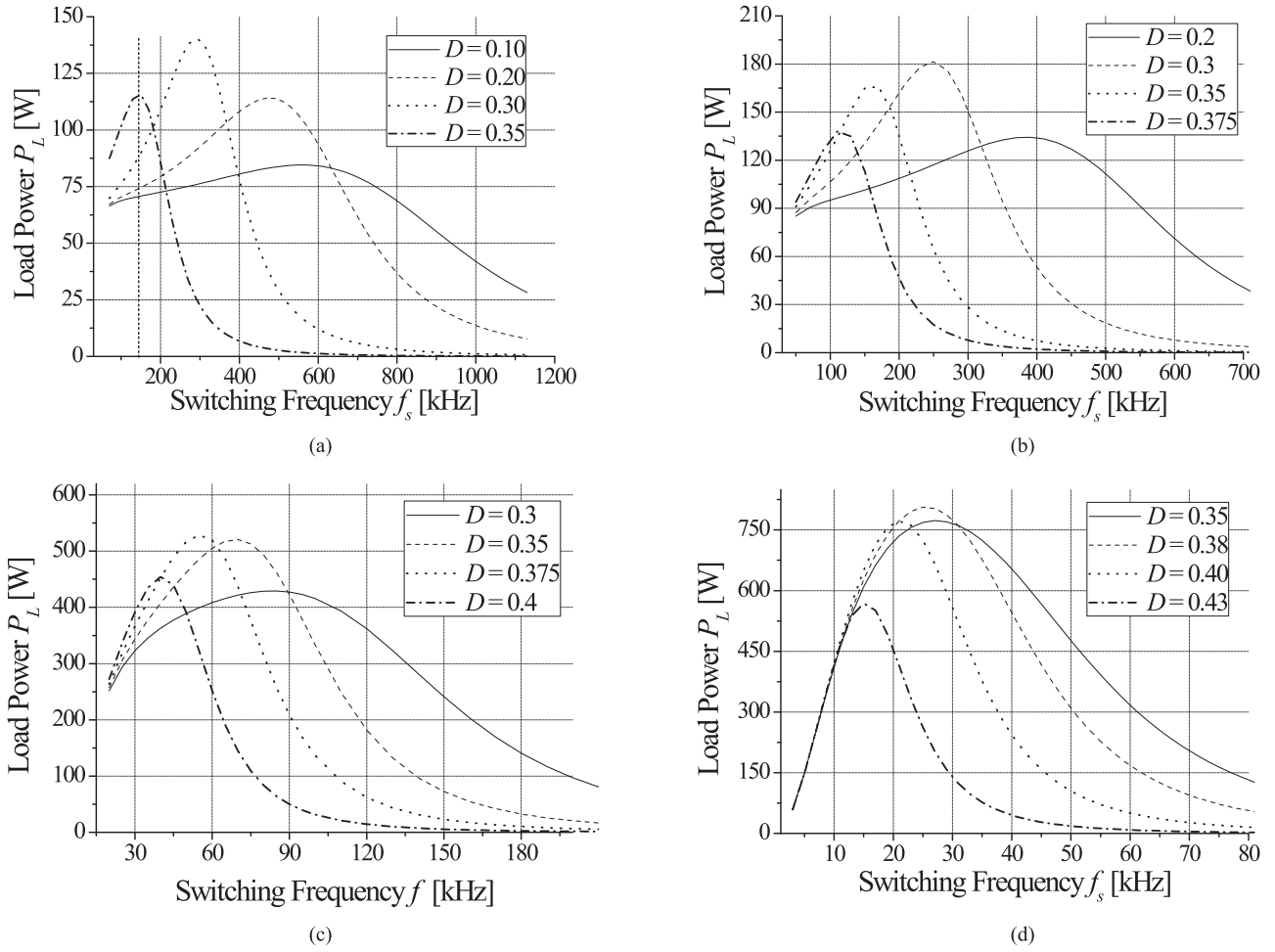


Fig. 13. Calculation results of  $P_L$  w.r.t.  $f_s$  for various duty  $D$ . (a)  $d = d_{max}$ . (b)  $d = d_2$ . (c)  $d = d_1$ . (d)  $d = d_{min}$ .

is surely guaranteed. Then,  $i_c$  is simply determined as follows:

$$i_c(t) = i_2(t) = -\frac{V_E}{\omega_s L_e} (\cos \omega_s t - \cos \omega_s t_1) + i_2(t_1) \text{ for } t_1 < t < t_2. \quad (17)$$

This mode ends when  $S_1$ , whose duty cycle is arbitrarily controlled to regulate the load power, is turned OFF.

**Mode 3** [ $t_2, t_3$ ]: At  $t_2$ , the switch  $S_1$  is just turned OFF, as shown in Fig. 15(c). Then,  $v_c$  is determined, where  $i_2$  is assumed to be constant for a short time period of this mode as follows:

$$v_c(t) \cong \frac{1}{\omega_v C_p} \left( i_2(t_2) - \frac{V_E}{\omega_s L_e} \cos \omega_s t_2 \right) \times \sin \omega_v (t - t_2) \text{ for } t_2 < t < t_3. \quad (18)$$

During this mode, a rising edge of  $v_{d1}$  is detected by MCU, as shown in Fig. 3. In this way, the gate signal for negative polarity operation of  $v_{gs2}$  will be turned on after the delay time  $t_d$ , which can be arbitrarily chosen in the MCU, considering the switching frequency, e.g.,  $t_d = 1.0 \mu\text{s}$  for  $f_s = 140 \text{ kHz}$  throughout this paper.

This mode ends when  $v_c$  reaches  $V_L$ , and the time interval  $t_{32}$  can be straightforwardly determined from (18) as follows:

$$t_{32} \cong \frac{1}{\omega_v} \sin^{-1} \left( \frac{\omega_v \omega_s L_e C_p V_L}{\omega_s L_e i_2(t_2) - V_E \cos \omega_s t_2} \right). \quad (19)$$

**Mode 4** [ $t_3, t_4$ ]: At  $t_3$ , the diode  $D_1$  and the body-diode of the switch  $S_2$  are turned ON as a result of  $v_c(t_3) = V_L$ . Then,  $i_2$  can be determined as follows:

$$i_2(t) = \frac{V_E}{\omega_s L_e} (\cos \omega_s t_3 - \cos \omega_s t) - \frac{V_L}{L_e} (t - t_3) + i_2(t_3) \text{ for } t_3 < t < t_4 \quad (20)$$

During this mode,  $v_{gs2}$  is applied to  $S_2$ , and margin time  $t_m (> 0)$  is enough to achieve the ZVS operation of  $S_2$  until the next polarity transition point, as shown in Fig. 15(d). This mode ends when  $i_2$  in (20) becomes zero.

As shown in Fig. 3, load power  $P_L$  can be sensed by load voltage and current sensing circuits, and calculated by the MCU for load power regulation. Thus, the feedback of load power  $P_L$ ,  $f$  can be obtained and compared to the reference load power  $P_L$ ,  $r$ , corresponding to 100 W in this paper. Through this negative feedback control loop by digital controller, an appropriate

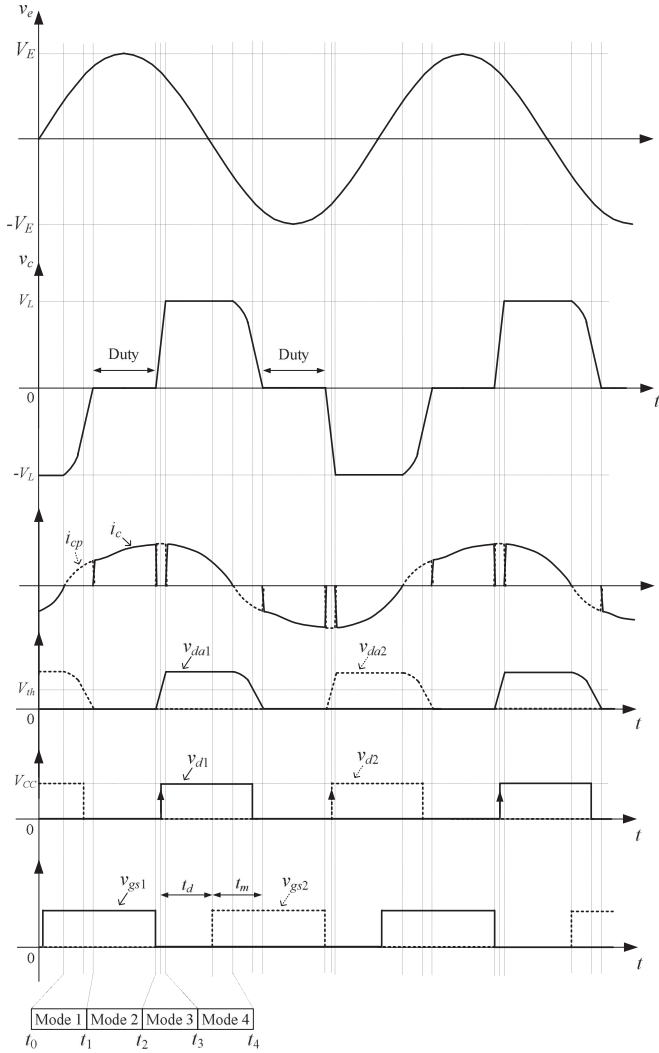


Fig. 14. Waveform diagrams of the proposed IPT.

switching duty cycle  $d$  for S1 and S2 is finally determined by the PI control routine by MCU coding for load power regulation against distance variations. Those contents are omitted due to its simple coding tasks in this paper.

## V. EXPERIMENTAL VERIFICATIONS

The design results for the baseline of 100 W IPT will be experimentally verified in this section. In this application, if the coil distance is fixed after installation, it is hardly possible to move Tx or Rx coil due to its large and heavy structures of the proposed IPT. Even though utility line voltage  $V_s$  changes, the PFC of SMPS in Fig. 3 shall control the regulated  $V_{dc}$ , which corresponds to the input voltage of the proposed IPT. Due to such reasons, dynamic regulation performances by distance  $d$  and utility line voltage  $V_s$  variations are out of scope in this paper.

### A. Fabrication and Parameters Selection

The analysis and design considerations of the proposed IPT are verified by an experimental kit of 100 W load power delivery at the wide-range distance variations of  $20 \text{ cm} \leq d \leq 70 \text{ cm}$ . As shown in Fig. 16(a), the fabricated size of the Tx and Rx

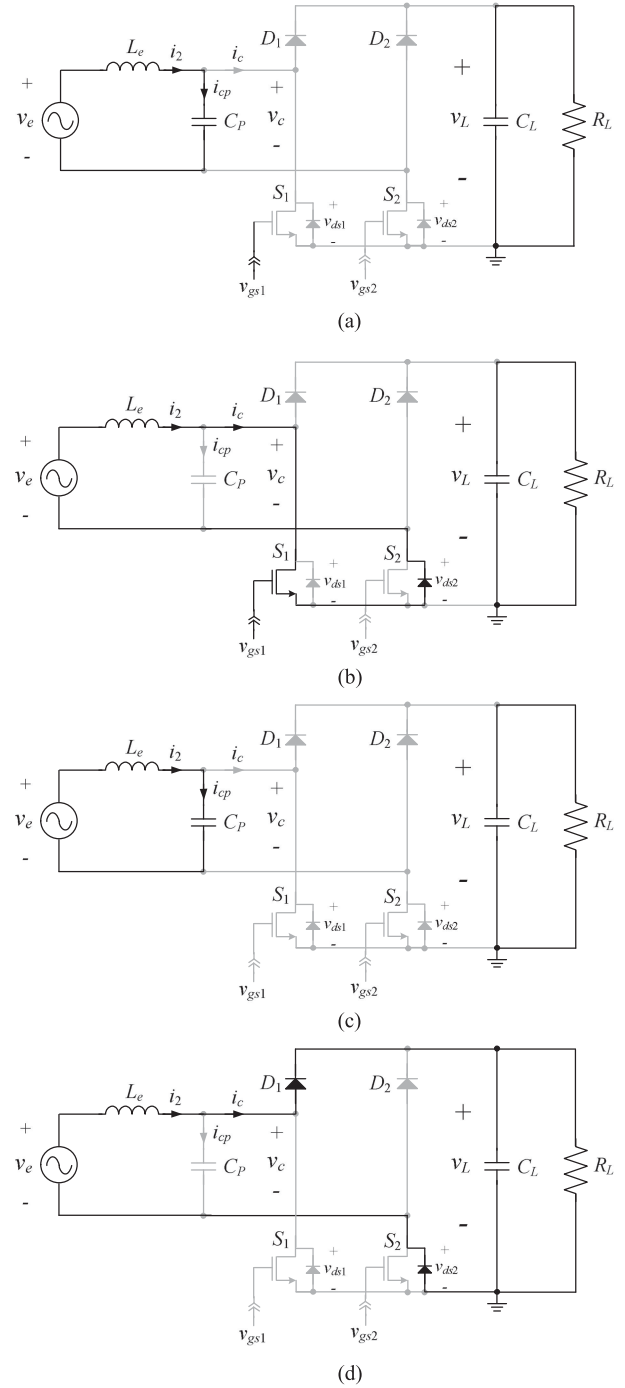


Fig. 15. Operating modes of the proposed IPT. (a) Mode 1. (b) Mode 2. (c) Mode 3. (d) Mode 4.

coils are  $100 \text{ cm} \times 5.0 \text{ cm} \times 5.0 \text{ cm}$  and  $100 \text{ cm} \times 2.5 \text{ cm} \times 5.0 \text{ cm}$ , respectively, with an optimized stepped core structure, considering the characteristics of the used core, total weight, and length in this paper [14]–[15]. An aluminum plate, whose length, width, and thickness are 150 cm, 15 cm, and 2 mm, respectively, is adopted as the Tx reflector, which blocks the magnetic flux behind the Tx reflector for human safety and reflects the magnetic flux generated from the Tx coil to Rx coil [23]. The number of turns for Tx and Rx coils  $N_1$  and  $N_2$  are 40 and 70, respectively, and litz wire having 3.0 mm

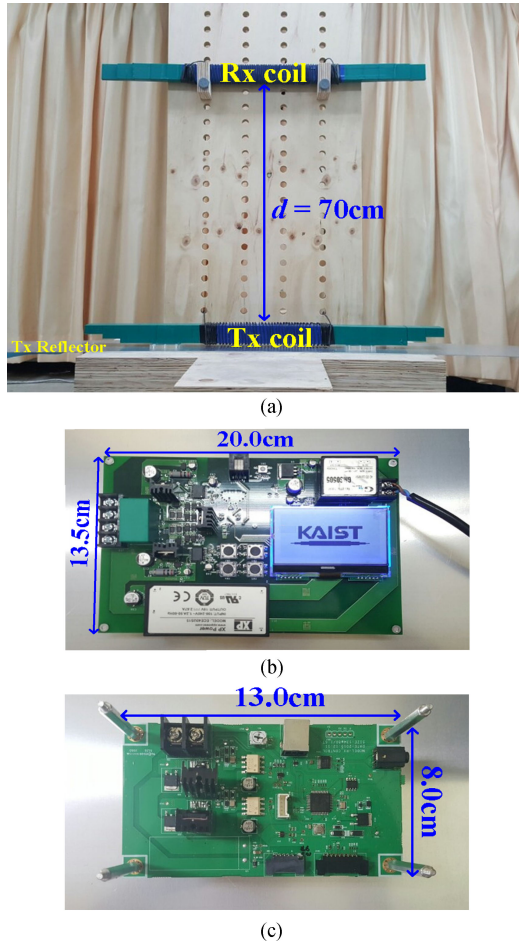


Fig. 16. Fabricated prototype of the proposed IPT for 100 W load power delivery. (a) Fabricated Tx and Rx coils. (b) Asymmetric half-bridge inverter. (c) Rectifier and control circuit for the variable switched capacitance.

TABLE II  
PARAMETER SELECTIONS OF THE PROPOSED IPT

Parameters	Values	Parameters	Values
$r_1$	8.0 $\Omega$	$C_3$	0.1 $\mu\text{F}$
$r_2$	18.0 $\Omega$	$C_4$	0.1 $\mu\text{F}$
$R_3$	620 k $\Omega$	$C_L$	5.0 $\mu\text{F}$
$R_4$	10 k $\Omega$	$V_{th}$	3.3 V
$R_5$	750 k $\Omega$	MCU	STM32F105RCT6
$R_6$	10 k $\Omega$	Comparator	TLV3502
$R_7$	0.2 $\Omega$	$GD_1, GD_2$	TLP250
$R_8$	3.9 k $\Omega$	$S_1, S_2$	STD10NM60N
$R_9$	200 k $\Omega$	$D_1 \sim D_2$	QD606S
$R_{1,0}$	300 k $\Omega$	$n_1$	40
$C_1$	1.57 nF	$n_2$	70
$C_2$	570 pF		

diameter of thickness was adopted for Tx and Rx windings. The measured internal resistances of the Tx and Rx coils  $r_1$  and  $r_2$  in Fig. 3 were 8.0  $\Omega$  and 18.0  $\Omega$ , respectively, and the series resonant capacitors  $C_1$  and  $C_2$  were selected as 1.57 nF and 570 pF to fully resonate with  $L_1$  and  $L_2$ , respectively. The sensing resistors  $R_3$  and  $R_4$  are selected as 620 k $\Omega$  and 1.0 k $\Omega$ , considering maximum load voltage level of 300 V to compare  $V_{th}$  in Fig. 14, which is generated from the MCU for threshold

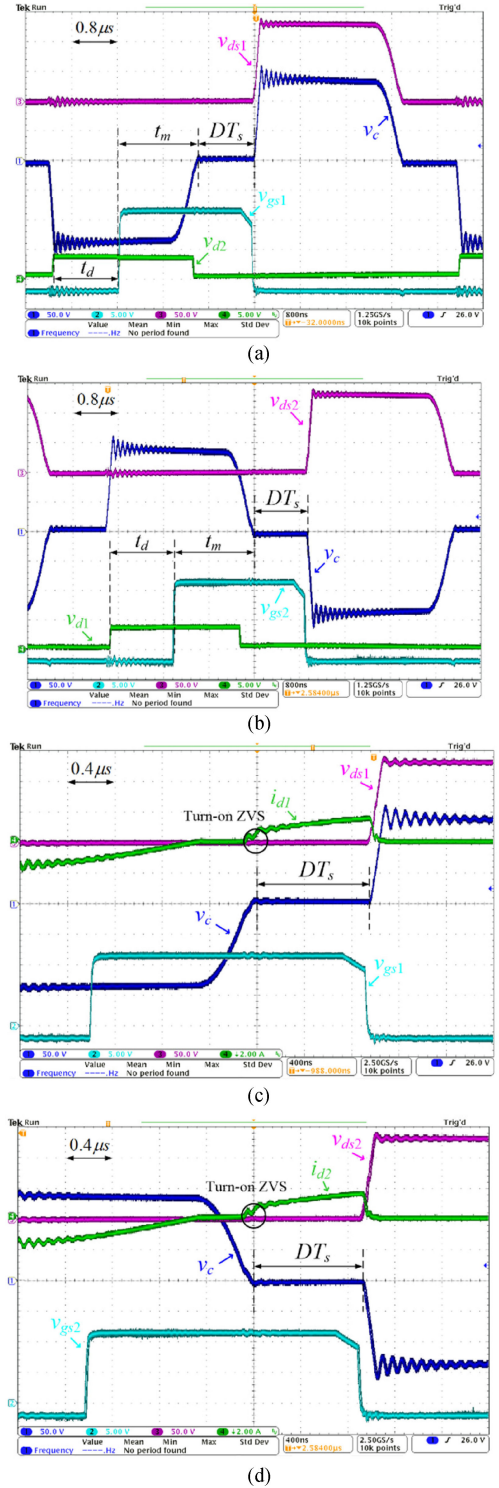


Fig. 17. Experimental waveforms of the proposed control circuit for ZVS operations of  $S_1$  and  $S_2$  at  $d = d_{max}$  for  $P_L = 100$  W. (a)  $v_c$ ,  $v_{gs1}$ ,  $v_{ds1}$ , and  $v_{d2}$ . (b)  $v_c$ ,  $v_{gs2}$ ,  $v_{ds2}$ , and  $v_{d1}$ . (c)  $v_c$ ,  $v_{gs1}$ ,  $v_{ds1}$ , and  $i_{d1}$ . (d)  $v_c$ ,  $v_{gs2}$ ,  $v_{ds2}$ , and  $i_{d2}$ .

voltage:  $V_{th} = 3.3$  V.  $R_5 \sim R_{10}$  with an op-amp is adopted for simply dividing load voltage and sensing load current [38]. A high-frequency operation film capacitor having a capacitance of 5  $\mu\text{F}$  was selected for  $C_L$  and the small size of external dc-dc converters, which were connected to the load in parallel, were used to provide  $V_{CC}$ ,  $V_{EE}$  with gate drivers, a comparator, an

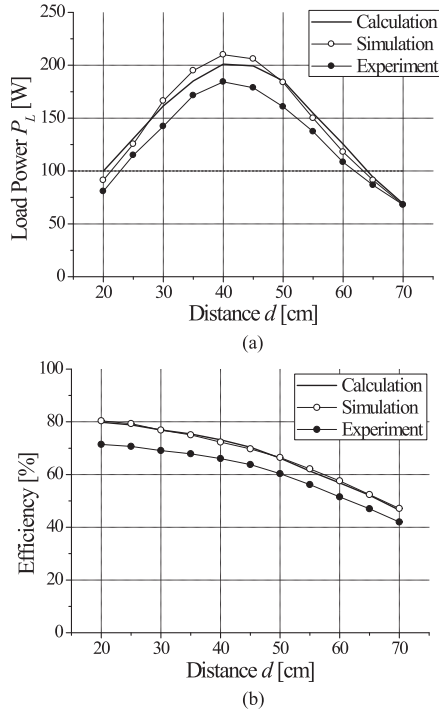


Fig. 18. Experimental results of  $P_L$  and  $\eta$  when  $d$  changes without the variable switched capacitance, compared with the calculation and simulation results. (a)  $P_L$ , (b)  $\eta$

op-amp, and the MCU. All the parameter values are summarized in Table II based on the design principles.

### B. ZVS Operation of the Variable Switched Capacitance Circuit

As identified from Figs. 14 and 15, the operations of the proposed control circuit were experimentally verified for ZVS operations of  $S_1$  and  $S_2$ , as shown in Fig. 17. The rising edge of  $v_{d2}$  or  $v_{d1}$  is detected by the MCU, and gate signal  $v_{gs1}$  or  $v_{gs2}$  is applied after  $t_d$ , as shown in Fig. 17(a) and (b);  $t_m$  was measured as  $1.44 \mu\text{s}$  when  $t_d = 1.0 \mu\text{s}$  for both positive and negative polarities, whose value is still enough to achieve ZVS operations of  $S_1$  and  $S_2$ . As a result, the turn-on ZVS operations of  $S_1$  and  $S_2$  were successfully achieved, as shown in Fig. 17(c) and (d), where the turn-OFF ZVS operation will be guaranteed if slow increases of  $v_{ds1}$  and  $v_{ds2}$  are achieved by the reasonable or large  $C_p$  case, as identified from Fig. 4(b) and (c).

### C. Load Power Regulation

As identified from Fig. 10 for the proposed design procedure, the characteristics of the load power and power efficiency of the proposed IPT when  $d$  changes from  $d_{\text{max}}$  to  $d_{\text{min}}$  without the variable switched capacitance were verified by simulations and experiments, as shown in Fig. 18. The experimental results showed good agreements with the calculation and simulation results, where a PSIM simulation was performed for the circuit of Fig. 3 without a control circuit. The major discrepancy between the calculation and simulation results is the constant value of  $\alpha$  ( $= 0.75$ ) under wide-range distance variation for calculation results from (2)–(7). From Fig. 18, it was experimen-

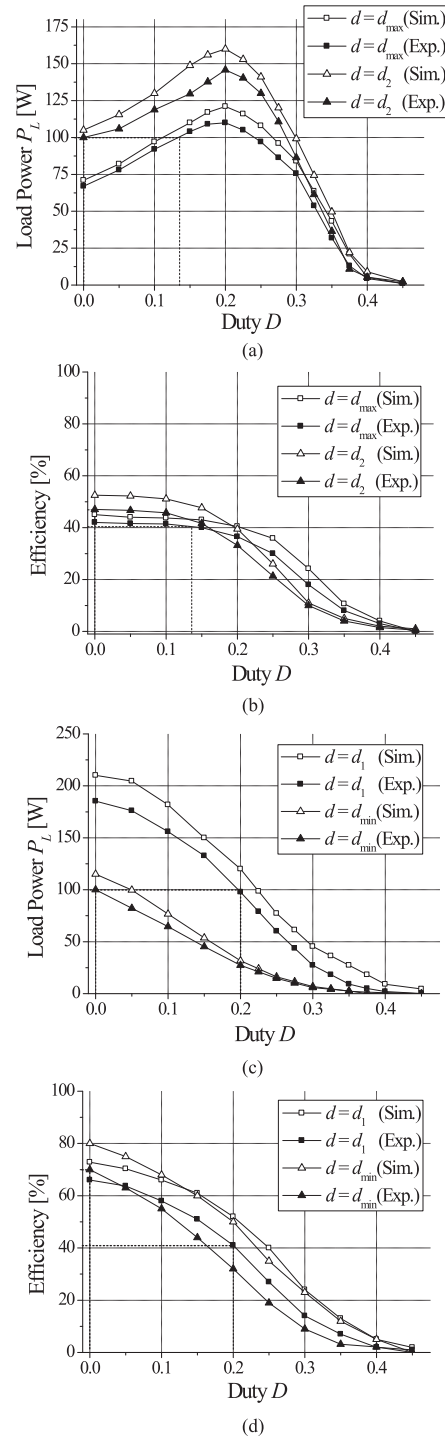


Fig. 19. Experimental results of  $P_L$  w.r.t.  $D$  for various  $d$ . (a)  $P_L$  for  $d_{\text{max}}$  and  $d_2$ , (b)  $\eta$  for  $d = d_{\text{max}}$  and  $d_2$ , (c)  $P_L$  for  $d = d_1$  and  $d = d_{\text{min}}$ , (d)  $\eta$  for  $d = d_1$  and  $d_{\text{min}}$ .

tally found that  $d_{\text{max}} = 70 \text{ cm}$ ,  $d_2 = 62 \text{ cm}$ ,  $d_1 = 40 \text{ cm}$ , and  $d_{\text{min}} = 23 \text{ cm}$ , and the load power was completely regulated to 100 W by the variable switched capacitance under a wide-range of distance variation  $d_v = 47 \text{ cm}$ .

The major behaviors of the variable switched capacitance were verified by simulations and experiments, as shown in Fig. 19. The discrepancies between simulation and experiment results in Figs. 18 and 19 are due to conduction losses of

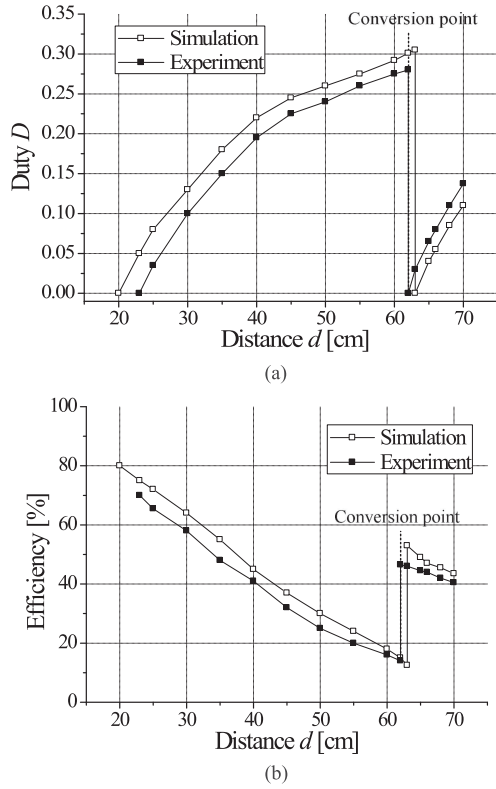


Fig. 20. Experimental results of  $D$  and  $\eta$  for the distance variation, satisfying  $P_L = 100$  W by  $D$ . (a)  $D$ , (b)  $\eta$ .

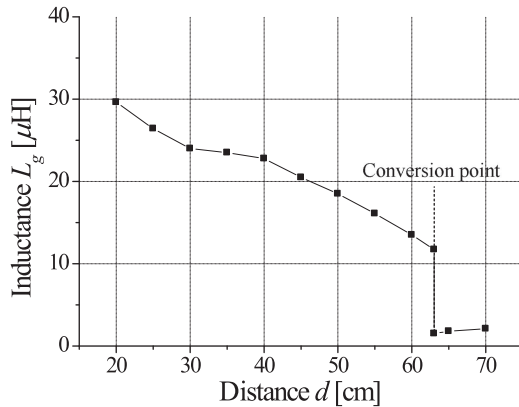


Fig. 21. Inductance  $L_g$  variation when load power is regulated by the variable switched capacitance, satisfying  $P_L = 100$  W for ZVS operations of  $M_1$  and  $M_2$ .

internal resistance of  $L_a$ , the half-bridge inverter in Tx circuit, and a diode rectifier in Rx circuit, which are not considered in calculation results and simulation verifications. The measured values do not perfectly match the calculation results in Fig. 12, e.g., the peak value of the  $P_L$  at  $d = d_{\max}$  was measured as  $D = 0.2$ , whereas the calculation value was  $D = 0.35$ . Nevertheless, it is clear that the tendency and characteristics of the proposed IPTS are the same, and the performance of the proposed IPT works perfectly. The major reason for this discrepancy is the nonlinearity of  $v_c$ , i.e., the calculated values of the equivalent capacitance determined by  $D$  in (1) did not

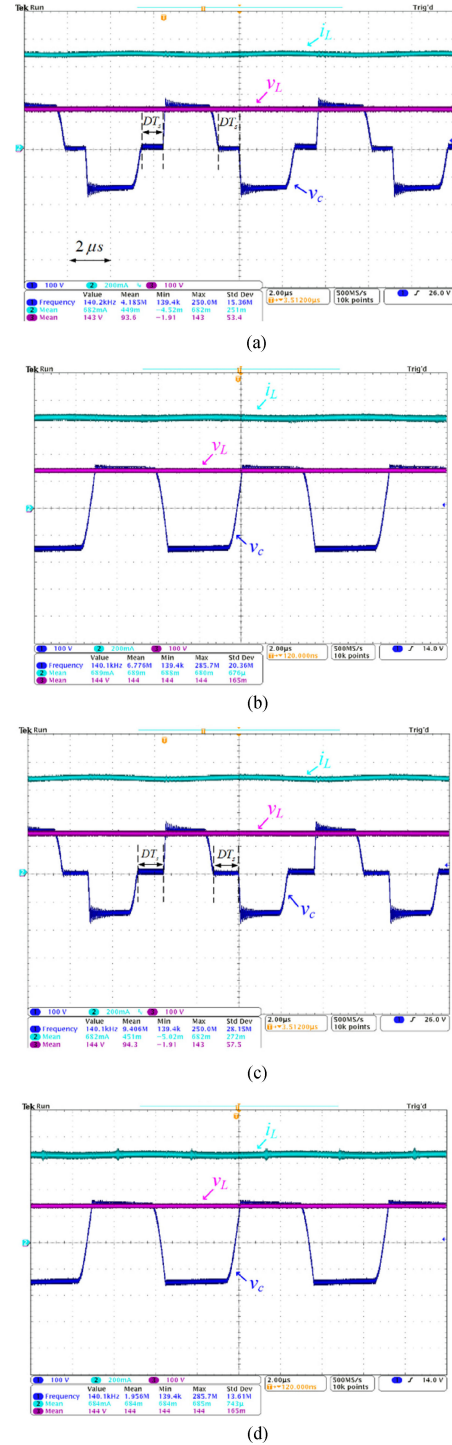


Fig. 22. Experimental waveforms of  $v_c$ ,  $v_L$ , and  $i_L$  for various distances, satisfying  $P_L = 100$  W. (a)  $d = d_{\max}$ , (b)  $d = d_{d2}$ , (c)  $d = d_{d1}$ , (d)  $d = d_{\min}$ .

match well with the simulation and experiment due to a small value of  $C_p$  ( $= 1$  nF) in this paper, as identified from Section II. Therefore, it is not possible to analytically find the exact value of the equivalent capacitance of  $C_V$  determined by  $D$  for this nonlinearity case, considering the conversion ratio of  $\alpha$ .

The optimum duty, satisfying  $P_L = 100$  W under distance variation, can be found from Figs. 18 and 19, as shown in Fig. 20, where conversion point exists. It is because two duty points,

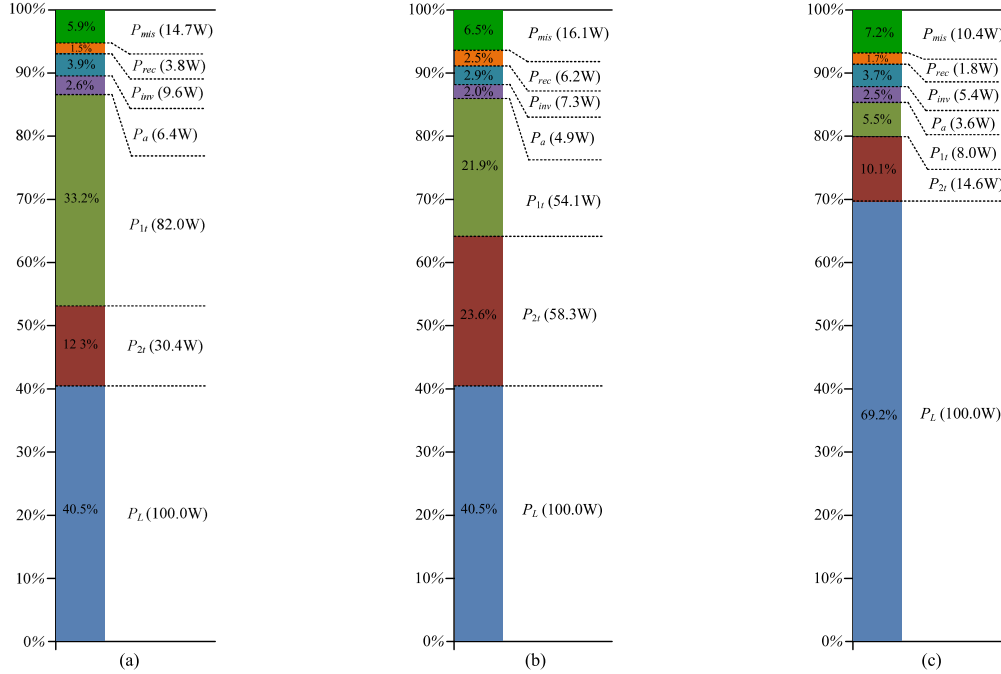


Fig. 23. Power loss analysis of the proposed IPTS. (a)  $d = d_{\max}$ , (b)  $d = d_{d1}$ , (c)  $d = d_{\min}$ .

satisfying  $P_L = 100$  W, exist below conversion point range, which corresponds to  $d_2 \leq d \leq d_{\max}$  ( $62 \text{ cm} \leq d \leq 70 \text{ cm}$ ), as shown in Fig. 19(a). Even though both duty points are available for  $P_L = 100$  W, a lower duty is recommended due to its higher efficiency for  $d_2 \leq d \leq d_{\max}$ , as shown in Fig. 19(b). Concerning control method of adopting a lower duty among two duty points for  $d_2 \leq d \leq d_{\max}$ , switching duty cycle  $D$  starts to be increase from zero until  $P_L = 100$  W at the beginning of the control operation. If  $P_L = 100$  W,  $D$  will stop to increase, which corresponds to a lower duty operation, implemented by MCU in Fig. 3. Therefore, a lower duty is automatically chosen as an optimum duty point for high efficiency. On the other hands, above conversion point range, which corresponds to  $d_{\min} \leq d < d_2$  ( $23 \text{ cm} \leq d < 62 \text{ cm}$ ), only one duty point exists for  $P_L = 100$  W in Fig. 19(c). The ZVS operations of  $M_1$  and  $M_2$  were experimentally verified, as shown in Fig. 21, where  $L_g$  was calculated from (9) based on the distance  $d$  and switching duty cycle  $D$ . In Fig. 21,  $L_g$  is always lower than  $L_a (= 70 \mu\text{H})$ , which satisfies (11) for ZVS conditions of  $M_1$  and  $M_2$ . As shown in Fig. 22, which shows the regulated  $v_L$ ,  $i_L$ , and  $v_c$ , the load voltage and current were well regulated to constant values, which corresponds to 100 W of nominal load power  $P_{L,\text{nom}}$ . As a result, 40.5%, 46.1%, 40.5%, and 69.2% were achieved for  $d = d_{\max}$ ,  $d_2$ ,  $d_1$ , and  $d_{\min}$ , respectively, for  $P_L = 100$  W with 47 cm of very wide-range distance variations.

Although it is not possible to measure all the detail power losses, the power loss analysis of the proposed IPT for three cases is presented, as shown in Fig. 23, where parameter remarks are summarized in Table III. All power losses can be calculated or measured except for the miscellaneous loss, which is the remaining discrepancy that cannot be explained.  $P_{1t}$  and  $P_{2t}$  can be found by measuring  $I_1$ ,  $r_1$ ,  $I_2$ , and  $r_2$ ; however, each component of power loss in  $P_{1t}$  and  $P_{2t}$  cannot be exactly separated

TABLE III  
NOMENCLATURES FOR POWER LOSS ANALYSIS

Parameters	Remarks	Parameters	Remarks
$P_{\text{mis}}$	Miscellaneous loss	$P_{1h}$	Hysteresis loss of Tx coil
$P_{\text{rec}}$	Conduction loss in rectifier for Rx coil	$P_{2t}$	Total loss in Rx coil ( $= P_{2c} + P_{2e} + P_{2h}$ )
$P_{\text{inv}}$	Conduction loss in inverter for Tx coil	$P_{2c}$	Copper loss of Rx coil
$P_a$	Conduction loss by $L_a$ and $C_a$	$P_{2e}$	Eddy current loss of Rx coil
$P_{1t}$	Total loss in Tx coil ( $= P_{1c} + P_{1e} + P_{1h}$ )	$P_{2h}$	Hysteresis loss of Rx coil
$P_{1c}$	Copper loss of Tx coil	$P_L$	Load power
$P_{1e}$	Eddy current loss of Tx coil		

by calculation or experiment, i.e.,  $P_{1e}$ . Hysteresis losses  $P_{1h}$  and  $P_{2h}$ , which are the major source of  $P_{1t}$  and  $P_{2t}$  in Fig. 23, were roughly occupied by 30–40% of  $P_{1t}$  and  $P_{2t}$  by Steinmetz equation calculations [14]. Dominant losses are found to be  $P_{1t}$  and  $P_{2t}$ , whose loss portions become decrease when the distance decreases due to decrement of Tx and Rx coil currents of  $I_1$  and  $I_2$ . Especially,  $P_{2t}$  at  $d = d_1$  becomes relatively larger compared to the other distance cases, which mainly comes from large switching duty cycle of proposed variable switched capacitance, as identified from Fig. 20(a). Therefore, a better ferrite core will be required to be developed in order to improve the power efficiency for the long distance IPT.

## VI. EVALUATION OF THE CONVERSION RATIO BY EXPERIMENT

It has been proven that the conversion ratio  $\alpha$  in (2) is nearly 0.9 in the case of the CCM of the diode rectifier [42]–[46]. However, in the case of the DCM of the diode rectifier, it

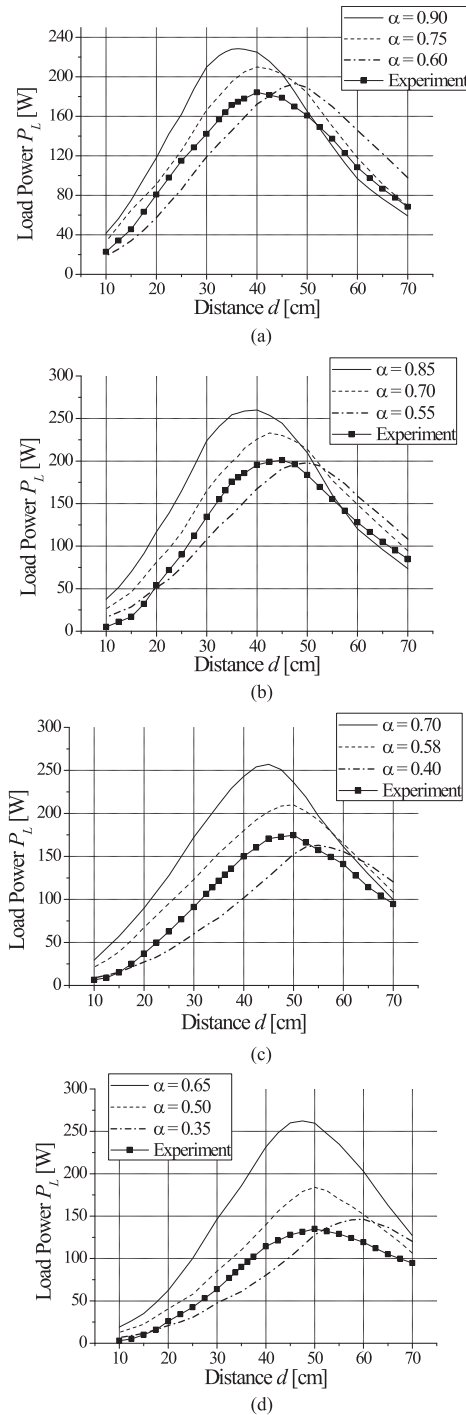


Fig. 24. Comparison of the experimental results with theoretical results by different conversion ratio  $\alpha$  for various  $C_p$ . (a)  $C_p = 1.0$  nF. (b)  $C_p = 2.2$  nF. (c)  $C_p = 4.4$  nF. (d)  $C_p = 6.8$  nF.

is almost impossible to analytically find the exact value of  $\alpha$  for different charging times of  $t_{c1}$  and  $t_{c2}$  in Fig. 4 due to its nonlinearity of  $v_c$  [42]–[46]. Note that if an effective turn-ON period of the diode rectifier is reduced by large parallel capacitance  $C_p$ ,  $\alpha$  decreases; hence,  $\alpha$  is determined by  $C_p$  if other parameters are fixed, and  $\alpha$  cannot be arbitrarily chosen for the design procedure. Instead, the optimum values of  $\alpha$  for different  $C_p$  have been found by comparing the experimental results

with the theoretical results of load power from (7), as shown in Fig. 24.

As identified from Fig. 24, the different optimum values of  $\alpha$  are found according to  $C_p$  where all parameter conditions are identical:  $\alpha = 0.75, 0.70, 0.58,$  and  $0.50$  for  $C_p = 1.0$  nF,  $2.2$  nF,  $4.4$  nF and  $6.8$  nF, respectively. It is certain that large  $C_p$  requires a small value of  $\alpha$ , and this is why  $\alpha$  was selected as  $0.75$  for  $C_p = 1$  nF throughout this paper.

## VII. CONCLUSION

Dipole-coil-based IPT with the Tx reflector, which regulates the load power successfully under very wide-range distance variation, has been fully verified throughout this paper. The load power of 100 W was completely regulated by the variable switched capacitance, and no bulky passive components such as inductors, transformers, and electrolytic capacitors were used in the Rx circuit, which makes the proposed IPT system simple, compact, and low cost manufacture. By proposed gyrator-based static analysis and secondary control circuit, reliable ZVS conditions of both  $M_1 \& M_2$  and  $S_1 \& S_2$  have been successfully realized. As a result, the Tx and Rx coils can be arbitrarily placed within 47 cm of very wide-range distance variation, which is one of the main issues for WPT applications. Therefore, it is expected that the proposed IPT can be applied to not only home appliances, which usually require power consumptions of around 100 W, but also high power applications, e.g., electric vehicles having larger than 1 kW, by virtue of the variable switched capacitance capable of adaptive modulation of LC resonant frequency.

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